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P R O B L È M E S

**P 629, R 1.** The answer is no. The results of Comer, Olin and Pierce<sup>(1)</sup> yield examples of compact spaces  $X$  such that  $X^2 \approx X^3$  and  $X$  non  $\approx X^2$ , where  $\approx$  denotes homeomorphism.

XIX.1, p. 181,

Letter of Jan Mycielski, September 1976.

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(<sup>1</sup>) See P. Olin, *Free products of elementary types of BA's*, Mathematica Scandinavica 38 (1976), p. 5-23.

**P 884, R 1.** The problem has been solved. Berrondo has constructed<sup>(2)</sup> an example of a non-algebraically closed field complete with respect to two independent valuations.

XXIX.1, p. 159.

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(<sup>2</sup>) F. Berrondo, *Un corps non algébriquement clos complet pour deux valuations indépendantes*, Comptes Rendus Hebdomadaires des Séances de l'Académie des Sciences, Séries A et B, 282 (1976), p. 675-677.

**P 949, R 1.** The problem has been solved<sup>(3)</sup>.

XXXIII.2, p. 305.

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(<sup>3</sup>) M. Kanter, *Completion measurable linear functionals on a probability space*, this fascicle, p. 277-304; see Theorem 3.1.

**P 956 et P 957, R 1.** The answer to both problems is negative<sup>(4)</sup>.

XXXIV.1, p. 144.

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(<sup>4</sup>) T. Maćkowiak, *Some examples of irreducibly confluent mappings*, this fascicle, p. 193-196.

R. FRANKIEWICZ (KATOWICE)

**P 1021.** Formulé dans la communication *Assertion Q distinguishes topologically  $\omega^*$  and  $m^*$  when  $m$  regular and  $m > \omega$ .*

Ce fascicule, p. 175.

L. D. LOVELAND AND J. E. VALENTINE (LOGAN, UTAH)

**P 1022.** Formulé dans la communication *Generalized midset properties characterize geodesic circles and intervals.*

Ce fascicule, p. 240

ZBIGNIEW GRANDE (ELBLĄG)

**P 1023.** Formulé dans la communication *Sur les suites de fonctions approximativement continues et continues presque partout.*

Ce fascicule, p. 262

Z. JUREK AND K. URBANIK (WROCŁAW)

**P 1024.** Formulé dans la communication *Remarks on stable measures on Banach spaces.*

Ce fascicule, p. 275.

W. WIĘSLAW (WROCŁAW)

**P 1025.** Can a non-algebraically closed metrizable field be complete with respect to two inequivalent locally bounded metrizable field topologies, i.e. can Schmidt's result <sup>(5)</sup> be extended from norms to pseudo-norms? It cannot if norms are replaced by arbitrary minimal topologies (see P 884, R 1 above), but it remains valid for maximally complete valuations. In fact, Vámos has proved <sup>(6)</sup> that for a field  $K$  the following conditions are equivalent:

- (i)  $K$  is algebraically closed and  $\text{card}(K) = \text{card}(K)^{\aleph_0}$ ;
- (ii)  $K$  is maximally complete with respect to two independent valuations;
- (iii) there exist independent valuations  $v_1$  and  $v_2$  such that  $v_1$  is maximal on  $K$  and  $K_{v_2}$  is Henselian.

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<sup>(5)</sup> F. K. Schmidt, *Mehrfach perfekte Körper*, Mathematische Annalen 108 (1933), p. 287-302. Compare also W. Więsław, *On topological fields*, this journal 29 (1974), p. 119-146, especially p. 123.

<sup>(6)</sup> P. Vámos, *Multiply maximally complete fields*, Journal of the London Mathematical Society 12 (1975), p. 103-111.