HOW MANY SIMPLICES ARE NEEDED TO TRIANGULATE A GRASSMANNIAN?

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We will explain how R. Stong's [3] determination of non-trivial products in the cohomology of Grassmann manifolds and the Lower Bound Theorem of G. Kalai [2] can be combined with some recent results on the covering type of manifolds by the authors [1] to obtain a lower bound for the number of vertices and of top dimensional simplices in a triangulation of the Grassmann manifold of k-dimensional subspaces of \mathbb{R}^n .

References

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