

# KNOT THEORY

*Editors of the Volume*

V A U G H A N F. R. J O N E S

J O A N N A K A N I A - B A R T O S Z Y N S K A

J Ó Z E F H. P R Z Y T Y C K I

P A W E Ł T R A C Z Y K

V L A D I M I R G. T U R A E V

W A R S Z A W A 1998

## PREFACE

The mini-semester on Knot Theory took place from July 13 until August 17, 1995, in Stefan Banach International Center in Warsaw, Poland. The semester was divided into three parts. The first part was mainly devoted to expository lectures on various topics related to knot theory, 3-manifold topology and topological quantum field theory. The second part, from July 31 to August 13, was a research conference on knot theory. During the last part there was a series of workshops organized by some of the participants.

The semester had over 90 participants from 17 countries, listed on pages 8–10.

The research conference was co-sponsored by the Department of Mathematics, University of Warsaw, and by the grant from KBN.

We thank all the participants for making the mini-semester successful. We also thank the staff of Banach Center for all their help.

We are dedicating this volume to the memory of François Jaeger (1947–1997).

*The Editors*

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