

On a class of submanifolds in $\mathbb{S}^n \times \mathbb{R}$ and $\mathbb{H}^n \times \mathbb{R}$

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Abstract

Given an isometric immersion $f : M^m \rightarrow \mathbb{Q}_\epsilon^n \times \mathbb{R}$, where \mathbb{Q}_ϵ^n denote either the unit sphere \mathbb{S}^n or the hyperbolic space \mathbb{H}^n , according as $\epsilon = 1$ or $\epsilon = -1$, respectively, let ∂_t be a unit vector field tangent to the second factor. Then, a tangent vector field T on M^m and a normal vector field η along f are defined by

$$\partial_t = f_*T + \eta. \quad (0.1)$$

Let \mathcal{A} denote the class of isometric immersions $f : M^m \rightarrow \mathbb{Q}_\epsilon^n \times \mathbb{R}$ with the property that T is an eigenvector of all shape operators of f . In this talk we will discuss some important subclasses of \mathcal{A} , such as submanifolds with constant sectional curvature [3], rotational submanifolds [1], constant angle hypersurfaces [6] and, with more details, recent works about biconservative submanifolds with parallel mean curvature vector field [2], [4].

References

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