Elliptic systems with critical growth

I will present some old and new results concerning existence of sign-changing solutions to the Yamabe problem on the round sphere and existence of positive solutions to a class of systems of PDE's with critical growth in the whole euclidean space in presence of a competitive regime.