Infinitely many entire solutions to the curl-curl problem with critical exponent

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We prove the existence of an unbounded sequence of solutions to

$$\nabla \times \nabla \times \mathbf{U} = |\mathbf{U}|^4 \mathbf{U}, \quad \mathbf{U} \colon \mathbb{R}^3 \to \mathbb{R}^3.$$
 (1)

We combine a first group action introduced in [1] to reduce (1) to the vector Yamabe problem with a second group action introduced in [2] to recover compactness in the critical case.

This is joint work with Michał Gaczkowski and Jarosław Mederski.

References

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