Quasiconvexity meets nonlinear potential theory

A classical problem in the regularity theory for vector-valued minimizers of multiple integrals consists in proving their smoothness outside a negligible set, cf. Evans $(ARMA \ '86)$, Acerbi & Fusco $(ARMA \ '87)$, Duzaar & Mingione $(Ann. \ IHP-AN \ '04)$, Schmidt $(ARMA \ '09)$. In this talk, I will show how to infer sharp partial regularity results for relaxed minimizers of degenerate/singular, nonuniformly elliptic quasiconvex functionals, using tools from nonlinear potential theory. In particular, in the setting of functionals with (p,q)-growth - according to the terminology introduced by Marcellini $(Ann. \ IHP-AN \ '86; \ ARMA \ '89)$ - I will derive optimal local regularity criteria under minimal assumptions on the data. This talk is partly based on joint work with Bianca Stroffolini (University of Naples Federico II).