

**$L_p$  Markov exponent of certain UPC sets**Tomasz Beberok <sup>a</sup><sup>a</sup> Department of Mathematics, University of Applied Sciences in Tarnow (Poland)  
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We say that a compact set  $\emptyset \neq E \subset \mathbb{R}^m$  satisfies  $L_p$  Markov type inequality (or: is a  $L_p$  Markov set) if there exist  $\kappa, C > 0$  such that, for each polynomial  $P \in \mathcal{P}(\mathbb{R}^m)$  and each  $\alpha \in \mathbb{N}_0^m$ ,

$$\|D^\alpha P\|_{L_p(E)} \leq (C(\deg P)^\kappa)^{|\alpha|} \|P\|_{L_p(E)}, \quad (1)$$

where  $D^\alpha P = \frac{\partial^{|\alpha|} P}{\partial x_1^{\alpha_1} \dots \partial x_m^{\alpha_m}}$  and  $|\alpha| = \alpha_1 + \dots + \alpha_m$ .

Clearly, by iteration, it is enough to consider in the above definition multi-indices  $\alpha$  with  $|\alpha| = 1$ . The inequality (1) is a generalization of the classical Markov inequality:

$$\|P'\|_{C([-1,1])} \leq (\deg P)^2 \|P\|_{C([-1,1])}.$$

In this talk we shall consider the following problem:

*For a given  $L_p$  Markov set  $E$  determine  $\mu_p(E) := \inf\{\kappa : E \text{ satisfies (1)}\}$ .*