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**ABSTRACT**

Alexandru Nica (University of Waterloo)

**A central limit theorem for star-generators of  $S_\infty$ , which relates to traceless CCR-GUE matrices**

**Abstract:** I will present a limit theorem for the sequence of star-generators  $(1, 2), (1, 3), \dots, (1, n), \dots$  of the infinite symmetric group  $S_\infty$ , with respect to an expectation functional provided by a character of  $S_\infty$ , where the character is defined by using some positive weights  $w_1, \dots, w_d$  of sum 1. The limit law turns out to be the law of a  $d \times d$  ‘traceless CCR-GUE’ matrix, an analogue of the traceless GUE where the off-diagonal entries satisfy certain canonical commutation relations dictated by the weights  $w_i$ . The special case when all the  $w_i$ ’s are equal to  $1/d$  yields the law of a bona fide traceless GUE matrix, and we retrieve a result of Koestler-Nica from 2021, which in turn retrieves (for  $d \rightarrow \infty$ ) a result of Biane from 1995.

This is joint work with Jacob Campbell and Claus Koestler, arXiv:2203.01763.