### MSC2020-Mathematical Sciences Classification System

#### Editors of Mathematical Reviews and zbMATH

	<b>00</b>	General	and	overarching	topics;	collections
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- 01 History and biography
- 03 Mathematical logic and foundations
- **05** Combinatorics
- **06** Order, lattices, ordered algebraic structures
- 08 General algebraic systems
- 11 Number theory
- 12 Field theory and polynomials
- 13 Commutative algebra
- 14 Algebraic geometry
- 15 Linear and multilinear algebra; matrix theory
- 16 Associative rings and algebras
- 17 Nonassociative rings and algebras
- 18 Category theory; homological algebra
- **19** K-theory
- **20** Group theory and generalizations
- 22 Topological groups, Lie groups
- **26** Real functions
- 28 Measure and integration
- **30** Functions of a complex variable
- **31** Potential theory
- 32 Several complex variables and analytic spaces
- **33** Special functions
- **34** Ordinary differential equations
- 35 Partial differential equations
- 37 Dynamical systems and ergodic theory
- **39** Difference and functional equations
- ${f 40}$  Sequences, series, summability
- **41** Approximations and expansions
- 42 Harmonic analysis on Euclidean spaces
- 43 Abstract harmonic analysis
- 44 Integral transforms, operational calculus

- 45 Integral equations
- 46 Functional analysis
- **47** Operator theory
- 49 Calculus of variations and optimal control; optimization
- 51 Geometry
- **52** Convex and discrete geometry
- **53** Differential geometry
- **54** General topology
- 55 Algebraic topology
- 57 Manifolds and cell complexes
- 58 Global analysis, analysis on manifolds
- **60** Probability theory and stochastic processes
- **62** Statistics
- 65 Numerical analysis
- **68** Computer science
- 70 Mechanics of particles and systems
- 74 Mechanics of deformable solids
- **76** Fluid mechanics
- 78 Optics, electromagnetic theory
- 80 Classical thermodynamics, heat transfer
- **81** Quantum theory
- 82 Statistical mechanics, structure of matter
- 83 Relativity and gravitational theory
- 85 Astronomy and astrophysics
- **86** Geophysics
- 90 Operations research, mathematical programming
- 91 Game theory, economics, social and behavioral sciences
- **92** Biology and other natural sciences
- 93 Systems theory; control
- 94 Information and communication, circuits
- 97 Mathematics education

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This document is a printed form of MSC2020, an MSC revision produced jointly by the editorial staffs of Mathematical Reviews (MR) and zbMATH in consultation with the mathematical community. The goals of this revision of the Mathematics Subject Classification (MSC) were set out in the announcement of it and call for comments by the Executive Editor of MR and the Editor-in-Chief of zbMATH in July 2016.

### How to use the Mathematics Subject Classification [MSC]

The main purpose of the classification of items in the mathematical literature using the Mathematics Subject Classification scheme is to help users find the items of present or potential interest to them as readily as possible—in products derived from the Mathematical Reviews Database (MRDB) such as MathSciNet, in Zentralblatt MATH (zbMATH), or anywhere else where this classification scheme is used. An item in the mathematical literature should be classified so as to attract the attention of all those possibly interested in it. The item may be something that falls squarely within one clear area of the MSC, or it may involve several areas. Ideally, the MSC codes attached to an item should represent the subjects to which the item contains a contribution. The classification should serve both those closely concerned with specific subject areas, and those familiar enough with subjects to apply their results and methods elsewhere, inside or outside of mathematics. It will be extremely useful for both users and classifiers to familiarize themselves with the entire classification system and thus to become aware of all the classifications of possible interest to them. Every item in the MRDB or zbMATH receives precisely one primary classification, which is simply the MSC code that describes its principal contribution. When an item contains several principal contributions to different areas, the primary classification should cover the most important among them. A paper or book may be assigned one or several secondary classification numbers to cover any remaining principal contributions, ancillary results, motivation or origin of the matters discussed, intended or potential field of application, or other significant aspects worthy of notice. The principal contribution is meant to be the one including the most important part of the work actually done in the item. For example, a paper whose main overall content is the solution of a problem in graph theory, which arose in computer science and whose solution is (perhaps) at present only of interest to computer scientists, would have a primary classification in 05C (Graph Theory) with one or more secondary classifications in 68 (Computer Science); conversely, a paper whose overall content lies mainly in computer science should receive a primary classification in 68, even if it makes heavy use of graph theory and proves several new graph-theoretic results along the way. There are two types of cross-references given at the end of many of the MSC2020 entries in the MSC. The first type is in braces: "{For A, see X}"; if this appears in section Y, it means that contributions described by A should usually be assigned the classification code X, not Y. The other type of cross-reference merely points out related classifications; it is in brackets: "[See also ... ]", "[See mainly ... ]", etc., and the classification codes listed in the brackets may, but need not, be included in the classification codes of a paper, or they may be used in place of the classification where the cross-reference is given. The classifier must judge which classification is the most appropriate for the paper at hand.

### 00-XX General and overarching 00B30 Festschriften topics; collections

00-01 Introductory exposition (textbooks, tutorial papers, etc.) pertaining to mathematics in general

**00-02** Research exposition (monographs, survey articles) pertaining to mathematics in general

### 00Axx General and miscellaneous specific topics

00A05 Mathematics in general

**00A06** Mathematics for nonmathematicians (engineering, social sciences, etc.)

**00A07** Problem books {For open problems, see 00A27}

00A08 Recreational mathematics

**00A09** Popularization of mathematics

00A15 Bibliographies for mathematics in general [See also 01A70 and the classification number -00 in the other sections

00A17 External book reviews

00A20 Dictionaries and other general reference works [See also the classification number -00 in the other sections

00A22 Formularies

00A27 Lists of open problems

**00A30** Philosophy of mathematics [See also 03A05]

00A35 Methodology of mathematics {For mathematics education, see 97-XX}

**00A64** Mathematics and literature

00A65 Mathematics and music

00A66 Mathematics and visual arts

00A67 Mathematics and architecture

**00A69** General applied mathematics {For physics, see 00A79 and Sections 70 through 86}

00A71 General theory of mathematical modeling

00A72 General theory of simulation

**00A79** Physics (Use more specific entries from Sections 70 through 86 when possible)

00A99 None of the above, but in this section

### 00Bxx Conference proceedings and collections of articles

00B05 Collections of abstracts of lectures

00B10 Collections of articles of general interest

00B15 Collections of articles of miscellaneous specific interest

00B20 Proceedings of conferences of general interest

00B25 Proceedings of conferences of miscellaneous specific interest

00B50 Collections of translated articles of general interest

00B55 Collections of translated articles of miscellaneous specific interest

**00B60** Collections of reprinted articles [See also 01A75]

00B99 None of the above, but in this section

### 01-XX History and biography [See also the classification number -03 in the other sections

01-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to history and biography

01-01 Introductory exposition (textbooks, tutorial papers, etc.) pertaining to history and biography

01-02 Research exposition (monographs, survey articles) pertaining to history and biography

01-06 Proceedings, conferences, collections, etc. pertaining to history and biography

01-11 Research data for problems pertaining to history and biography

### 01Axx History of mathematics and mathematicians

01A05 General histories, source books

01A07 Ethnomathematics, general

01A10 History of mathematics in Paleolithic and Neolithic

01A11 History of mathematics of the indigenous cultures of Africa, Asia, and Oceania

01A12 History of mathematics of the indigenous cultures of the Americas

01A15 History of mathematics of the indigenous cultures of Europe (pre-Greek, etc.)

**01A16** History of mathematics in Ancient Egypt

01A17 History of mathematics in Ancient Babylon

**01A20** History of mathematics in Ancient Greece and Rome

01A25 History of mathematics in China

01A27 History of mathematics in Japan

01A29 History of mathematics in Southeast Asia

01A30 History of mathematics in the Golden Age of Islam

01A32 History of mathematics in India

01A35 History of mathematics in late antiquity and medieval Europe

01A40 History of mathematics in the 15th and 16th centuries, Renaissance

01A45 History of mathematics in the 17th century

**01A50** History of mathematics in the 18th century

01A55 History of mathematics in the 19th century

- 01A60 History of mathematics in the 20th century
- 01A61 History of mathematics in the 21st century
- 01A65 Development of contemporary mathematics
- 01A67 Future perspectives in mathematics
- 01A70 Biographies, obituaries, personalia, bibliographies
- 01A72 Schools of mathematics
- 01A73 History of mathematics at specific universities
- **01A74** History of mathematics at institutions and academies (non-university)
- 01A75 Collected or selected works; reprintings or translations of classics [See also 00B60]
- 01A80 Sociology (and profession) of mathematics
- 01A85 Historiography
- 01A90 Bibliographic studies
- 01A99 None of the above, but in this section

## 03-XX Mathematical logic and foundations

- 03-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to mathematical logic and foundations
- **03-01** Introductory exposition (textbooks, tutorial papers, etc.) pertaining to mathematical logic and foundations
- **03-02** Research exposition (monographs, survey articles) pertaining to mathematical logic and foundations
- ${f 03\text{-}03}$  History of mathematical logic and foundations [Consider also classification numbers pertaining to Section  ${f 01}$ ]
- **03-04** Software, source code, etc. for problems pertaining to mathematical logic and foundations
- **03-06** Proceedings, conferences, collections, etc. pertaining to mathematical logic and foundations
- **03-08** Computational methods for problems pertaining to mathematical logic and foundations
- ${f 03\text{-}11}$  Research data for problems pertaining to mathematical logic and foundations

## 03Axx Philosophical aspects of logic and foundations

- 03A05 Philosophical and critical aspects of logic and foundations {For philosophy of mathematics, see also 00A30}
- 03A10 Logic in the philosophy of science
- 03A99 None of the above, but in this section

### 03Bxx General logic

- 03B05 Classical propositional logic
- 03B10 Classical first-order logic
- 03B16 Higher-order logic
- ${f 03B20}$  Subsystems of classical logic (including intuitionistic logic)
- 03B22 Abstract deductive systems
- ${f 03B25}$  Decidability of theories and sets of sentences [See also  $11U05,\ 12L05,\ 20F10$ ]
- ${\bf 03B30}$  Foundations of classical theories (including reverse mathematics) [See also  ${\bf 03F35}]$
- ${f 03B35}$  Mechanization of proofs and logical operations [See also  ${f 68V15}$ ]
- **03B38** Type theory
- ${f 03B40}$  Combinatory logic and lambda calculus [See also  ${f 68N18}$ ]
- 03B42 Logics of knowledge and belief (including belief change)
- 03B44 Temporal logic
- **03B45** Modal logic (including the logic of norms) {For knowledge and belief, see 03B42; for temporal logic, see 03B44; for provability logic, see also 03F45}
- 03B48 Probability and inductive logic [See also 60A05]
- 03B50 Many-valued logic
- $egin{aligned} \textbf{03B52} & \text{Fuzzy logic; logic of vagueness} & [\text{See also } 68\text{T}27, 68\text{T}37, \\ 94\text{D}05] & \end{aligned}$
- 03B53 Paraconsistent logics
- 03B55 Intermediate logics
- 03B60 Other nonclassical logic
- ${f 03B62}$  Combined logics
- 03B65 Logic of natural languages [See also 68T50, 91F20]
- 03B70 Logic in computer science [See also 68-XX]
- 03B80 Other applications of logic
- 03B99 None of the above, but in this section

### 03Cxx Model theory

- 03C05 Equational classes, universal algebra in model theory [See also 08Axx, 08Bxx, 18C05]
- ${f 03C07}$  Basic properties of first-order languages and structures
- ${f 03C10}$  Quantifier elimination, model completeness and related topics
- 03C13 Model theory of finite structures [See also 68Q15, 68Q19]

- ${f 03C15}$  Model theory of denumerable and separable structures
- 03C20 Ultraproducts and related constructions
- 03C25 Model-theoretic forcing
- 03C30 Other model constructions
- 03C35 Categoricity and completeness of theories
- 03C40 Interpolation, preservation, definability
- ${f 03C45}$  Classification theory, stability and related concepts in model theory [See also  ${f 03C48}$ ]
- 03C48 Abstract elementary classes and related topics [See also 03C45]
- 03C50 Models with special properties (saturated, rigid, etc.)
- ${f 03C52}$  Properties of classes of models
- 03C55 Set-theoretic model theory
- 03C57 Computable structure theory, computable model theory [See also 03D45]
- 03C60 Model-theoretic algebra [See also 08C10, 12Lxx, 13L05]
- 03C62 Models of arithmetic and set theory [See also 03Hxx]
- 03C64 Model theory of ordered structures; o-minimality
- 03C65 Models of other mathematical theories
- ${f 03C66}$  Continuous model theory, model theory of metric structures
- 03C68 Other classical first-order model theory
- 03C70 Logic on admissible sets
- 03C75 Other infinitary logic
- 03C80 Logic with extra quantifiers and operators [See also 03B42, 03B44, 03B45, 03B48]
- 03C85 Second- and higher-order model theory
- 03C90 Nonclassical models (Boolean-valued, sheaf, etc.)
- 03C95 Abstract model theory
- **03C98** Applications of model theory [See also 03C60]
- 03C99 None of the above, but in this section

## 03Dxx Computability and recursion theory

- 03D03 Thue and Post systems, etc.
- **03D05** Automata and formal grammars in connection with logical questions [See also 68Q45, 68Q70, 68R15]
- **03D10** Turing machines and related notions [See also 68Q04]
- **03D15** Complexity of computation (including implicit computational complexity) [See also 68Q15, 68Q17]
- ${f 03D20}$  Recursive functions and relations, subrecursive hierarchies
- ${f 03D25}$  Recursively (computably) enumerable sets and degrees
- 03D28 Other Turing degree structures

- 03D30 Other degrees and reducibilities in computability and recursion theory
- 03D32 Algorithmic randomness and dimension [See also 68Q30]
- 03D35 Undecidability and degrees of sets of sentences
- 03D40 Word problems, etc. in computability and recursion theory [See also  $06B25,\ 08A50,\ 20F10,\ 68R15]$
- **03D45** Theory of numerations, effectively presented structures [See also 03C57] {For intuitionistic and similar approaches, see 03F55}
- 03D50 Recursive equivalence types of sets and structures, isols
- 03D55 Hierarchies of computability and definability
- 03D60 Computability and recursion theory on ordinals, admissible sets, etc.
- 03D65 Higher-type and set recursion theory
- 03D70 Inductive definability
- 03D75 Abstract and axiomatic computability and recursion theory
- 03D78 Computation over the reals, computable analysis {For constructive aspects, see 03F60}
- 03D80 Applications of computability and recursion theory
- 03D99 None of the above, but in this section

### 03Exx Set theory

- 03E02 Partition relations
- 03E04 Ordered sets and their cofinalities; pcf theory
- 03E05 Other combinatorial set theory
- 03E10 Ordinal and cardinal numbers
- **03E15** Descriptive set theory [See also 28A05, 54H05]
- 03E17 Cardinal characteristics of the continuum
- **03E20** Other classical set theory (including functions, relations, and set algebra)
- 03E25 Axiom of choice and related propositions
- 03E30 Axiomatics of classical set theory and its fragments
- 03E35 Consistency and independence results
- ${f 03E40}$  Other aspects of forcing and Boolean-valued models
- 03E45 Inner models, including constructibility, ordinal definability, and core models
- **03E47** Other notions of set-theoretic definability
- 03E50 Continuum hypothesis and Martin's axiom [See also 03E57]
- 03E55 Large cardinals
- 03E57 Generic absoluteness and forcing axioms [See also 03E50]
- 03E60 Determinacy principles
- ${f 03E65}$  Other set-theoretic hypotheses and axioms
- 03E70 Nonclassical and second-order set theories
- 03E72 Theory of fuzzy sets, etc.
- **03E75** Applications of set theory
- 03E99 None of the above, but in this section

## mathematics

- 03F03 Proof theory, general (including proof-theoretic semantics)
- 03F05 Cut-elimination and normal-form theorems
- **03F07** Structure of proofs
- 03F10 Functionals in proof theory
- **03F15** Recursive ordinals and ordinal notations
- 03F20 Complexity of proofs
- **03F25** Relative consistency and interpretations
- **03F30** First-order arithmetic and fragments
- 03F35 Second- and higher-order arithmetic and fragments [See also 03B30]
- 03F40 Gödel numberings and issues of incompleteness
- 03F45 Provability logics and related algebras (e.g., diagonalizable algebras) [See also 03B45, 03G25, 06E25]
- **03F50** Metamathematics of constructive systems
- 03F52 Proof-theoretic aspects of linear logic and other substructural logics [See also 03B47]
- 03F55 Intuitionistic mathematics
- **03F60** Constructive and recursive analysis [See also 03B30, 03D45, 03D78, 26E40, 46S30, 47S30]
- **03F65** Other constructive mathematics [See also 03D45]
- 03F99 None of the above, but in this section

### 03Gxx Algebraic logic

- 03G05 Logical aspects of Boolean algebras [See also 06Exx]
- 03G10 Logical aspects of lattices and related structures [See also 06Bxx
- 03G12 Quantum logic [See also 06C15, 81P10]
- 03G15 Cylindric and polyadic algebras; relation algebras
- 03G20 Logical aspects of Łukasiewicz and Post algebras [See also 06D25, 06D30]
- 03G25 Other algebras related to logic [See also 03F45, 06D20, 06E25, 06F35
- 03G27 Abstract algebraic logic
- **03G30** Categorical logic, topoi [See also 18B25, 18C05, 18C10
- 03G99 None of the above, but in this section

### 03Hxx Nonstandard models [See also 03C62

- 03H05 Nonstandard models in mathematics [See also 26E35, 28E05, 30G06, 46S20, 47S20, 54J05]
- 03H10 Other applications of nonstandard models (economics, physics, etc.)
- 03H15 Nonstandard models of arithmetic [See also 11U10, 12L15, 13L05
- 03H99 None of the above, but in this section

### 03Fxx Proof theory and constructive 05-XX Combinatorics {For finite fields, see 11Txx

- 05-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to combinatorics
- **05-01** Introductory exposition (textbooks, tutorial papers, etc.) pertaining to combinatorics
- **05-02** Research exposition (monographs, survey articles) pertaining to combinatorics
- **05-03** History of combinatorics [Consider also classification numbers pertaining to Section 01]
- 05-04 Software, source code, etc. for problems pertaining to combinatorics
- 05-06 Proceedings, conferences, collections, etc. pertaining to combinatorics
- 05-08 Computational methods for problems pertaining to combinatorics
- 05-11 Research data for problems pertaining to combinatorics

### 05Axx Enumerative combinatorics {For enumeration in graph theory, see 05C30

- 05A05 Permutations, words, matrices
- 05A10 Factorials, binomial coefficients, combinatorial functions [See also 11B65, 33Cxx]
- 05A15 Exact enumeration problems, generating functions [See also 33Cxx, 33Dxx]
- **05A16** Asymptotic enumeration
- 05A17 Combinatorial aspects of partitions of integers [See also 11P81, 11P82, 11P83]
- 05A18 Partitions of sets
- **05A19** Combinatorial identities, bijective combinatorics
- 05A20 Combinatorial inequalities
- 05A30 q-calculus and related topics [See also 33Dxx]
- 05A40 Umbral calculus
- 05A99 None of the above, but in this section

## 05Bxx Designs and configurations {For applications of design theory, see 94C30}

 ${f 05B05}$  Combinatorial aspects of block designs [See also  ${f 51E05},\,{f 62K10}$ ]

05B07 Triple systems

**05B10** Combinatorial aspects of difference sets (number-theoretic, group-theoretic, etc.) [See also 11B13]

05B15 Orthogonal arrays, Latin squares, Room squares

**05B20** Combinatorial aspects of matrices (incidence, Hadamard, etc.)

 ${f 05B25}$  Combinatorial aspects of finite geometries [See also  ${f 51D20,\,51Exx}$ ]

**05B30** Other designs, configurations [See also 51E30]

 ${f 05B35}$  Combinatorial aspects of matroids and geometric lattices [See also  ${f 52B40},\, {f 90C27}]$ 

05B40 Combinatorial aspects of packing and covering [See also 11H31, 52C15, 52C17]

 $\bf 05B45$  Combinatorial aspects of tessellation and tiling problems [See also 52C20, 52C22]

05B50 Polyominoes

05B99 None of the above, but in this section

## 05Cxx Graph theory {For applications of graphs, see 68R10, 81Q30, 81T15, 82B20, 82C20, 90C35, 92E10, 94C15}

05C05 Trees

05C07 Vertex degrees [See also 05E30]

**05C09** Graphical indices (Wiener index, Zagreb index, Randić index, etc.)

 $\bf 05C10$  Planar graphs; geometric and topological aspects of graph theory [See also  $\bf 57K10,\, 57M15]$ 

05C12 Distance in graphs

05C15 Coloring of graphs and hypergraphs

05C17 Perfect graphs

05C20 Directed graphs (digraphs), tournaments

 ${\bf 05C21} \ \ {\rm Flows \ in \ graphs}$ 

05C22 Signed and weighted graphs

05C25 Graphs and abstract algebra (groups, rings, fields, etc.) [See also 20F65]

05C30 Enumeration in graph theory

05C31 Graph polynomials

**05C35** Extremal problems in graph theory [See also 90C35]

05C38 Paths and cycles [See also 90B10]

05C40 Connectivity

**05C42** Density (toughness, etc.)

05C45 Eulerian and Hamiltonian graphs

05C48 Expander graphs

05C50 Graphs and linear algebra (matrices, eigenvalues, etc.)

05C51 Graph designs and isomorphic decomposition [See also 05B30]

05C55 Generalized Ramsey theory [See also 05D10]

05C57 Games on graphs (graph-theoretic aspects) [See also  $91A43, \, 91A46$ ]

**05C60** Isomorphism problems in graph theory (reconstruction conjecture, etc.) and homomorphisms (subgraph embedding, etc.)

 $\begin{array}{ll} \textbf{05C62} \ \, \text{Graph representations (geometric and intersection} \\ \text{representations, etc.)} \quad \, \{\text{For graph drawing, see also} \\ & \quad \, &$ 

05C63 Infinite graphs

05C65 Hypergraphs

**05C69** Vertex subsets with special properties (dominating sets, independent sets, cliques, etc.)

**05C70** Edge subsets with special properties (factorization, matching, partitioning, covering and packing, etc.)

05C72 Fractional graph theory, fuzzy graph theory

05C75 Structural characterization of families of graphs

05C76 Graph operations (line graphs, products, etc.)

05C78 Graph labelling (graceful graphs, bandwidth, etc.)

05C80 Random graphs (graph-theoretic aspects) [See also 60B20]

05C81 Random walks on graphs

 $\bf 05C82$  Small world graphs, complex networks (graph-theoretic aspects) [See also  $90Bxx,\,91D30]$ 

05C83 Graph minors

05C85 Graph algorithms (graph-theoretic aspects) [See also  $68R10, \, 68W05$ ]

**05C90** Applications of graph theory [See also 68R10, 81Q30, 81T15, 82B20, 82C20, 90C35, 92E10, 94C15]

**05C92** Chemical graph theory [See also 92E10]

05C99 None of the above, but in this section

#### 05Dxx Extremal combinatorics

05D05 Extremal set theory

**05D10** Ramsey theory [See also 05C55]

 ${f 05D15}$  Transversal (matching) theory

05D40 Probabilistic methods in extremal combinatorics, including polynomial methods (combinatorial Nullstellensatz, etc.)

05D99 None of the above, but in this section

### 05Exx Algebraic combinatorics

- 05E05 Symmetric functions and generalizations
- ${f 05E10}$  Combinatorial aspects of representation theory [See also  ${f 20C30}$ ]
- ${f 05E14}$  Combinatorial aspects of algebraic geometry [See also  ${f 14Nxx}$ ]
- ${f 05E16}$  Combinatorial aspects of groups and algebras [See also  ${f 22E45},\,{\bf 33C80}]$
- 05E18 Group actions on combinatorial structures
- 05E30 Association schemes, strongly regular graphs
- 05E40 Combinatorial aspects of commutative algebra
- 05E45 Combinatorial aspects of simplicial complexes
- 05E99 None of the above, but in this section

## 06-XX Order, lattices, ordered algebraic structures [See also 18B35]

- **06-00** General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to ordered structures
- 06-01 Introductory exposition (textbooks, tutorial papers, etc.) pertaining to ordered structures
- **06-02** Research exposition (monographs, survey articles) pertaining to ordered structures
- 06-03 History of ordered structures [Consider also classification numbers pertaining to Section 01]
- ${f 06\text{-}04}$  Software, source code, etc. for problems pertaining to ordered structures
- **06-06** Proceedings, conferences, collections, etc. pertaining to ordered structures
- ${f 06\text{-}08}$  Computational methods for problems pertaining to ordered structures
- ${f 06\text{-}11}$  Research data for problems pertaining to ordered structures

### 06Axx Ordered sets

- 06A05 Total orders
- 06A06 Partial orders, general
- 06A07 Combinatorics of partially ordered sets
- ${f 06A11}$  Algebraic aspects of posets
- $\bf 06A12$  Semilattices [See also 20M10] {For topological semilattices, see 22A26}
- 06A15 Galois correspondences, closure operators (in relation to ordered sets)
- 06A75 Generalizations of ordered sets
- 06A99 None of the above, but in this section

### 06Bxx Lattices [See also 03G10]

- 06B05 Structure theory of lattices
- 06B10 Lattice ideals, congruence relations
- 06B15 Representation theory of lattices
- 06B20 Varieties of lattices
- 06B23 Complete lattices, completions
- 06B25 Free lattices, projective lattices, word problems [See also  $03D40,\ 08A50,\ 20F10$ ]
- **06B30** Topological lattices [See also 06F30, 22A26, 54F05, 54H12]
- 06B35 Continuous lattices and posets, applications [See also  $06B30,\ 06D10,\ 06F30,\ 18B35,\ 22A26,\ 68Q55]$
- 06B75 Generalizations of lattices
- 06B99 None of the above, but in this section

### 06Cxx Modular lattices, complemented lattices

- 06C05 Modular lattices, Desarguesian lattices
- 06C10 Semimodular lattices, geometric lattices
- 06C15 Complemented lattices, orthocomplemented lattices and posets [See also  $03G12,\,81P10$ ]
- 06C20 Complemented modular lattices, continuous geometries
- 06C99 None of the above, but in this section

### 06Dxx Distributive lattices

- ${f 06D05}$  Structure and representation theory of distributive lattices
- 06D10 Complete distributivity
- 06D15 Pseudocomplemented lattices
- ${\bf 06D20}$  Heyting algebras (lattice-theoretic aspects) [See also  ${\bf 03G25}]$
- 06D22 Frames, locales {For topological questions, see 54- XX}
- ${\bf 06D25}$  Post algebras (lattice-theoretic aspects) [See also  ${\bf 03G20}]$
- $06\mathrm{D}30$  De Morgan algebras, Lukasiewicz algebras (lattice-theoretic aspects) [See also  $03\mathrm{G}20]$
- 06D35 MV-algebras
- ${f 06D50}$  Lattices and duality
- 06D72 Fuzzy lattices (soft algebras) and related topics
- 06D75 Other generalizations of distributive lattices
- 06D99 None of the above, but in this section

### 06Exx Boolean algebras (Boolean rings) [See also 03G05]

- 06E05 Structure theory of Boolean algebras
- 06E10 Chain conditions, complete algebras
- ${f 06E15}$  Stone spaces (Boolean spaces) and related structures
- 06E20 Ring-theoretic properties of Boolean algebras [See also  $16E50,\,16G30$ ]
- **06E25** Boolean algebras with additional operations (diagonalizable algebras, etc.) [See also 03G25, 03F45]
- **06E30** Boolean functions [See also 94D10]
- 06E75 Generalizations of Boolean algebras
- 06E99 None of the above, but in this section

### 06Fxx Ordered structures

- **06F05** Ordered semigroups and monoids [See also 20Mxx]
- 06F07 Quantales
- 06F10 Noether lattices
- **06F15** Ordered groups [See also 20F60]
- $\bf 06F20$  Ordered abelian groups, Riesz groups, ordered linear spaces [See also  $\bf 46A40$ ]
- 06F25 Ordered rings, algebras, modules {For ordered fields, see 12J15} [See also 13J25, 16W80]
- **06F30** Ordered topological structures (aspects of ordered structures) [See also 06B30, 22A26, 54F05, 54H12]
- 06F35 BCK-algebras, BCI-algebras (aspects of ordered structures) [See also 03G25]
- 06F99 None of the above, but in this section

### 08-XX General algebraic systems

- ${f 08\text{-}00}$  General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to general algebraic systems
- **08-01** Introductory exposition (textbooks, tutorial papers, etc.) pertaining to general algebraic systems
- **08-02** Research exposition (monographs, survey articles) pertaining to general algebraic systems
- **08-03** History of general algebraic systems [Consider also classification numbers pertaining to Section 01]
- ${f 08\text{-}04}$  Software, source code, etc. for problems pertaining to general algebraic systems
- $\begin{array}{c} \textbf{08-06} \ \ \text{Proceedings, conferences, collections, etc.} \\ \ \ \text{pertaining} \\ \ \ \text{to general algebraic systems} \end{array}$
- **08-08** Computational methods for problems pertaining to general algebraic systems
- ${f 08-11}$  Research data for problems pertaining to general algebraic systems

## 08Axx Algebraic structures [See also 03C05]

- 08A02 Relational systems, laws of composition
- 08A05 Structure theory of algebraic structures
- 08A30 Subalgebras, congruence relations
- 08A35 Automorphisms and endomorphisms of algebraic structures
- 08A40 Operations and polynomials in algebraic structures, primal algebras
- **08A45** Equational compactness
- 08A50 Word problems (aspects of algebraic structures) [See also 03D40, 06B25, 20F10, 68R15]
- 08A55 Partial algebras
- 08A60 Unary algebras
- 08A62 Finitary algebras
- 08A65 Infinitary algebras
- ${f 08A68}$  Heterogeneous algebras
- 08A70 Applications of universal algebra in computer science
- 08A72 Fuzzy algebraic structures
- 08A99 None of the above, but in this section

### 08Bxx Varieties [See also 03C05]

- 08B05 Equational logic, Mal'tsev conditions
- 08B10 Congruence modularity, congruence distributivity
- 08B15 Lattices of varieties
- 08B20 Free algebras
- ${\bf 08B25}\,$  Products, amalgamated products, and other kinds of limits and colimits [See also  ${\bf 18A30}]$
- 08B26 Subdirect products and subdirect irreducibility
- 08B30 Injectives, projectives
- 08B99 None of the above, but in this section

### 08Cxx Other classes of algebras

- **08C05** Categories of algebras [See also 18C05]
- ${\bf 08C10}\,$  Axiomatic model classes [See also  ${\bf 03Cxx},$  in particular  ${\bf 03C60}]$
- 08C15 Quasivarieties
- 08C20 Natural dualities for classes of algebras [See also  $06E15,\ 18A40,\ 22A30$ ]
- 08C99 None of the above, but in this section

### 11-XX Number theory

- 11-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to number theory
- 11-01 Introductory exposition (textbooks, tutorial papers, etc.) pertaining to number theory
- 11-02 Research exposition (monographs, survey articles) pertaining to number theory
- 11-03 History of number theory [Consider also classification numbers pertaining to Section 01]
- ${f 11\text{-}04}$  Software, source code, etc. for problems pertaining to number theory
- 11-06 Proceedings, conferences, collections, etc. pertaining to number theory
- ${\bf 11\text{-}11}\,$  Research data for problems pertaining to number theory

## 11Axx Elementary number theory {For analogues in number fields, see 11R04}

- 11A05 Multiplicative structure; Euclidean algorithm; greatest common divisors
- 11A07 Congruences; primitive roots; residue systems
- 11A15 Power residues, reciprocity
- ${f 11A25}$  Arithmetic functions; related numbers; inversion formulas
- 11A41 Primes
- 11A51 Factorization; primality
- 11A55 Continued fractions {For approximation results, see 11J70} [See also 11K50, 30B70, 40A15]
- 11A63 Radix representation; digital problems {For metric results, see 11K16}
- 11A67 Other number representations
- 11A99 None of the above, but in this section

### 11Bxx Sequences and sets

- 11B05 Density, gaps, topology
- 11B13 Additive bases, including sumsets [See also 05B10]
- 11B25 Arithmetic progressions [See also 11N13]
- 11B30 Arithmetic combinatorics; higher degree uniformity
- 11B34 Representation functions
- 11B37 Recurrences {For applications to special functions, see 33-XX}
- 11B39 Fibonacci and Lucas numbers and polynomials and generalizations
- **11B50** Sequences (mod m)
- 11B57 Farey sequences; the sequences  $1^k, 2^k, \dots$
- **11B65** Binomial coefficients; factorials; q-identities [See also 05A10, 05A30]

- 11B68 Bernoulli and Euler numbers and polynomials
- 11B73 Bell and Stirling numbers
- 11B75 Other combinatorial number theory
- 11B83 Special sequences and polynomials
- 11B85 Automata sequences
- 11B99 None of the above, but in this section

### 11Cxx Polynomials and matrices

- 11C08 Polynomials in number theory [See also 13F20]
- 11C20 Matrices, determinants in number theory [See also 15B36]
- 11C99 None of the above, but in this section

## 11Dxx Diophantine equations [See also 11Gxx, 14Gxx]

- 11D04 Linear Diophantine equations
- 11D07 The Frobenius problem
- 11D09 Quadratic and bilinear Diophantine equations
- 11D25 Cubic and quartic Diophantine equations
- 11D41 Higher degree equations; Fermat's equation
- 11D45 Counting solutions of Diophantine equations
- 11D57 Multiplicative and norm form equations
- 11D59 Thue-Mahler equations
- 11D61 Exponential Diophantine equations
- 11D68 Rational numbers as sums of fractions
- 11D72 Diophantine equations in many variables [See also 11P55]
- 11D75 Diophantine inequalities [See also 11J25]
- 11D79 Congruences in many variables
- 11D85 Representation problems [See also 11P55]
- 11D88 p-adic and power series fields
- 11D99 None of the above, but in this section

## 11Exx Forms and linear algebraic groups [See also 19Gxx] {For quadratic forms in linear algebra, see 15A63}

- 11E04 Quadratic forms over general fields
- 11E08 Quadratic forms over local rings and fields
- 11E10 Forms over real fields
- 11E12 Quadratic forms over global rings and fields
- 11E16 General binary quadratic forms
- 11E20 General ternary and quaternary quadratic forms; forms of more than two variables
- 11E25 Sums of squares and representations by other particular quadratic forms
- 11E39 Bilinear and Hermitian forms
- 11E41 Class numbers of quadratic and Hermitian forms

- 11E45 Analytic theory (Epstein zeta functions; relations 11F66 Langlands L-functions; one variable Dirichlet series with automorphic forms and functions)
- 11E57 Classical groups [See also 14Lxx, 20Gxx]
- 11E70 K-theory of quadratic and Hermitian forms
- 11E72 Galois cohomology of linear algebraic groups [See also 20G10
- 11E76 Forms of degree higher than two
- 11E81 Algebraic theory of quadratic forms; Witt groups and rings [See also 19G12, 19G24]
- 11E88 Quadratic spaces; Clifford algebras [See also 15A63, 15A66
- 11E95 p-adic theory
- 11E99 None of the above, but in this section

### 11Fxx Discontinuous groups and automorphic forms [See also 11R39, 11S37, 14Gxx, 14Kxx, 22E50, 22E55, 30F35, 32Nxx] {For relations with quadratic forms, see 11E45

- 11F03 Modular and automorphic functions
- 11F06 Structure of modular groups and generalizations; arithmetic groups [See also 20H05, 20H10, 22E40]
- 11F11 Holomorphic modular forms of integral weight
- 11F12 Automorphic forms, one variable
- 11F20 Dedekind eta function, Dedekind sums
- 11F22 Relationship to Lie algebras and finite simple groups
- 11F23 Relations with algebraic geometry and topology
- 11F25 Hecke-Petersson operators, differential operators (one variable)
- 11F27 Theta series; Weil representation; theta correspondences
- 11F30 Fourier coefficients of automorphic forms
- 11F32 Modular correspondences, etc.
- **11F33** Congruences for modular and *p*-adic modular forms [See also 14G20, 22E50]
- 11F37 Forms of half-integer weight; nonholomorphic modular forms
- 11F41 Automorphic forms on GL(2); Hilbert and Hilbert-Siegel modular groups and their modular and automorphic forms; Hilbert modular surfaces [See also 14J20]
- 11F46 Siegel modular groups; Siegel and Hilbert-Siegel modular and automorphic forms
- 11F50 Jacobi forms
- 11F52 Modular forms associated to Drinfel'd modules
- 11F55 Other groups and their modular and automorphic forms (several variables)
- 11F60 Hecke-Petersson operators, differential operators (several variables)

- and functional equations
- 11F67 Special values of automorphic L-series, periods of automorphic forms, cohomology, modular symbols
- 11F68 Dirichlet series in several complex variables associated to automorphic forms; Weyl group multiple Dirichlet se-
- 11F70 Representation-theoretic methods; automorphic representations over local and global fields
- 11F72 Spectral theory; trace formulas (e.g., that of Selberg)
- 11F75 Cohomology of arithmetic groups
- 11F77 Automorphic forms and their relations with perfectoid spaces [See also 14G45]
- 11F80 Galois representations
- 11F85 p-adic theory, local fields [See also 14G20, 22E50]
- 11F99 None of the above, but in this section

### 11Gxx Arithmetic algebraic geometry (Diophantine geometry) [See also 11Dxx, 14Gxx, 14Kxx

- 11G05 Elliptic curves over global fields [See also 14H52]
- 11G07 Elliptic curves over local fields [See also 14G20, 14H52
- 11G09 Drinfel'd modules; higher-dimensional motives, etc. [See also 14L05]
- 11G10 Abelian varieties of dimension > 1 [See also 14Kxx]
- 11G15 Complex multiplication and moduli of abelian varieties [See also 14K22]
- 11G16 Elliptic and modular units [See also 11R27]
- 11G18 Arithmetic aspects of modular and Shimura varieties [See also 14G35]
- 11G20 Curves over finite and local fields [See also 14H25]
- 11G25 Varieties over finite and local fields [See also 14G15, 14G20
- 11G30 Curves of arbitrary genus or genus  $\neq 1$  over global fields [See also 14H25]
- 11G32 Arithmetic aspects of dessins d'enfants, Belyĭ theory
- 11G35 Varieties over global fields [See also 14G25]
- 11G40 L-functions of varieties over global fields; Birch-Swinnerton-Dyer conjecture [See also 14G10]
- 11G42 Arithmetic mirror symmetry [See also 14J33]
- 11G45 Geometric class field theory [See also 11R37, 14C35, 19F05
- **11G50** Heights [See also 14G40, 37P30]
- 11G55 Polylogarithms and relations with K-theory
- 11G99 None of the above, but in this section

## cations in coding theory, see 94B75

- 11H06 Lattices and convex bodies (number-theoretic aspects) [See also 11P21, 52C05, 52C07]
- 11H16 Nonconvex bodies
- 11H31 Lattice packing and covering (number-theoretic aspects) [See also 05B40, 52C15, 52C17]
- 11H46 Products of linear forms
- 11H50 Minima of forms
- 11H55 Quadratic forms (reduction theory, extreme forms,
- 11H56 Automorphism groups of lattices
- 11H60 Mean value and transfer theorems
- 11H71 Relations with coding theory
- 11H99 None of the above, but in this section

### 11Jxx Diophantine approximation, transcendental number theory [See also 11K60]

- 11J04 Homogeneous approximation to one number
- 11J06 Markov and Lagrange spectra and generalizations
- 11J13 Simultaneous homogeneous approximation, linear
- 11J17 Approximation by numbers from a fixed field
- 11J20 Inhomogeneous linear forms
- 11J25 Diophantine inequalities [See also 11D75]
- 11J54 Small fractional parts of polynomials and generalizations
- 11J61 Approximation in non-Archimedean valuations
- 11J68 Approximation to algebraic numbers
- 11J70 Continued fractions and generalizations [See also 11A55, 11K50
- 11J71 Distribution modulo one [See also 11K06]
- 11J72 Irrationality; linear independence over a field
- 11J81 Transcendence (general theory)
- 11J82 Measures of irrationality and of transcendence
- 11J83 Metric theory
- 11J85 Algebraic independence; Gel'fond's method
- 11J86 Linear forms in logarithms; Baker's method
- 11J87 Schmidt Subspace Theorem and applications
- 11J89 Transcendence theory of elliptic and abelian functions
- 11J91 Transcendence theory of other special functions
- 11J93 Transcendence theory of Drinfel'd and t-modules
- 11J95 Results involving abelian varieties
- 11J97 Number-theoretic analogues of methods in Nevanlinna theory (work of Vojta et al.)
- 11J99 None of the above, but in this section

### 11Hxx Geometry of numbers {For appli- 11Kxx Probabilistic theory: distribution modulo 1; metric theory of algorithms

- 11K06 General theory of distribution modulo 1 [See also 11J71
- 11K16 Normal numbers, radix expansions, Pisot numbers, Salem numbers, good lattice points, etc. 11A63
- 11K31 Special sequences
- 11K36 Well-distributed sequences and other variations
- 11K38 Irregularities of distribution, discrepancy [See also 11Nxx
- 11K41 Continuous, p-adic and abstract analogues
- 11K45 Pseudo-random numbers; Monte Carlo methods [See also 65C05, 65C10]
- 11K50 Metric theory of continued fractions [See also 11A55, 11J70]
- 11K55 Metric theory of other algorithms and expansions; measure and Hausdorff dimension [See also 11N99, 28Dxx
- 11K60 Diophantine approximation in probabilistic number theory [See also 11Jxx]
- 11K65 Arithmetic functions in probabilistic number theory [See also 11Nxx]
- 11K70 Harmonic analysis and almost periodicity in probabilistic number theory
- 11K99 None of the above, but in this section

### 11Lxx Exponential sums and character sums {For finite fields, see 11Txx}

- 11L03 Trigonometric and exponential sums, general
- 11L05 Gauss and Kloosterman sums; generalizations
- 11L07 Estimates on exponential sums
- 11L10 Jacobsthal and Brewer sums; other complete character sums
- 11L15 Weyl sums
- 11L20 Sums over primes
- 11L26 Sums over arbitrary intervals
- 11L40 Estimates on character sums
- 11L99 None of the above, but in this section

### 11Mxx Zeta and L-functions: analytic the- 11Pxx Additive number theory; partitions orv

- **11M06**  $\zeta(s)$  and  $L(s,\chi)$
- **11M20** Real zeros of  $L(s,\chi)$ ; results on  $L(1,\chi)$
- **11M26** Nonreal zeros of  $\zeta(s)$  and  $L(s,\chi)$ ; Riemann and other hypotheses
- 11M32 Multiple Dirichlet series and zeta functions and multizeta values
- 11M35 Hurwitz and Lerch zeta functions
- 11M36 Selberg zeta functions and regularized determinants; applications to spectral theory, Dirichlet series, Eisenstein series, etc. (explicit formulas)
- 11M38 Zeta and L-functions in characteristic p
- 11M41 Other Dirichlet series and zeta functions {For local and global ground fields, see 11R42, 11R52, 11S40, 11S45; for algebro-geometric methods, see 14G10} [See also 11E45, 11F66, 11F70, 11F72]
- 11M45 Tauberian theorems [See also 40E05]
- 11M50 Relations with random matrices
- 11M55 Relations with noncommutative geometry
- 11M99 None of the above, but in this section

### 11Nxx Multiplicative number theory

- 11N05 Distribution of primes
- 11N13 Primes in congruence classes
- 11N25 Distribution of integers with specified multiplicative constraints
- 11N30 Turán theory [See also 30Bxx]
- 11N32 Primes represented by polynomials; other multiplicative structures of polynomial values
- 11N35 Sieves
- 11N36 Applications of sieve methods
- 11N37 Asymptotic results on arithmetic functions
- 11N45 Asymptotic results on counting functions for algebraic and topological structures
- 11N56 Rate of growth of arithmetic functions
- 11N60 Distribution functions associated with additive and positive multiplicative functions
- 11N64 Other results on the distribution of values or the characterization of arithmetic functions
- 11N69 Distribution of integers in special residue classes
- 11N75 Applications of automorphic functions and forms to multiplicative problems [See also 11Fxx]
- 11N80 Generalized primes and integers
- 11N99 None of the above, but in this section

- 11P05 Waring's problem and variants
- 11P21 Lattice points in specified regions
- 11P32 Goldbach-type theorems; other additive questions involving primes
- 11P55 Applications of the Hardy-Littlewood method [See also 11D85]
- 11P70 Inverse problems of additive number theory, including sumsets
- 11P81 Elementary theory of partitions [See also 05A17]
- 11P82 Analytic theory of partitions
- 11P83 Partitions; congruences and congruential restrictions
- 11P84 Partition identities; identities of Rogers-Ramanujan
- 11P99 None of the above, but in this section

### 11Rxx Algebraic number theory: global fields {For complex multiplication, see 11G15}

- 11R04 Algebraic numbers; rings of algebraic integers
- 11R06 PV-numbers and generalizations; other special algebraic numbers; Mahler measure
- 11R09 Polynomials (irreducibility, etc.)
- 11R11 Quadratic extensions
- 11R16 Cubic and quartic extensions
- 11R18 Cyclotomic extensions
- 11R20 Other abelian and metabelian extensions
- 11R21 Other number fields
- 11R23 Iwasawa theory
- 11R27 Units and factorization
- 11R29 Class numbers, class groups, discriminants
- 11R32 Galois theory
- 11R33 Integral representations related to algebraic numbers; Galois module structure of rings of integers [See also
- 11R34 Galois cohomology [See also 12Gxx, 19A31]
- 11R37 Class field theory
- 11R39 Langlands-Weil conjectures, nonabelian class field theory [See also 11Fxx, 22E55]
- 11R42 Zeta functions and L-functions of number fields [See also 11M41, 19F27
- 11R44 Distribution of prime ideals [See also 11N05]
- 11R45 Density theorems
- 11R47 Other analytic theory [See also 11Nxx]
- 11R52 Quaternion and other division algebras: arithmetic, zeta functions

- 11R54 Other algebras and orders, and their zeta and L-functions [See also 11S45, 16Hxx, 16Kxx]
- 11R56 Adèle rings and groups
- 11R58 Arithmetic theory of algebraic function fields [See also 14-XX]
- 11R59 Zeta functions and L-functions of function fields
- 11R60 Cyclotomic function fields (class groups, Bernoulli objects, etc.)
- 11R65 Class groups and Picard groups of orders
- 11R70 K-theory of global fields [See also 19Fxx]
- 11R80 Totally real fields [See also 12J15]
- 11R99 None of the above, but in this section

## 11Sxx Algebraic number theory: local and *p*-adic fields

- 11S05 Polynomials
- 11S15 Ramification and extension theory
- 11S20 Galois theory
- 11S23 Integral representations
- 11S25 Galois cohomology [See also 12Gxx, 16H05]
- **11S31** Class field theory; p-adic formal groups [See also 14L05]
- 11S37 Langlands-Weil conjectures, nonabelian class field theory [See also 11Fxx, 22E50]
- ${\bf 11S40}$  Zeta functions and L-functions [See also 11M41, 19F27]
- 11S45 Algebras and orders, and their zeta functions [See also 11R52, 11R54, 16Hxx, 16Kxx]
- 11S70 K-theory of local fields [See also 19Fxx]
- **11S80** Other analytic theory (analogues of beta and gamma functions, p-adic integration, etc.)
- 11S82 Non-Archimedean dynamical systems [See mainly 37Pxx]
- 11S85 Other nonanalytic theory
- 11S90 Prehomogeneous vector spaces
- 11S99 None of the above, but in this section

## 11Txx Finite fields and commutative rings (number-theoretic aspects)

- 11T06 Polynomials over finite fields
- 11T22 Cyclotomy
- 11T23 Exponential sums
- 11T24 Other character sums and Gauss sums
- ${f 11T30}$  Structure theory for finite fields and commutative rings, number-theoretic aspects
- 11T55 Arithmetic theory of polynomial rings over finite fields
- 11T60 Finite upper half-planes
- 11T71 Algebraic coding theory; cryptography (number-theoretic aspects)
- 11T99 None of the above, but in this section

## 11Uxx Connections of number theory and logic

- 11U05 Decidability (number-theoretic aspects) [See also 03B25]
- 11U07 Ultraproducts (number-theoretic aspects) [See also 03C20]
- 11U09 Model theory (number-theoretic aspects) [See also 03Cxx]
- 11U99 None of the above, but in this section

## 11Yxx Computational number theory {For software etc., see 11-04}

- 11Y05 Factorization
- 11Y11 Primality
- ${f 11Y16}$  Number-theoretic algorithms; complexity [See also  ${f 68Q25}$ ]
- 11Y35 Analytic computations
- 11Y40 Algebraic number theory computations
- 11Y50 Computer solution of Diophantine equations
- 11Y55 Calculation of integer sequences
- 11Y60 Evaluation of number-theoretic constants
- 11Y65 Continued fraction calculations (number-theoretic aspects)
- 11Y70 Values of arithmetic functions; tables
- 11Y99 None of the above, but in this section

## 11Zxx Miscellaneous applications of number theory

- 11Z05 Miscellaneous applications of number theory
- 11Z99 None of the above, but in this section

## 12-XX Field theory and polynomials

- 12-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to field theory
- 12-01 Introductory exposition (textbooks, tutorial papers, etc.) pertaining to field theory
- 12-02 Research exposition (monographs, survey articles) pertaining to field theory
- 12-03 History of field theory [Consider also classification numbers pertaining to Section 01]
- ${f 12\text{-}04}$  Software, source code, etc. for problems pertaining to field theory
- ${f 12\text{-}06}$  Proceedings, conferences, collections, etc. pertaining to field theory

- 12-08 Computational methods for problems pertaining to field theory
- 12-11 Research data for problems pertaining to field theory

### 12Dxx Real and complex fields

- 12D05 Polynomials in real and complex fields: factorization
- 12D10 Polynomials in real and complex fields: location of zeros (algebraic theorems) {For the analytic theory, see  $26C10,\ 30C15$ }
- 12D15 Fields related with sums of squares (formally real fields, Pythagorean fields, etc.) [See also 11Exx]
- 12D99 None of the above, but in this section

### 12Exx General field theory

- 12E05 Polynomials in general fields (irreducibility, etc.)
- 12E10 Special polynomials in general fields
- 12E12 Equations in general fields
- **12E15** Skew fields, division rings [See also 11R52, 11R54, 11S45, 16Kxx]
- 12E20 Finite fields (field-theoretic aspects)
- 12E25 Hilbertian fields; Hilbert's irreducibility theorem
- 12E30 Field arithmetic
- 12E99 None of the above, but in this section

### 12Fxx Field extensions

- 12F05 Algebraic field extensions
- 12F10 Separable extensions, Galois theory
- 12F12 Inverse Galois theory
- 12F15 Inseparable field extensions
- 12F20 Transcendental field extensions
- 12F99 None of the above, but in this section

### 12Gxx Homological methods (field theory)

- 12G05 Galois cohomology [See also 14F22, 16Hxx, 16K50]
- 12G10 Cohomological dimension of fields
- 12G99 None of the above, but in this section

### 12Hxx Differential and difference algebra

- 12H05 Differential algebra [See also 13Nxx]
- 12H10 Difference algebra [See also 39Axx]
- ${\bf 12H20}\,$  Abstract differential equations [See also  ${\bf 34Mxx}]$
- 12H25 p-adic differential equations [See also 11S80, 14G20]
- 12H99 None of the above, but in this section

### 12Jxx Topological fields

- 12J05 Normed fields
- 12J10 Valued fields
- **12J12** Formally p-adic fields
- 12J15 Ordered fields
- 12J17 Topological semifields
- 12J20 General valuation theory for fields [See also 13A18]
- **12J25** Non-Archimedean valued fields [See also 30G06, 32P05, 46S10, 47S10]
- **12J27** Krasner-Tate algebras [See mainly 32P05; see also 46S10, 47S10]
- 12J99 None of the above, but in this section

### 12Kxx Generalizations of fields

- 12K05 Near-fields [See also 16Y30]
- 12K10 Semifields [See also 16Y60]
- 12K99 None of the above, but in this section

## 12Lxx Connections between field theory and logic

- 12L05 Decidability and field theory [See also 03B25]
- 12L10 Ultraproducts and field theory [See also 03C20]
- 12L12 Model theory of fields [See also 03C60]
- 12L15 Nonstandard arithmetic and field theory [See also 03H15]
- 12L99 None of the above, but in this section

### 13-XX Commutative algebra

- 13-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to commutative algebra
- 13-01 Introductory exposition (textbooks, tutorial papers, etc.) pertaining to commutative algebra
- 13-02 Research exposition (monographs, survey articles) pertaining to commutative algebra
- 13-03 History of commutative algebra [Consider also classification numbers pertaining to Section 01]
- ${f 13\text{-}04}$  Software, source code, etc. for problems pertaining to commutative algebra
- ${\bf 13\text{-}06} \ \ {\rm Proceedings}, \ {\rm conferences}, \ {\rm collections}, \ {\rm etc.} \ \ {\rm pertaining} \\ \ \ {\rm to} \ {\rm commutative} \ {\rm algebra}$
- ${\bf 13\text{-}11} \ \ {\rm Research \ data \ for \ problems \ pertaining \ to \ commutative} \\ {\rm algebra}$

### 13Axx General commutative ring theory

- 13A02 Graded rings [See also 16W50]
- 13A05 Divisibility and factorizations in commutative rings [See also 13F15]
- 13A15 Ideals and multiplicative ideal theory in commutative rings
- 13A18 Valuations and their generalizations for commutative rings [See also 12J20]
- 13A30 Associated graded rings of ideals (Rees ring, form ring), analytic spread and related topics
- 13A35 Characteristic p methods (Frobenius endomorphism) and reduction to characteristic p; tight closure [See also 13B22]
- 13A50 Actions of groups on commutative rings; invariant theory [See also 14L24]
- 13A70 General commutative ring theory and combinatorics (zero-divisor graphs, annihilating-ideal graphs, etc.) [See also 05C25, 05E40]
- 13A99 None of the above, but in this section

## 13Bxx Commutative ring extensions and related topics

- 13B02 Extension theory of commutative rings
- 13B05 Galois theory and commutative ring extensions
- 13B10 Morphisms of commutative rings
- 13B21 Integral dependence in commutative rings; going up, going down
- 13B22 Integral closure of commutative rings and ideals [See also 13A35]; integrally closed rings, related rings (Japanese, etc.)
- **13B25** Polynomials over commutative rings [See also 11C08, 11T06, 13F20, 13M10]
- 13B30 Rings of fractions and localization for commutative rings [See also 16S85]
- 13B35 Completion of commutative rings [See also 13J10]
- 13B40 Étale and flat extensions; Henselization; Artin approximation [See also 13J15, 14B12, 14B25]
- 13B99 None of the above, but in this section

## 13Cxx Theory of modules and ideals in commutative rings

- 13C05 Structure, classification theorems for modules and ideals in commutative rings
- 13C10 Projective and free modules and ideals in commutative rings [See also 19A13]
- ${f 13C11}$  Injective and flat modules and ideals in commutative rings
- 13C12 Torsion modules and ideals in commutative rings

- 13C13 Other special types of modules and ideals in commutative rings
- 13C14 Cohen-Macaulay modules [See also 13H10]
- 13C15 Dimension theory, depth, related commutative rings (catenary, etc.)
- 13C20 Class groups [See also 11R29]
- 13C40 Linkage, complete intersections and determinantal ideals [See also 14M06, 14M10, 14M12]
- 13C60 Module categories and commutative rings
- 13C70 Theory of modules and ideals in commutative rings described by combinatorial properties [See also 05C25, 05E40]
- 13C99 None of the above, but in this section

# 13Dxx Homological methods in commutative ring theory {For noncommutative rings, see 16Exx; for general categories, see 18Gxx}

- ${\bf 13D02}$  Syzygies, resolutions, complexes and commutative rings
- 13D03 (Co)homology of commutative rings and algebras (e.g., Hochschild, André-Quillen, cyclic, dihedral, etc.)
- 13D05 Homological dimension and commutative rings
- 13D07 Homological functors on modules of commutative rings (Tor, Ext, etc.)
- 13D09 Derived categories and commutative rings
- 13D10 Deformations and infinitesimal methods in commutative ring theory [See also 14B10, 14B12, 14D15, 32Gxx]
- 13D22 Homological conjectures (intersection theorems) in commutative ring theory
- 13D30 Torsion theory for commutative rings [See also 13C12, 18E40]
- ${\bf 13D40}\,$  Hilbert-Samuel and Hilbert-Kunz functions; Poincaré series
- $13\mathrm{D}45$  Local cohomology and commutative rings [See also  $14\mathrm{B}15]$
- 13D99 None of the above, but in this section

## 13Exx Chain conditions, finiteness conditions in commutative ring theory

- 13E05 Commutative Noetherian rings and modules
- 13E10 Commutative Artinian rings and modules, finitedimensional algebras
- **13E15** Commutative rings and modules of finite generation or presentation; number of generators
- 13E99 None of the above, but in this section

## commutative rings

13F05 Dedekind, Prüfer, Krull and Mori rings and their generalizations

13F07 Euclidean rings and generalizations

**13F10** Principal ideal rings

**13F15** Commutative rings defined by factorization properties (e.g., atomic, factorial, half-factorial) [See also 13A05, 14M05

13F20 Polynomial rings and ideals; rings of integer-valued polynomials [See also 11C08, 13B25]

13F25 Formal power series rings [See also 13J05]

13F30 Valuation rings [See also 13A18]

13F35 Witt vectors and related rings

13F40 Excellent rings

13F45 Seminormal rings

13F50 Rings with straightening laws, Hodge algebras

13F55 Commutative rings defined by monomial ideals; Stanley-Reisner face rings; simplicial complexes [See also 55U10]

13F60 Cluster algebras

13F65 Commutative rings defined by binomial ideals, toric rings, etc. [See also 14M25]

13F70 Other commutative rings defined by combinatorial properties

13F99 None of the above, but in this section

### 13Gxx Integral domains

13G05 Integral domains

13G99 None of the above, but in this section

### 13Hxx Local rings and semilocal rings

13H05 Regular local rings

13H10 Special types (Cohen-Macaulay, Gorenstein, Buchsbaum, etc.) [See also 14M05]

 ${\bf 13H15}$  Multiplicity theory and related topics [See also 14C17

13H99 None of the above, but in this section

### 13Jxx Topological rings and modules [See also 16W60, 16W80]

13J05 Power series rings [See also 13F25]

13J07 Analytical algebras and rings [See also 32B05]

**13J10** Complete rings, completion [See also 13B35]

13J15 Henselian rings [See also 13B40]

**13J20** Global topological rings

13J25 Ordered rings [See also 06F25]

13J30 Real algebra [See also 12D15, 14Pxx]

13J99 None of the above, but in this section

### 13Fxx Arithmetic rings and other special 13Lxx Applications of logic to commutative algebra [See also 03Cxx, 03Hxx]

13L05 Applications of logic to commutative algebra [See also 03Cxx, 03Hxx

13L99 None of the above, but in this section

### 13Mxx Finite commutative rings {For number-theoretic aspects, see 11Txx

13M05 Structure of finite commutative rings

13M10 Polynomials and finite commutative rings

13M99 None of the above, but in this section

#### 13Nxx Differential also algebra See 12H05, 14F10

13N05 Modules of differentials

13N10 Commutative rings of differential operators and their modules [See also 16S32, 32C38]

13N15 Derivations and commutative rings

13N99 None of the above, but in this section

### 13Pxx Computational aspects and applications of commutative rings [See also 14Qxx, 68W30] {For software etc., see 13-04}

13P05 Polynomials, factorization in commutative rings [See also 12-08]

13P10 Gröbner bases: other bases for ideals and modules (e.g., Janet and border bases)

13P15 Solving polynomial systems; resultants

13P20 Computational homological algebra [See also 13Dxx]

13P25 Applications of commutative algebra (e.g., to statistics, control theory, optimization, etc.)

13P99 None of the above, but in this section

### 14-XX Algebraic geometry

14-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to algebraic geometry

14-01 Introductory exposition (textbooks, tutorial papers, etc.) pertaining to algebraic geometry

14-02 Research exposition (monographs, survey articles) pertaining to algebraic geometry

14-03 History of algebraic geometry [Consider also classification numbers pertaining to Section 01]

14-04 Software, source code, etc. for problems pertaining to algebraic geometry

14-06 Proceedings, conferences, collections, etc. pertaining to algebraic geometry

14-11 Research data for problems pertaining to algebraic geometry

### 14Axx Foundations of algebraic geometry

- 14A05 Relevant commutative algebra [See also 13-XX]
- 14A10 Varieties and morphisms
- 14A15 Schemes and morphisms
- 14A20 Generalizations (algebraic spaces, stacks)
- 14A21 Logarithmic algebraic geometry, log schemes
- 14A22 Noncommutative algebraic geometry [See also 16S38]
- 14A23 Geometry over the field with one element
- 14A25 Elementary questions in algebraic geometry
- 14A30 Fundamental constructions in algebraic geometry involving higher and derived categories (homotopical algebraic geometry, derived algebraic geometry, etc.) {For categorical aspects, see 18Fxx, 18Gxx}
- 14A99 None of the above, but in this section

### 14Bxx Local theory in algebraic geometry

- 14B05 Singularities in algebraic geometry [See also 14E15, 14H20, 14J17, 32Sxx, 58Kxx]
- 14B07 Deformations of singularities [See also 14D15, 32S30]
- ${\bf 14B10}$  Infinitesimal methods in algebraic geometry [See also  ${\bf 13D10}]$
- 14B12 Local deformation theory, Artin approximation, etc. [See also  $13B40,\ 13D10$ ]
- **14B15** Local cohomology and algebraic geometry [See also 13D45, 32C36]
- 14B20 Formal neighborhoods in algebraic geometry
- **14B25** Local structure of morphisms in algebraic geometry: étale, flat, etc. [See also 13B40]
- 14B99 None of the above, but in this section

### 14Cxx Cycles and subschemes

- 14C05 Parametrization (Chow and Hilbert schemes)
- 14C15 (Equivariant) Chow groups and rings; motives
- ${\bf 14C17} \ \ {\bf Intersection \ theory, \ characteristic \ classes, \ intersection} \\ {\bf multiplicities \ in \ algebraic \ geometry \ [See \ also \ 13H15]}$
- 14C20 Divisors, linear systems, invertible sheaves
- **14C21** Pencils, nets, webs in algebraic geometry [See also 53A60]
- 14C22 Picard groups
- 14C25 Algebraic cycles
- $\begin{array}{c} \textbf{14C30} \ \ \text{Transcendental methods, Hodge theory (algebrogeometric aspects)} \ \ [\text{See also 14D07}, \ 32\text{G20}, \ 32\text{J25}, \\ 32\text{S35}], \ \ \text{Hodge conjecture} \end{array}$
- 14C34 Torelli problem [See also 32G20]
- ${\bf 14C35}$  Applications of methods of algebraic K-theory in algebraic geometry [See also 19Exx]
- 14C40 Riemann-Roch theorems [See also 19E20, 19L10]
- 14C99 None of the above, but in this section

## 14Dxx Families, fibrations in algebraic geometry

- 14D05 Structure of families (Picard-Lefschetz, monodromy, etc.)
- 14D06 Fibrations, degenerations in algebraic geometry
- 14D07 Variation of Hodge structures (algebro-geometric aspects) [See also 32G20]
- 14D10 Arithmetic ground fields (finite, local, global) and families or fibrations
- 14D15 Formal methods and deformations in algebraic geometry [See also 13D10, 14B07, 32Gxx]
- 14D20 Algebraic moduli problems, moduli of vector bundles  $\{For\ analytic\ moduli\ problems,\ see\ 32G13\}$
- 14D21 Applications of vector bundles and moduli spaces in mathematical physics (twistor theory, instantons, quantum field theory) [See also 32L25, 81Txx]
- 14D22 Fine and coarse moduli spaces
- 14D23 Stacks and moduli problems
- 14D24 Geometric Langlands program (algebro-geometric aspects) [See also 22E57]
- 14D99 None of the above, but in this section

### 14Exx Birational geometry

- 14E05 Rational and birational maps
- 14E07 Birational automorphisms, Cremona group and generalizations
- 14E08 Rationality questions in algebraic geometry [See also 14M20]
- 14E15 Global theory and resolution of singularities (algebrogeometric aspects) [See also 14B05, 32S20, 32S45]
- 14E16 McKay correspondence
- 14E18 Arcs and motivic integration
- 14E20 Coverings in algebraic geometry [See also 14H30]
- 14E22 Ramification problems in algebraic geometry [See also 11S15]
- 14E25 Embeddings in algebraic geometry
- 14E30 Minimal model program (Mori theory, extremal rays)
- 14E99 None of the above, but in this section

### 14Fxx (Co)homology theory in algebraic 14G35 Modular and Shimura varieties [See also 11F41, geometry [See also 13Dxx]

- 14F06 Sheaves in algebraic geometry [See also 14F07, 14H60, 14J60, 18F20, 32Lxx, 46M20
- 14F07 Derived categories of sheaves, dg categories, and related constructions in algebraic geometry [See also 14A30, 14F06, 18Gxx
- 14F10 Differentials and other special sheaves; D-modules; Bernstein-Sato ideals and polynomials [See also 13Nxx, 32C38
- 14F17 Vanishing theorems in algebraic geometry [See also
- 14F18 Multiplier ideals
- 14F20 Étale and other Grothendieck topologies and (co)homologies
- **14F22** Brauer groups of schemes [See also 12G05, 16K50]
- 14F25 Classical real and complex (co)homology in algebraic geometry
- **14F30** p-adic cohomology, crystalline cohomology
- 14F35 Homotopy theory and fundamental groups in algebraic geometry [See also 14H30]
- 14F40 de Rham cohomology and algebraic geometry [See also 14C30, 32C35, 32L10]
- 14F42 Motivic cohomology; motivic homotopy theory [See also 19E15]
- 14F43 Other algebro-geometric (co)homologies (e.g., intersection, equivariant, Lawson, Deligne (co)homologies)
- 14F45 Topological properties in algebraic geometry
- 14F99 None of the above, but in this section

### 14Gxx Arithmetic problems in algebraic geometry; Diophantine geometry [See also 11Dxx, 11Gxx

- 14G05 Rational points
- 14G10 Zeta functions and related questions in algebraic geometry (e.g., Birch-Swinnerton-Dyer conjecture) [See also 11G40]
- 14G12 Hasse principle, weak and strong approximation, Brauer-Manin obstruction [See also 14F22]
- 14G15 Finite ground fields in algebraic geometry
- 14G17 Positive characteristic ground fields in algebraic geometry
- **14G20** Local ground fields in algebraic geometry
- 14G22 Rigid analytic geometry
- 14G25 Global ground fields in algebraic geometry
- 14G27 Other nonalgebraically closed ground fields in algebraic geometry
- 14G32 Universal profinite groups (relationship to moduli spaces, projective and moduli towers, Galois theory)

- 11F46, 11G18
- 14G40 Arithmetic varieties and schemes; Arakelov theory; heights [See also 11G50, 37P30]
- 14G45 Perfectoid spaces and mixed characteristic
- 14G50 Applications to coding theory and cryptography of arithmetic geometry [See also 94A60, 94B27, 94B40]
- 14G99 None of the above, but in this section

### 14Hxx Curves in algebraic geometry

- 14H05 Algebraic functions and function fields in algebraic geometry [See also 11R58]
- 14H10 Families, moduli of curves (algebraic)
- 14H15 Families, moduli of curves (analytic) [See also 30F10, 32G15
- 14H20 Singularities of curves, local rings [See also 13Hxx, 14B05
- 14H25 Arithmetic ground fields for curves [See also 11Dxx, 11G05, 14Gxx
- 14H30 Coverings of curves, fundamental group [See also 14E20, 14F35
- 14H37 Automorphisms of curves
- 14H40 Jacobians, Prym varieties [See also 32G20]
- 14H42 Theta functions and curves; Schottky problem [See also 14K25, 32G20]
- 14H45 Special algebraic curves and curves of low genus
- 14H50 Plane and space curves
- 14H51 Special divisors on curves (gonality, Brill-Noether theory)
- 14H52 Elliptic curves [See also 11G05, 11G07, 14Kxx]
- 14H55 Riemann surfaces; Weierstrass points; gap sequences [See also 30Fxx]
- 14H57 Dessins d'enfants theory {For arithmetic aspects, see 11G32}
- 14H60 Vector bundles on curves and their moduli [See also 14D20, 14F06, 14J60
- 14H70 Relationships between algebraic curves and integrable systems
- 14H81 Relationships between algebraic curves and physics
- 14H99 None of the above, but in this section

## 14Jxx Surfaces and higher-dimensional varieties {For analytic theory, see 32Jxx}

- 14J10 Families, moduli, classification: algebraic theory
- 14J15 Moduli, classification: analytic theory; relations with modular forms [See also 32G13]
- **14J17** Singularities of surfaces or higher-dimensional varieties [See also 14B05, 14E15, 32S05, 32S25]
- 14J20 Arithmetic ground fields for surfaces or higher-dimensional varieties [See also 11Dxx, 11G25, 11G35, 14Gxx]
- **14J25** Special surfaces {For Hilbert modular surfaces, see 14G35}
- 14J26 Rational and ruled surfaces
- 14J27 Elliptic surfaces, elliptic or Calabi-Yau fibrations
- 14J28 K3 surfaces and Enriques surfaces
- 14J29 Surfaces of general type
- **14J30** 3-folds
- 14J32 Calabi-Yau manifolds (algebro-geometric aspects) [See also 32Q25]
- 14J33 Mirror symmetry (algebro-geometric aspects) [See also 11G42, 53D37]
- **14J35** 4-folds
- **14J40** *n*-folds (n > 4)
- 14J42 Holomorphic symplectic varieties, hyper-Kähler varieties
- 14J45 Fano varieties
- 14J50 Automorphisms of surfaces and higher-dimensional varieties
- 14J60 Vector bundles on surfaces and higher-dimensional varieties, and their moduli [See also 14D20, 14F06, 14H60, 32Lxx]
- 14J70 Hypersurfaces and algebraic geometry
- 14J80 Topology of surfaces (Donaldson polynomials, Seiberg-Witten invariants)
- 14J81 Relationships with physics
- 14J99 None of the above, but in this section

#### 14Kxx Abelian varieties and schemes

- 14K02 Isogeny
- 14K05 Algebraic theory of abelian varieties
- 14K10 Algebraic moduli of abelian varieties, classification [See also 11G15]
- 14K12 Subvarieties of abelian varieties
- $\bf 14K15$  Arithmetic ground fields for abelian varieties [See also  $\bf 11Dxx,\, 11Fxx,\, 11G10,\, 14Gxx]$
- 14K20 Analytic theory of abelian varieties; abelian integrals and differentials

- 14K22 Complex multiplication and abelian varieties [See also 11G15]
- 14K25 Theta functions and abelian varieties [See also 14H42]
- 14K30 Picard schemes, higher Jacobians [See also 14H40, 32G20]
- 14K99 None of the above, but in this section

## 14Lxx Algebraic groups {For linear algebraic groups, see 20Gxx; for Lie algebras, see 17B45}

- **14L05** Formal groups, *p*-divisible groups [See also 55N22]
- **14L10** Group varieties
- 14L15 Group schemes
- $\bf 14L17$  Affine algebraic groups, hyperalgebra constructions [See also 17B45, 18C40]
- 14L24 Geometric invariant theory [See also 13A50]
- $14L30\,$  Group actions on varieties or schemes (quotients) [See also  $13A50,\ 14L24,\ 14M17]$
- ${\bf 14L35}$  Classical groups (algebro-geometric aspects) [See also  ${\bf 20Gxx},\,{\bf 51N30}]$
- 14L40 Other algebraic groups (geometric aspects)
- 14L99 None of the above, but in this section

### 14Mxx Special varieties

- **14M05** Varieties defined by ring conditions (factorial, Cohen-Macaulay, seminormal) [See also 13F15, 13F45, 13H10]
- 14M06 Linkage [See also 13C40]
- 14M07 Low codimension problems in algebraic geometry
- 14M10 Complete intersections [See also 13C40]
- 14M12 Determinantal varieties [See also 13C40]
- 14M15 Grassmannians, Schubert varieties, flag manifolds [See also 32M10, 51M35]
- 14M17 Homogeneous spaces and generalizations [See also 32M10, 53C30, 57T15]
- **14M20** Rational and unirational varieties [See also 14E08]
- 14M22 Rationally connected varieties
- ${\bf 14M25}\,$  Toric varieties, Newton polyhedra, Okounkov bodies [See also  ${\bf 52B20}]$
- 14M27 Compactifications; symmetric and spherical varieties
- 14M30 Supervarieties [See also 32C11, 58A50]
- 14M35 Character varieties
- 14M99 None of the above, but in this section

## 14Nxx Projective and enumerative algebraic geometry [See also 51-XX]

- 14N05 Projective techniques in algebraic geometry [See also 51N35]
- 14N07 Secant varieties, tensor rank, varieties of sums of powers
- 14N10 Enumerative problems (combinatorial problems) in algebraic geometry
- 14N15 Classical problems, Schubert calculus
- 14N20 Configurations and arrangements of linear subspaces
- 14N25 Varieties of low degree
- 14N30 Adjunction problems
- 14N35 Gromov-Witten invariants, quantum cohomology, Gopakumar-Vafa invariants, Donaldson-Thomas invariants (algebro-geometric aspects) [See also 53D45]
- 14N99 None of the above, but in this section

## 14Pxx Real algebraic and real-analytic geometry

- 14P05 Real algebraic sets [See also 12D15, 13J30]
- 14P10 Semialgebraic sets and related spaces
- ${\bf 14P15}\,$  Real-analytic and semi-analytic sets [See also 32B20,  $32{\rm C}05]$
- 14P20 Nash functions and manifolds [See also 32C07, 58A07]
- 14P25 Topology of real algebraic varieties
- 14P99 None of the above, but in this section

## 14Qxx Computational aspects in algebraic geometry {For software etc., see 14-04} [See also 12-08, 13Pxx, 68W30]

- 14Q05 Computational aspects of algebraic curves [See also  $14\mathrm{Hxx}]$
- ${\bf 14Q10}\,$  Computational aspects of algebraic surfaces [See also  ${\bf 14Jxx}]$
- 14Q15 Computational aspects of higher-dimensional varieties [See also 14Jxx, 14Mxx]
- 14Q20 Effectivity, complexity and computational aspects of algebraic geometry
- 14Q25 Computational algebraic geometry over arithmetic ground fields [See also 14Gxx, 14H25, 14Kxx]
- 14Q30 Computational real algebraic geometry [See also 14Pxx]
- 14Q65 Geometric aspects of numerical algebraic geometry [See also 65H14]
- 14Q99 None of the above, but in this section

### 14Rxx Affine geometry

- 14R05 Classification of affine varieties
- **14R10** Affine spaces (automorphisms, embeddings, exotic structures, cancellation problem)
- 14R15 Jacobian problem [See also 13F20]
- 14R20 Group actions on affine varieties [See also 13A50, 14L30]
- **14R25** Affine fibrations [See also 14D06]
- 14R99 None of the above, but in this section

## 14Txx Tropical geometry [See also 12K10, 14M25, 14N10, 52B20]

- 14T10 Foundations of tropical geometry and relations with algebra {For algebraic aspects, see 15A80}
- 14T15 Combinatorial aspects of tropical varieties
- 14T20 Geometric aspects of tropical varieties
- 14T25 Arithmetic aspects of tropical varieties
- 14T90 Applications of tropical geometry
- 14T99 None of the above, but in this section

## 15-XX Linear and multilinear algebra; matrix theory

- 15-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to linear algebra
- 15-01 Introductory exposition (textbooks, tutorial papers, etc.) pertaining to linear algebra
- 15-02 Research exposition (monographs, survey articles) pertaining to linear algebra
- 15-03 History of linear algebra [Consider also classification numbers pertaining to Section 01]
- ${\bf 15\text{-}04}\,$  Software, source code, etc. for problems pertaining to linear algebra
- ${\bf 15\text{-}06}$  Proceedings, conferences, collections, etc. pertaining to linear algebra
- 15-11 Research data for problems pertaining to linear algebra

### 15Axx Basic linear algebra

- 15A03 Vector spaces, linear dependence, rank, lineability
- ${\bf 15A04} \ \ {\bf Linear} \ {\bf transformations}, \ {\bf semilinear} \ {\bf transformations}$
- 15A06 Linear equations (linear algebraic aspects)
- 15A09 Theory of matrix inversion and generalized inverses
- 15A10 Applications of generalized inverses
- **15A12** Conditioning of matrices [See also 65F35]
- **15A15** Determinants, permanents, traces, other special matrix functions [See also 19B10, 19B14]
- 15A16 Matrix exponential and similar functions of matrices
- 15A18 Eigenvalues, singular values, and eigenvectors
- 15A20 Diagonalization, Jordan forms
- 15A21 Canonical forms, reductions, classification

- 15A22 Matrix pencils [See also 47A56]
- 15A23 Factorization of matrices
- 15A24 Matrix equations and identities
- 15A27 Commutativity of matrices
- 15A29 Inverse problems in linear algebra
- 15A30 Algebraic systems of matrices [See also 16S50, 20Gxx, 20Hxx]
- 15A39 Linear inequalities of matrices
- 15A42 Inequalities involving eigenvalues and eigenvectors
- 15A45 Miscellaneous inequalities involving matrices
- 15A54 Matrices over function rings in one or more variables
- 15A60 Norms of matrices, numerical range, applications of functional analysis to matrix theory [See also 65F35, 65J05]
- 15A63 Quadratic and bilinear forms, inner products [See mainly 11Exx]
- 15A66 Clifford algebras, spinors
- 15A67 Applications of Clifford algebras to physics, etc.
- 15A69 Multilinear algebra, tensor calculus
- 15A72 Vector and tensor algebra, theory of invariants [See also 13A50, 14L24]
- 15A75 Exterior algebra, Grassmann algebras
- 15A78 Other algebras built from modules
- 15A80 Max-plus and related algebras
- 15A83 Matrix completion problems
- 15A86 Linear preserver problems
- 15A99 None of the above, but in this section

### 15Bxx Special matrices

- 15B05 Toeplitz, Cauchy, and related matrices
- 15B10 Orthogonal matrices
- 15B15 Fuzzy matrices
- 15B30 Matrix Lie algebras
- 15B33 Matrices over special rings (quaternions, finite fields, etc.)
- 15B34 Boolean and Hadamard matrices
- 15B35 Sign pattern matrices
- 15B36 Matrices of integers [See also 11C20]
- ${f 15B48}$  Positive matrices and their generalizations; cones of matrices
- 15B51 Stochastic matrices
- **15B52** Random matrices (algebraic aspects) {For probabilistic aspects, see 60B20}
- 15B57 Hermitian, skew-Hermitian, and related matrices
- 15B99 None of the above, but in this section

# 16-XX Associative rings and algebras {For the commutative case, see 13-XX}

- 16-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to associative rings and algebras
- 16-01 Introductory exposition (textbooks, tutorial papers, etc.) pertaining to associative rings and algebras
- 16-02 Research exposition (monographs, survey articles) pertaining to associative rings and algebras
- 16-03 History of associative rings and algebras [Consider also classification numbers pertaining to Section 01]
- 16-04 Software, source code, etc. for problems pertaining to associative rings and algebras
- **16-06** Proceedings, conferences, collections, etc. pertaining to associative rings and algebras
- ${f 16\text{-}11}$  Research data for problems pertaining to associative rings and algebras

### 16Bxx General and miscellaneous

- 16B50 Category-theoretic methods and results in associative algebras (except as in 16D90) [See also 18-XX]
- 16B70 Applications of logic in associative algebras [See also 03Cxx]
- 16B99 None of the above, but in this section

## 16Dxx Modules, bimodules and ideals in associative algebras

- 16D10 General module theory in associative algebras
- 16D20 Bimodules in associative algebras
- 16D25 Ideals in associative algebras
- **16D30** Infinite-dimensional simple rings (except as in 16Kxx)
- ${\bf 16D40}\,$  Free, projective, and flat modules and ideals in associative algebras [See also 19A13]
- ${\bf 16D50}$  Injective modules, self-injective associative rings [See also  ${\bf 16L60}]$
- 16D60 Simple and semisimple modules, primitive rings and ideals in associative algebras
- $\begin{array}{c} \textbf{16D70} \ \ \text{Structure and classification for modules, bimodules} \\ \ \ \text{and ideals (except as in 16Gxx), direct sum decomposition and cancellation in associative algebras)} \\ \end{array}$
- 16D80 Other classes of modules and ideals in associative algebras [See also  $16\mathrm{G}50]$
- 16D90 Module categories in associative algebras [See also 16Gxx, 16S90]; module theory in a category-theoretic context; Morita equivalence and duality
- 16D99 None of the above, but in this section

### 16Exx Homological methods in associative 16Kxx Division rings and semisimple algebras {For commutative rings, see 13Dxx; for general categories, see 18Gxx}

16E05 Syzygies, resolutions, complexes in associative algebras

16E10 Homological dimension in associative algebras

**16E20** Grothendieck groups, K-theory, etc. [See also 18F30, 19Axx, 19D50

16E30 Homological functors on modules (Tor, Ext, etc.) in associative algebras

16E35 Derived categories and associative algebras

16E40 (Co)homology of rings and associative algebras (e.g., Hochschild, cyclic, dihedral, etc.)

16E45 Differential graded algebras and applications (associative algebraic aspects)

16E50 von Neumann regular rings and generalizations (associative algebraic aspects)

16E60 Semihereditary and hereditary rings, free ideal rings, Sylvester rings, etc.

16E65 Homological conditions on associative rings (generalizations of regular, Gorenstein, Cohen-Macaulay rings, etc.)

16E99 None of the above, but in this section

### 16Gxx Representation theory of associative rings and algebras

**16G10** Representations of associative Artinian rings

16G20 Representations of quivers and partially ordered sets

16G30 Representations of orders, lattices, algebras over commutative rings [See also 16Hxx]

16G50 Cohen-Macaulay modules in associative algebras

**16G60** Representation type (finite, tame, wild, etc.) of associative algebras

**16G70** Auslander-Reiten sequences (almost split sequences) and Auslander-Reiten guivers

16G99 None of the above, but in this section

### 16Hxx Associative algebras and orders {For arithmetic aspects, 11R52. 11R54, 11S45; for representation theory, see 16G30}

16H05 Separable algebras (e.g., quaternion algebras, Azumaya algebras, etc.)

16H10 Orders in separable algebras

**16H15** Commutative orders

16H20 Lattices over orders

16H99 None of the above, but in this section

## Artin rings [See also 12E15, 15A30]

16K20 Finite-dimensional division rings {For crossed products, see 16S35}

16K40 Infinite-dimensional and general division rings

16K50 Brauer groups (algebraic aspects) [See also 12G05, 14F22

16K99 None of the above, but in this section

### 16Lxx Local rings and generalizations

16L30 Noncommutative local and semilocal rings, perfect rings

**16L60** Quasi-Frobenius rings [See also 16D50]

16L99 None of the above, but in this section

### 16Nxx Radicals and radical properties of associative rings

16N20 Jacobson radical, quasimultiplication

16N40 Nil and nilpotent radicals, sets, ideals, associative rings

16N60 Prime and semiprime associative rings [See also 16D60, 16U10

16N80 General radicals and associative rings {For radicals in module categories, see 16S90}

16N99 None of the above, but in this section

### 16Pxx Chain conditions, growth conditions, and other forms of finiteness for associative rings and algebras

16P10 Finite rings and finite-dimensional associative algebras {For semisimple, see 16K20; for commutative, see 11Txx, 13Mxx}

16P20 Artinian rings and modules (associative rings and al-

16P40 Noetherian rings and modules (associative rings and algebras)

16P50 Localization and associative Noetherian rings [See also 16U20]

16P60 Chain conditions on annihilators and summands: Goldie-type conditions [See also 16U20], Krull dimension (associative rings and algebras)

16P70 Chain conditions on other classes of submodules, ideals, subrings, etc.; coherence (associative rings and al-

16P90 Growth rate, Gelfand-Kirillov dimension

16P99 None of the above, but in this section

### 16Rxx Rings with polynomial identity

- ${f 16R10}$  T-ideals, identities, varieties of associative rings and algebras
- 16R20 Semiprime p.i. rings, rings embeddable in matrices over commutative rings
- 16R30 Trace rings and invariant theory (associative rings and algebras)
- 16R40 Identities other than those of matrices over commutative rings
- 16R50 Other kinds of identities (generalized polynomial, rational, involution)
- 16R60 Functional identities (associative rings and algebras)
- 16R99 None of the above, but in this section

## 16Sxx Associative rings and algebras arising under various constructions

- **16S10** Associative rings determined by universal properties (free algebras, coproducts, adjunction of inverses, etc.)
- 16S15 Finite generation, finite presentability, normal forms (diamond lemma, term-rewriting)
- 16S20 Centralizing and normalizing extensions
- 16S30 Universal enveloping algebras of Lie algebras [See mainly 17B35]
- 16S32 Rings of differential operators (associative algebraic aspects) [See also 13N10, 32C38]
- 16S34 Group rings [See also 20C05, 20C07], Laurent polynomial rings (associative algebraic aspects)
- 16S35 Twisted and skew group rings, crossed products
- 16S36 Ordinary and skew polynomial rings and semigroup rings [See also 20M25]
- 16S37 Quadratic and Koszul algebras
- 16S38 Rings arising from noncommutative algebraic geometry [See also 14A22]
- ${\bf 16S40}$  Smash products of general Hopf actions [See also  ${\bf 16T05}]$
- **16S50** Endomorphism rings; matrix rings [See also 15-XX]
- 16S60 Associative rings of functions, subdirect products, sheaves of rings
- 16S70 Extensions of associative rings by ideals
- 16S80 Deformations of associative rings [See also 13D10, 14D15]
- 16S85 Associative rings of fractions and localizations [See also 13B30]
- 16S88 Leavitt path algebras
- 16S90 Torsion theories; radicals on module categories (associative algebraic aspects) [See also 13D30, 18E40] {For radicals of rings, see 16Nxx}
- 16S99 None of the above, but in this section

## 16Txx Hopf algebras, quantum groups and related topics

- 16T05 Hopf algebras and their applications [See also 16S40, 57T05]
- 16T10 Bialgebras
- 16T15 Coalgebras and comodules; corings
- 16T20 Ring-theoretic aspects of quantum groups [See also 17B37, 20G42, 81R50]
- 16T25 Yang-Baxter equations
- 16T30 Connections of associative rings and algebras with combinatorics
- 16T99 None of the above, but in this section

### 16Uxx Conditions on elements

- 16U10 Integral domains (associative rings and algebras)
- 16U20 Ore rings, multiplicative sets, Ore localization
- 16U30 Divisibility, noncommutative UFDs
- 16U40 Idempotent elements
- 16U50 Generalized inverses
- 16U60 Units, groups of units (associative rings and algebras)
- 16U70 Center, normalizer (invariant elements) (associative rings and algebras)
- 16U80 Generalizations of commutativity (associative rings and algebras)
- 16U99 None of the above, but in this section

## 16Wxx Associative rings and algebras with additional structure

- 16W10 Rings with involution; Lie, Jordan and other nonassociative structures [See also 17B60, 17C50, 46Kxx]
- 16W20 Automorphisms and endomorphisms
- 16W22 Actions of groups and semigroups; invariant theory (associative rings and algebras)
- 16W25 Derivations, actions of Lie algebras
- 16W50 Graded rings and modules (associative rings and algebras)
- 16W55 "Super" (or "skew") structure [See also 17A70, 17Bxx, 17C70] {For exterior algebras, see 15A75; for Clifford algebras, see 11E88, 15A66}
- ${\bf 16W60} \ \ {\bf Valuations, completions, formal power series and related constructions (associative rings and algebras) [See also $13{\rm Jxx}]$$
- 16W70 Filtered associative rings; filtrational and graded techniques
- **16W80** Topological and ordered rings and modules [See also 06F25, 13Jxx]
- 16W99 None of the above, but in this section

### 16Yxx Generalizations {For nonassocia- 17A42 Other n-ary compositions $(n \ge 3)$ tive rings, see 17-XX

16Y20 Hyperrings

16Y30 Near-rings [See also 12K05]

16Y60 Semirings [See also 12K10]

**16Y80**  $\Gamma$  and fuzzy structures

16Y99 None of the above, but in this section

### 16Zxx Computational aspects of associative rings {For software etc., see 16-04}

16Z05 Computational aspects of associative rings [See also 68W30

16Z10 Gröbner-Shirshov bases

16Z99 None of the above, but in this section

### 17-XX Nonassociative rings and algebras

- 17-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to nonassociative rings and algebras
- 17-01 Introductory exposition (textbooks, tutorial papers, etc.) pertaining to nonassociative rings and algebras
- 17-02 Research exposition (monographs, survey articles) pertaining to nonassociative rings and algebras
- 17-03 History of nonassociative rings and algebras [Consider also classification numbers pertaining to Section 01]
- 17-04 Software, source code, etc. for problems pertaining to nonassociative rings and algebras
- 17-06 Proceedings, conferences, collections, etc. pertaining to nonassociative rings and algebras
- 17-08 Computational methods for problems pertaining to nonassociative rings and algebras
- 17-11 Research data for problems pertaining to nonassociative rings and algebras

### 17Axx General nonassociative rings

17A01 General theory of nonassociative rings and algebras

17A05 Power-associative rings

17A15 Noncommutative Jordan algebras

17A20 Flexible algebras

17A30 Nonassociative algebras satisfying other identities

17A32 Leibniz algebras

17A35 Nonassociative division algebras

17A36 Automorphisms, derivations, other operators (nonassociative rings and algebras)

17A40 Ternary compositions

17A45 Quadratic algebras (but not quadratic Jordan algebras)

17A50 Free nonassociative algebras

17A60 Structure theory for nonassociative algebras

17A61 Gröbner-Shirshov bases in nonassociative algebras

17A65 Radical theory (nonassociative rings and algebras)

17A70 Superalgebras

17A75 Composition algebras

17A80 Valued algebras

17A99 None of the above, but in this section

### 17Bxx Lie algebras and Lie superalgebras {For Lie groups, see 22Exx}

17B01 Identities, free Lie (super)algebras

17B05 Structure theory for Lie algebras and superalgebras

17B08 Coadjoint orbits; nilpotent varieties

17B10 Representations of Lie algebras and Lie superalgebras, algebraic theory (weights)

17B15 Representations of Lie algebras and Lie superalgebras, analytic theory

17B20 Simple, semisimple, reductive (super)algebras

17B22 Root systems

17B25 Exceptional (super)algebras

17B30 Solvable, nilpotent (super)algebras

17B35 Universal enveloping (super)algebras [See also 16S30]

17B37 Quantum groups (quantized enveloping algebras) and related deformations [See also 16T20, 20G42, 81R50, 82B23]

17B38 Yang-Baxter equations and Rota-Baxter operators

17B40 Automorphisms, derivations, other operators for Lie algebras and super algebras

17B45 Lie algebras of linear algebraic groups [See also 14Lxx and 20Gxx

17B50 Modular Lie (super)algebras

17B55 Homological methods in Lie (super)algebras

17B56 Cohomology of Lie (super)algebras

17B60 Lie (super)algebras associated with other structures (associative, Jordan, etc.) [See also 16W10, 17C40,

17B61 Hom-Lie and related algebras

17B62 Lie bialgebras; Lie coalgebras

17B63 Poisson algebras

17B65 Infinite-dimensional Lie (super)algebras [See also 22E65]

17B66 Lie algebras of vector fields and related (super) alge-

17B67 Kac-Moody (super)algebras; extended affine Lie algebras; toroidal Lie algebras

- 17B68 Virasoro and related algebras
- 17B69 Vertex operators; vertex operator algebras and related structures
- 17B70 Graded Lie (super)algebras
- 17B75 Color Lie (super)algebras
- ${\bf 17B80}\,$  Applications of Lie algebras and superalgebras to integrable systems
- 17B81 Applications of Lie (super)algebras to physics, etc.
- 17B99 None of the above, but in this section

## 17Cxx Jordan algebras (algebras, triples and pairs)

- 17C05 Identities and free Jordan structures
- 17C10 Structure theory for Jordan algebras
- 17C17 Radicals in Jordan algebras
- 17C20 Simple, semisimple Jordan algebras
- 17C27 Idempotents, Peirce decompositions
- 17C30 Associated groups, automorphisms of Jordan algebras
- 17C36 Associated manifolds of Jordan algebras
- 17C37 Associated geometries of Jordan algebras
- 17C40 Exceptional Jordan structures
- 17C50 Jordan structures associated with other structures [See also 16W10]
- 17C55 Finite-dimensional structures of Jordan algebras
- 17C60 Division algebras and Jordan algebras
- $\bf 17C65$  Jordan structures on Banach spaces and algebras [See also  $\bf 46H70,\, 46L70]$
- 17C70 Super structures
- 17C90 Applications of Jordan algebras to physics, etc.
- 17C99 None of the above, but in this section

## 17Dxx Other nonassociative rings and algebras

- 17D05 Alternative rings
- 17D10 Mal'tsev rings and algebras
- 17D15 Right alternative rings
- **17D20**  $(\gamma, \delta)$ -rings, including (1, -1)-rings
- ${\bf 17D25} \ \ {\bf Lie}\hbox{-admissible algebras}$
- 17D30 (non-Lie) Hom algebras and topics
- 17D92 Genetic algebras
- 17D99 None of the above, but in this section

- 18-XX Category theory; homological algebra {For commutative rings, see 13Dxx; for associative rings, see 16Exx; for groups, see 20Jxx; for topological groups and related structures, see 57Txx; for algebraic topology, see also 55Nxx, 55Uxx}
- 18-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to category theory
- **18-01** Introductory exposition (textbooks, tutorial papers, etc.) pertaining to category theory
- 18-02 Research exposition (monographs, survey articles) pertaining to category theory
- 18-03 History of category theory [Consider also classification numbers pertaining to Section 01]
- 18-04 Software, source code, etc. for problems pertaining to category theory
- **18-06** Proceedings, conferences, collections, etc. pertaining to category theory
- 18-08 Computational methods for problems pertaining to category theory
- ${f 18-11}$  Research data for problems pertaining to category theory

### 18Axx General theory of categories and functors

- 18A05 Definitions and generalizations in theory of categories
- 18A10 Graphs, diagram schemes, precategories
- ${\bf 18A15}\,$  Foundations, relations to logic and deductive systems [See also 03-XX]
- **18A20** Epimorphisms, monomorphisms, special classes of morphisms, null morphisms
- 18A22 Special properties of functors (faithful, full, etc.)
- 18A23 Natural morphisms, dinatural morphisms
- 18A25 Functor categories, comma categories
- 18A30 Limits and colimits (products, sums, directed limits, pushouts, fiber products, equalizers, kernels, ends and coends, etc.)
- **18A32** Factorization systems, substructures, quotient structures, congruences, amalgams
- ${\bf 18A35} \ \ {\bf Categories} \ \ {\bf admitting} \ \ {\bf limits} \ \ ({\bf complete} \ \ {\bf categories}), \\ {\bf functors} \ {\bf preserving} \ {\bf limits}, \ {\bf completions}$
- 18A40 Adjoint functors (universal constructions, reflective subcategories, Kan extensions, etc.)
- 18A50 Graded categories (general) {For dg categories, see 18G35}
- 18A99 None of the above, but in this section

### 18Bxx Special categories

- 18B05 Categories of sets, characterizations [See also 03-XX]
- 18B10 Categories of spans/cospans, relations, or partial maps
- 18B15 Embedding theorems, universal categories [See also 18E20]
- 18B20 Categories of machines, automata [See also 03D05, 68Qxx]
- **18B25** Topoi [See also 03G30, 18F10]
- **18B35** Preorders, orders, domains and lattices (viewed as categories) [See also 06-XX]
- **18B40** Groupoids, semigroupoids, semigroups, groups (viewed as categories) [See also 20Axx, 20L05, 20Mxx]
- 18B50 Extensive, distributive, and adhesive categories
- 18B99 None of the above, but in this section

### 18Cxx Categories and theories

- 18C05 Equational categories [See also 03C05, 08C05]
- 18C10 Theories (e.g., algebraic theories), structure, and semantics [See also 03G30]
- 18C15 Monads (= standard construction, monad or triad), algebras for a triple, homology and derived functors for triples [See also 18Gxx] {For functional programming, see also 68N18}
- 18C20 Eilenberg-Moore and Kleisli constructions for monads
- **18C30** Sketches and generalizations
- 18C35 Accessible and locally presentable categories
- 18C40 Structured objects in a category (group objects, etc.)
- **18C50** Categorical semantics of formal languages [See also 68Q55, 68Q65]
- 18C99 None of the above, but in this section

### 18Dxx Categorical structures

- 18D15 Closed categories (closed monoidal and Cartesian closed categories, etc.)
- 18D20 Enriched categories (over closed or monoidal categories)
- 18D25 Actions of a monoidal category, tensorial strength {For functional programming, see also 68N18}
- 18D30 Fibered categories
- 18D40 Internal categories and groupoids {For double categories, see 18N10; for topological groupoids, see 22A22; for Lie groupoids, see 58H05}
- **18D60** Profunctors (= correspondences, distributors, modules)
- **18D65** Proarrow equipments, Yoneda structures, KZ doctrines (lax idempotent monads)
- 18D70 Formal category theory
- 18D99 None of the above, but in this section

### 18Exx Categorical algebra

- 18E05 Preadditive, additive categories
- 18E08 Regular categories, Barr-exact categories
- 18E10 Abelian categories, Grothendieck categories
- 18E13 Protomodular categories, semi-abelian categories, Mal'tsev categories [See also 08B05 and 18B10]
- **18E20** Categorical embedding theorems [See also 18B15]
- **18E35** Localization of categories, calculus of fractions {For homotopical aspects, see also 18N45, 55P60}
- 18E40 Torsion theories, radicals [See also 13D30, 16S90]
- 18E45 Definable subcategories and connections with model theory [See also 13C60]
- 18E50 Categorical Galois theory
- 18E99 None of the above, but in this section

### 18Fxx Categories in geometry and topology

- 18F05 Local categories and functors
- 18F10 Grothendieck topologies and Grothendieck topol [See also 14F20, 18B25]
- **18F15** Abstract manifolds and fiber bundles (category-theoretic aspects) [See also 55Rxx, 57Pxx]
- **18F20** Presheaves and sheaves, stacks, descent conditions (category-theoretic aspects) [See also 14F06, 14F07, 32C35, 32L10, 54B40, 55N30]
- $\begin{array}{lll} \textbf{18F25} & \textbf{Algebraic} \ K\text{-theory and} \ L\text{-theory (category-theoretic aspects)} \ [\textbf{See also } 11\textbf{Exx}, \ 11\textbf{R70}, \ 11\textbf{S70}, \ 12\text{-XX}, \ 13\textbf{D15}, \\ 14\textbf{Cxx}, \ 16\textbf{E20}, \ 19\text{-XX}, \ 46\textbf{L80}, \ 57\textbf{R65}, \ 57\textbf{R67}] \end{array}$
- ${\bf 18F30}\,$  Grothendieck groups (category-theoretic aspects) [See also 13D15, 16E20, 19Axx]
- **18F40** Synthetic differential geometry, tangent categories, differential categories
- 18F50 Goodwillie calculus and functor calculus
- ${\bf 18F60}\,$  Categories of topological spaces and continuous mappings [See also 54-XX]
- 18F70 Frames and locales, pointfree topology, Stone duality [See also 06D22, 18B35]
- **18F75** Quantales [See also 06F07, 18B35]
- 18F99 None of the above, but in this section

- 18Gxx Homological algebra in category theory, derived categories and functors [See also 13Dxx, 16Exx, 20Jxx, 55Nxx, 55Uxx, 57Txx]
- **18G05** Projectives and injectives (category-theoretic aspects) [See also 13C10, 13C11, 16D40, 16D50]
- **18G10** Resolutions; derived functors (category-theoretic aspects) [See also 13D02, 16E05, 18Gxx]
- **18G15** Ext and Tor, generalizations, Künneth formula (category-theoretic aspects) [See also 55U25]
- 18G20 Homological dimension (category-theoretic aspects) [See also 13D05, 16E10]
- **18G25** Relative homological algebra, projective classes (category-theoretic aspects)
- 18G31 Simplicial modules and Dold-Kan correspondence
- **18G35** Chain complexes (category-theoretic aspects), dg categories [See also 14F07, 18G80, 55U15]
- 18G40 Spectral sequences, hypercohomology [See also 55Txx]
- 18G45 2-groups, crossed modules, crossed complexes
- **18G50** Nonabelian homological algebra (category-theoretic aspects)
- 18G65 Stable module categories [See also 20C20]
- 18G70  $A_{\infty}$ -categories, relations with homological mirror symmetry [See also 14F07, 14J33, 53D37]
- 18G80 Derived categories, triangulated categories
- 18G85 Graph complexes and graph homology {For relations with deformation quantization, see 53D55}
- 18G90 Other (co)homology theories (category-theoretic aspects) [See also  $19D55,\,46L80,\,58J20,\,58J22]$
- 18G99 None of the above, but in this section

### 18Mxx Monoidal categories and operads

- 18M05 Monoidal categories, symmetric monoidal categories [See also 19D23]
- **18M10** Traced monoidal categories, compact closed categories, star-autonomous categories
- 18M15 Braided monoidal categories and ribbon categories {For applications to knot theory, see also  $57\mathrm{Kxx}$ ; for applications to quantum groups, see also  $16\mathrm{T}20$ ,  $17\mathrm{B}37$ ,  $81\mathrm{R}50$ }
- 18M20 Fusion categories, modular tensor categories, modular functors {For applications to topological quantum field theories, see also 57R56; for applications to conformal field theories, see also 81T40}
- **18M25** Tannakian categories {For applications to motives, see also 14C15, 19E15}
- 18M30 String diagrams and graphical calculi
- ${\bf 18M35} \ \ {\bf Categories} \ \ {\bf of} \ \ {\bf networks} \ \ {\bf and} \ \ {\bf processes}, \ {\bf compositional-ity}$

- 18M40 Dagger categories, categorical quantum mechanics [See also 81P68]
- 18M45 Categorical aspects of linear logic [See also 03B47]
- 18M50 Bimonoidal, skew-monoidal, duoidal categories
- 18M60 Operads (general)
- 18M65 Non-symmetric operads, multicategories, generalized multicategories
- 18M70 Algebraic operads, cooperads, and Koszul duality
- 18M75 Topological and simplicial operads [See also 18N60]
- 18M80 Species, Hopf monoids, operads in combinatorics
- 18M85 Polycategories/dioperads, properads, PROPs, cyclic operads, modular operads
- 18M90 Globular operads
- 18M99 None of the above, but in this section

## 18Nxx Higher categories and homotopical algebra

- 18N10 2-categories, bicategories, double categories
- 18N15 2-dimensional monad theory [See also 18C15]
- 18 N20 Tricategories, weak n-categories, coherence, semi-strictification
- 18N25 Categorification
- 18N30 Strict omega-categories, computads, polygraphs
- 18N40 Homotopical algebra, Quillen model categories, derivators [See also 55U35]
- **18N45** Categories of fibrations, relations to K-theory, relations to type theory
- 18N50 Simplicial sets, simplicial objects [See also 55U10]
- 18N55 Localizations (e.g., simplicial localization, Bousfield localization) [See also 18E35, 55P60]
- 18N60 ( $\infty$ ,1)-categories (quasi-categories, Segal spaces, etc.);  $\infty$ -topoi, stable  $\infty$ -categories [See also 55U35, 55U40]
- **18N65**  $(\infty, n)$ -categories and  $(\infty, \infty)$ -categories
- 18N70 ∞-operads and higher algebra [See also 18M75]
- 18N99 None of the above, but in this section

## 19-XX *K*-theory [See also 16E20, 18F25]

- 19-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to K-theory
- 19-01 Introductory exposition (textbooks, tutorial papers, etc.) pertaining to K-theory
- ${f 19\text{-}02}$  Research exposition (monographs, survey articles) pertaining to  $K\text{-}{\it theory}$
- 19-03 History of K-theory [Consider also classification numbers pertaining to Section 01]

- **19-04** Software, source code, etc. for problems pertaining to K-theory
- ${f 19\text{-}06}$  Proceedings, conferences, collections, etc. pertaining to  $K\text{-}{theory}$
- 19-08 Computational methods for problems pertaining to Ktheory
- **19-11** Research data for problems pertaining to K-theory

## 19Axx Grothendieck groups and $K_0$ [See also 13D15, 18F30]

- **19A13** Stability for projective modules [See also 13C10]
- 19A15 Efficient generation of modules
- 19A22 Frobenius induction, Burnside and representation rings
- **19A31**  $K_0$  of group rings and orders
- **19A49**  $K_0$  of other rings
- 19A99 None of the above, but in this section

### 19Bxx Whitehead groups and $K_1$

- 19B10 Stable range conditions
- 19B14 Stability for linear groups
- **19B28**  $K_1$  of group rings and orders [See also 57Q10]
- 19B37 Congruence subgroup problems [See also 20H05]
- 19B99 None of the above, but in this section

### 19Cxx Steinberg groups and $K_2$

- 19C09 Central extensions and Schur multipliers
- **19C20** Symbols, presentations and stability of  $K_2$
- **19C30**  $K_2$  and the Brauer group
- **19C40** Excision for  $K_2$
- 19C99 None of the above, but in this section

### 19Dxx Higher algebraic K-theory

- **19D06** *Q* and plus-constructions
- 19D10 Algebraic K-theory of spaces
- 19D23 Symmetric monoidal categories [See also 18M05]
- $\mathbf{19D25}$  Karoubi-Villamayor-Gersten K-theory
- **19D35** Negative K-theory, NK and Nil
- **19D45** Higher symbols, Milnor K-theory
- **19D50** Computations of higher K-theory of rings [See also 13D15, 16E20]
- **19D55** K-theory and homology; cyclic homology and cohomology [See also 18G90]
- 19D99 None of the above, but in this section

### 19Exx K-theory in geometry

- **19E08** K-theory of schemes [See also 14C35]
- **19E15** Algebraic cycles and motivic cohomology (*K*-theoretic aspects) [See also 14C25, 14C35, 14F42]
- **19E20** Relations of K-theory with cohomology theories [See also 14Fxx]
- 19E99 None of the above, but in this section

## 19Fxx K-theory in number theory [See also 11R70, 11S70]

- 19F05 Generalized class field theory (K-theoretic aspects) [See also 11G45]
- 19F15 Symbols and arithmetic (K-theoretic aspects) [See also 11R37]
- 19F27 Étale cohomology, higher regulators, zeta and L-functions (K-theoretic aspects) [See also 11G40, 11R42, 11S40, 14F20, 14G10]
- 19F99 None of the above, but in this section

### 19Gxx K-theory of forms [See also 11Exx]

- 19G05 Stability for quadratic modules
- 19G12 Witt groups of rings [See also 11E81]
- **19G24** L-theory of group rings [See also 11E81]
- **19G38** Hermitian K-theory, relations with K-theory of rings
- 19G99 None of the above, but in this section

### 19Jxx Obstructions from topology

- **19J05** Finiteness and other obstructions in  $K_0$
- 19J10 Whitehead (and related) torsion
- **19J25** Surgery obstructions (K-theoretic aspects) [See also 57R67]
- **19J35** Obstructions to group actions (*K*-theoretic aspects)
- 19J99 None of the above, but in this section

## 19Kxx K-theory and operator algebras [See mainly 46L80, and also 46M20]

- **19K14**  $K_0$  as an ordered group, traces
- **19K33** Ext and K-homology [See also 55N22]
- **19K35** Kasparov theory (KK-theory) [See also 58J22]
- **19K56** Index theory [See also 58J20, 58J22]
- 19K99 None of the above, but in this section

## 19Lxx Topological K-theory [See also 55N15, 55R50, 55S25]

19L10 Riemann-Roch theorems, Chern characters

**19L20** *J*-homomorphism, Adams operations [See also 55Q50]

**19L41** Connective K-theory, cobordism [See also 55N22]

**19L47** Equivariant K-theory [See also 55N91, 55P91, 55Q91, 55R91, 55S91]

**19L50** Twisted K-theory; differential K-theory

**19L64** Geometric applications of topological K-theory

19L99 None of the above, but in this section

## 19Mxx Miscellaneous applications of K-theory

19M05 Miscellaneous applications of K-theory

19M99 None of the above, but in this section

## 20-XX Group theory and generalizations

**20-00** General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to group theory

20-01 Introductory exposition (textbooks, tutorial papers, etc.) pertaining to group theory

20-02 Research exposition (monographs, survey articles) pertaining to group theory

**20-03** History of group theory [Consider also classification numbers pertaining to Section 01]

**20-04** Software, source code, etc. for problems pertaining to group theory

 ${\bf 20\text{-}06}$  Proceedings, conferences, collections, etc. pertaining to group theory

 ${f 20\text{-}08}$  Computational methods for problems pertaining to group theory

 ${f 20\text{-}11}$  Research data for problems pertaining to group theory

### 20Axx Foundations

 ${f 20A05}$  Axiomatics and elementary properties of groups

**20A10** Metamathematical considerations in group theory  $\{For word problems, see 20F10\}$ 

20A15 Applications of logic to group theory

20A99 None of the above, but in this section

### 20Bxx Permutation groups

 ${\bf 20B05}\,$  General theory for finite permutation groups

20B07 General theory for infinite permutation groups

 ${f 20B10}$  Characterization theorems for permutation groups

20B15 Primitive groups

20B20 Multiply transitive finite groups

20B22 Multiply transitive infinite groups

20B25 Finite automorphism groups of algebraic, geometric, or combinatorial structures [See also 05Bxx, 12F10, 20G40, 20H30, 51-XX]

20B27 Infinite automorphism groups [See also 12F10]

20B30 Symmetric groups

20B35 Subgroups of symmetric groups

20B99 None of the above, but in this section

## 20Cxx Representation theory of groups {For representation rings and Burnside rings, see also 19A22}

20C05 Group rings of finite groups and their modules (group-theoretic aspects) [See also 16S34]

20C07 Group rings of infinite groups and their modules (group-theoretic aspects) [See also 16S34]

20C08 Hecke algebras and their representations

20C10 Integral representations of finite groups

20C11 p-adic representations of finite groups

20C12 Integral representations of infinite groups

 ${f 20C15}$  Ordinary representations and characters

20C20 Modular representations and characters

 ${f 20C25}$  Projective representations and multipliers

 ${f 20C30}$  Representations of finite symmetric groups

**20C32** Representations of infinite symmetric groups

 ${f 20C33}$  Representations of finite groups of Lie type

20C34 Representations of sporadic groups

20C35 Applications of group representations to physics and other areas of science

20C99 None of the above, but in this section

### 20Dxx Abstract finite groups

20D05 Finite simple groups and their classification

20D06 Simple groups: alternating groups and groups of Lie type [See also 20 Gxx]

20D08 Simple groups: sporadic groups

**20D10** Finite solvable groups, theory of formations, Schunck classes, Fitting classes,  $\pi$ -length, ranks [See also 20F17]

**20D15** Finite nilpotent groups, *p*-groups

**20D20** Sylow subgroups, Sylow properties,  $\pi$ -groups,  $\pi$ -structure

 ${\bf 20D25} \;\; {\bf Special \; subgroups \; (Frattini, \; Fitting, \; etc.)}$ 

 ${\bf 20D30}\,$  Series and lattices of subgroups

20D35 Subnormal subgroups of abstract finite groups

20D40 Products of subgroups of abstract finite groups

20D45 Automorphisms of abstract finite groups

20D60 Arithmetic and combinatorial problems involving abstract finite groups

20D99 None of the above, but in this section

### 20Exx Structure and classification of infi- 20F29 Representations of groups as automorphism groups of nite or finite groups

20E05 Free nonabelian groups

20E06 Free products of groups, free products with amalgamation, Higman-Neumann-Neumann extensions, and generalizations

20E07 Subgroup theorems; subgroup growth

**20E08** Groups acting on trees [See also 20F65]

20E10 Quasivarieties and varieties of groups

20E15 Chains and lattices of subgroups, subnormal subgroups [See also 20F22]

20E18 Limits, profinite groups

**20E22** Extensions, wreath products, and other compositions of groups [See also 20J05]

20E25 Local properties of groups

20E26 Residual properties and generalizations; residually finite groups

20E28 Maximal subgroups

**20E32** Simple groups [See also 20D05]

20E34 General structure theorems for groups

20E36 Automorphisms of infinite groups [For automorphisms of finite groups, see 20D45]

**20E42** Groups with a BN-pair; buildings [See also 51E24]

20E45 Conjugacy classes for groups

20E99 None of the above, but in this section

### 20Fxx Special aspects of infinite or finite groups

20F05 Generators, relations, and presentations of groups

20F06 Cancellation theory of groups; application of van Kampen diagrams [See also 57M05]

20F10 Word problems, other decision problems, connections with logic and automata (group-theoretic aspects) [See also 03B25, 03D05, 03D40, 06B25, 08A50, 20M05, 68Q70

**20F11** Groups of finite Morley rank [See also 03C45, 03C60]

20F12 Commutator calculus

20F14 Derived series, central series, and generalizations for groups

20F16 Solvable groups, supersolvable groups [See also 20D10

20F17 Formations of groups, Fitting classes [See also 20D10]

20F18 Nilpotent groups [See also 20D15]

20F19 Generalizations of solvable and nilpotent groups

20F22 Other classes of groups defined by subgroup chains

20F24 FC-groups and their generalizations

20F28 Automorphism groups of groups [See also 20E36]

algebraic systems

20F34 Fundamental groups and their automorphisms (group-theoretic aspects) [See also 57M05, 57Sxx]

20F36 Braid groups; Artin groups

20F38 Other groups related to topology or analysis

20F40 Associated Lie structures for groups

20F45 Engel conditions

20F50 Periodic groups; locally finite groups

20F55 Reflection and Coxeter groups (group-theoretic aspects) [See also 22E40, 51F15]

20F60 Ordered groups (group-theoretic aspects) [See mainly 06F15

20F65 Geometric group theory [See also 05C25, 20E08, 57Mxx

20F67 Hyperbolic groups and nonpositively curved groups

20F69 Asymptotic properties of groups

20F70 Algebraic geometry over groups; equations over

20F99 None of the above, but in this section

20Gxx Linear algebraic groups and related topics {For arithmetic theory, see 11E57, 11H56; for geometric theory, see 14Lxx, 22Exx; for other methods in representation theory, see 15A30, 22E45, 22E46, 22E47, 22E50, 22E55}

20G05 Representation theory for linear algebraic groups

20G07 Structure theory for linear algebraic groups

20G10 Cohomology theory for linear algebraic groups

20G15 Linear algebraic groups over arbitrary fields

20G20 Linear algebraic groups over the reals, the complexes, the quaternions

20G25 Linear algebraic groups over local fields and their in-

20G30 Linear algebraic groups over global fields and their

20G35 Linear algebraic groups over adèles and other rings and schemes

20G40 Linear algebraic groups over finite fields

20G41 Exceptional groups

20G42 Quantum groups (quantized function algebras) and their representations [See also 16T20, 17B37, 81R50]

20G43 Schur and q-Schur algebras

20G44 Kac-Moody groups

20G45 Applications of linear algebraic groups to the sciences

20G99 None of the above, but in this section

## 20Hxx Other groups of matrices [See also 15A30]

**20H05** Unimodular groups, congruence subgroups (grouptheoretic aspects) [See also 11F06, 19B37, 22E40, 51F20]

20H10 Fuchsian groups and their generalizations (group-theoretic aspects) [See also 11F06, 22E40, 30F35, 32Nxx]

**20H15** Other geometric groups, including crystallographic groups [See also 51-XX, especially 51F15, and 82D25]

20H20 Other matrix groups over fields

20H25 Other matrix groups over rings

20H30 Other matrix groups over finite fields

20H99 None of the above, but in this section

## 20Jxx Connections of group theory with homological algebra and category theory

20J05 Homological methods in group theory

20J06 Cohomology of groups

20J15 Category of groups

20J99 None of the above, but in this section

### 20Kxx Abelian groups

**20K01** Finite abelian groups {For sumsets, see 11B13, 11P70}

20K10 Torsion groups, primary groups and generalized primary groups

20K15 Torsion-free groups, finite rank

20K20 Torsion-free groups, infinite rank

20K21 Mixed groups

20K25 Direct sums, direct products, etc. for abelian groups

20K27 Subgroups of abelian groups

**20K30** Automorphisms, homomorphisms, endomorphisms, etc. for abelian groups

20K35 Extensions of abelian groups

20K40 Homological and categorical methods for abelian groups

20K45 Topological methods for abelian groups [See also 22A05, 22B05]

20K99 None of the above, but in this section

# 20Lxx Groupoids (i.e. small categories in which all morphisms are isomorphisms) {For sets with a single binary operation, see 20N02; for topological groupoids, see 22A22, 58H05}

20L05 Groupoids (i.e. small categories in which all morphisms are isomorphisms) {For sets with a single binary operation, see 20N02; for topological groupoids, see 22A22, 58H05}

20L99 None of the above, but in this section

### 20Mxx Semigroups

20M05 Free semigroups, generators and relations, word problems [See also  $03D40,\ 08A50,\ 20F10$ ]

20M07 Varieties and pseudovarieties of semigroups

20M10 General structure theory for semigroups

20M11 Radical theory for semigroups

20M12 Ideal theory for semigroups

20M13 Arithmetic theory of semigroups

20M14 Commutative semigroups

20M15 Mappings of semigroups

20M17 Regular semigroups

20M18 Inverse semigroups

20M19 Orthodox semigroups

**20M20** Semigroups of transformations, relations, partitions, etc. [See also 47D03, 47H20, 54H15]

20M25 Semigroup rings, multiplicative semigroups of rings [See also 16S36, 16Y60]

20M30 Representation of semigroups; actions of semigroups on sets

20M32 Algebraic monoids

20M35 Semigroups in automata theory, linguistics, etc. [See also 03D05, 68Q70, 68T50]

20M50 Connections of semigroups with homological algebra and category theory

20M75 Generalizations of semigroups

20M99 None of the above, but in this section

### 20Nxx Other generalizations of groups

20N02 Sets with a single binary operation (groupoids) {For groupoids in connection with category theory, see 20L05; for topological groupoids, see 22A22, 58H05}

20N05 Loops, quasigroups [See also 05Bxx]

20N10 Ternary systems (heaps, semiheaps, heapoids, etc.)

**20N15** *n*-ary systems  $(n \ge 3)$ 

20N20 Hypergroups

20N25 Fuzzy groups [See also 03E72]

20N99 None of the above, but in this section

## 20Pxx Probabilistic methods in group theory [See also 60Bxx]

**20P05** Probabilistic methods in group theory [See also 60Bxx]

20P99 None of the above, but in this section

### 22-XX Topological groups, Lie 22Cxx Compact groups groups {For transformation groups, see 54H15, 57Sxx, 58-XX; for abstract harmonic analysis, see 43-XX

- 22-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to topological groups
- 22-01 Introductory exposition (textbooks, tutorial papers, etc.) pertaining to topological groups
- 22-02 Research exposition (monographs, survey articles) pertaining to topological groups
- 22-03 History of topological groups [Consider also classification numbers pertaining to Section 01
- 22-04 Software, source code, etc. for problems pertaining to topological groups
- 22-06 Proceedings, conferences, collections, etc. pertaining to topological groups
- 22-08 Computational methods for problems pertaining to topological groups
- 22-11 Research data for problems pertaining to topological groups

### 22Axx Topological and differentiable algebraic systems {For topological rings and fields, see 12Jxx, 13Jxx, 16W80}

- 22A05 Structure of general topological groups
- 22A10 Analysis on general topological groups
- 22A15 Structure of topological semigroups
- 22A20 Analysis on topological semigroups
- 22A22 Topological groupoids (including differentiable and Lie groupoids) [See also 58H05]
- 22A25 Representations of general topological groups and semigroups
- 22A26 Topological semilattices, lattices and applications [See also 06B30, 06B35, 06F30]
- 22A30 Other topological algebraic systems and their representations
- 22A99 None of the above, but in this section

### 22Bxx Locally compact abelian groups (LCA groups)

- 22B05 General properties and structure of LCA groups
- 22B10 Structure of group algebras of LCA groups
- 22B99 None of the above, but in this section

22C05 Compact groups

22C99 None of the above, but in this section

### 22Dxx Locally compact groups and their algebras

- 22D05 General properties and structure of locally compact
- 22D10 Unitary representations of locally compact groups
- 22D12 Other representations of locally compact groups
- 22D15 Group algebras of locally compact groups
- 22D20 Representations of group algebras
- **22D25**  $C^*$ -algebras and  $W^*$ -algebras in relation to group representations [See also 46Lxx]
- 22D30 Induced representations for locally compact groups
- 22D35 Duality theorems for locally compact groups
- 22D40 Ergodic theory on groups [See also 28Dxx]
- 22D45 Automorphism groups of locally compact groups
- 22D50 Rigidity in locally compact groups
- **22D55** Kazhdan's property (T), the Haagerup property, and generalizations
- 22D99 None of the above, but in this section

### 22Exx Lie groups {For the topology of Lie groups and homogeneous spaces, see 57Sxx, 57Txx; for analysis thereon, see 43A80, 43A85, 43A90}

- **22E05** Local Lie groups [See also 34-XX, 35-XX, 58H05]
- 22E10 General properties and structure of complex Lie groups [See also 32M05]
- 22E15 General properties and structure of real Lie groups
- 22E20 General properties and structure of other Lie groups
- 22E25 Nilpotent and solvable Lie groups
- 22E27 Representations of nilpotent and solvable Lie groups (special orbital integrals, non-type I representations, etc.)
- 22E30 Analysis on real and complex Lie groups [See also 33C80, 43-XX
- **22E35** Analysis on *p*-adic Lie groups
- 22E40 Discrete subgroups of Lie groups [See also 20Hxx, 32Nxx
- 22E41 Continuous cohomologyof Lie groups [See also 57R32, 57Txx, 58H10
- 22E43 Structure and representation of the Lorentz group
- 22E45 Representations of Lie and linear algebraic groups over real fields: analytic methods (For the purely algebraic theory, see 20G05}
- 22E46 Semisimple Lie groups and their representations
- 22E47 Representations of Lie and real algebraic groups: algebraic methods (Verma modules, etc.) [See also 17B10]

- 22E50 Representations of Lie and linear algebraic groups over local fields [See also 20G05]
- 22E55 Representations of Lie and linear algebraic groups over global fields and adèle rings [See also 20G05]
- 22E57 Geometric Langlands program: representationtheoretic aspects [See also 14D24]
- **22E60** Lie algebras of Lie groups {For the algebraic theory of Lie algebras, see 17Bxx}
- 22E65 Infinite-dimensional Lie groups and their Lie algebras: general properties [See also 17B65, 58B25, 58D05 58H05]
- 22E66 Analysis on and representations of infinitedimensional Lie groups
- 22E67 Loop groups and related constructions, grouptheoretic treatment [See also 58D05]
- **22E70** Applications of Lie groups to the sciences; explicit representations [See also 81R05, 81R10]
- 22E99 None of the above, but in this section

### 22Fxx Noncompact transformation groups

- 22F05 General theory of group and pseudogroup actions  $\{\text{For topological properties of spaces with an action, see }57S20\}$
- **22F10** Measurable group actions [See also 22D40, 28Dxx, 37Axx]
- 22F30 Homogeneous spaces {For general actions on manifolds or preserving geometrical structures, see 57M60, 57Sxx; for discrete subgroups of Lie groups, see especially 22E40}
- **22F50** Groups as automorphisms of other structures
- 22F99 None of the above, but in this section

## 26-XX Real functions [See also 54C30]

- **26-00** General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to real functions
- **26-01** Introductory exposition (textbooks, tutorial papers, etc.) pertaining to real functions
- ${f 26\text{-}02}$  Research exposition (monographs, survey articles) pertaining to real functions
- ${f 26\text{-}03}$  History of real functions [Consider also classification numbers pertaining to Section  ${f 01}$ ]
- **26-04** Software, source code, etc. for problems pertaining to real functions
- **26-06** Proceedings, conferences, collections, etc. pertaining to real functions
- 26-08 Computational methods for problems pertaining to real functions
- **26-11** Research data for problems pertaining to real functions

### 26Axx Functions of one variable

- 26A03 Foundations: limits and generalizations, elementary topology of the line
- 26A06 One-variable calculus
- 26A09 Elementary functions
- 26A12 Rate of growth of functions, orders of infinity, slowly varying functions [See also 26A48]
- 26A15 Continuity and related questions (modulus of continuity, semicontinuity, discontinuities, etc.) for real functions in one variable {For properties determined by Fourier coefficients, see 42A16; for those determined by approximation properties, see 41A25, 41A27}
- 26A16 Lipschitz (Hölder) classes
- **26A18** Iteration of real functions in one variable [See also 37Bxx, 37Cxx, 37Exx, 39B12, 47H10, 54H25]
- **26A21** Classification of real functions; Baire classification of sets and functions [See also 03E15, 28A05, 54C50, 54H05]
- 26A24 Differentiation (real functions of one variable): general theory, generalized derivatives, mean value theorems [See also 28A15]
- **26A27** Nondifferentiability (nondifferentiable functions, points of nondifferentiability), discontinuous derivatives
- 26A30 Singular functions, Cantor functions, functions with other special properties
- **26A33** Fractional derivatives and integrals
- 26A36 Antidifferentiation
- 26A39 Denjoy and Perron integrals, other special integrals
- ${\bf 26A42}\,$  Integrals of Riemann, Stieltjes and Lebesgue type [See also 28-XX]
- 26A45 Functions of bounded variation, generalizations
- 26A46 Absolutely continuous real functions in one variable
- 26A48 Monotonic functions, generalizations
- ${f 26A51}$  Convexity of real functions in one variable, generalizations
- 26A99 None of the above, but in this section

### 26Bxx Functions of several variables

- ${f 26B05}$  Continuity and differentiation questions
- **26B10** Implicit function theorems, Jacobians, transformations with several variables
- 26B12 Calculus of vector functions
- **26B15** Integration of real functions of several variables: length, area, volume [See also 28A75, 51M25]
- **26B20** Integral formulas of real functions of several variables (Stokes, Gauss, Green, etc.)
- **26B25** Convexity of real functions of several variables, generalizations

- **26B30** Absolutely continuous real functions of several variables, functions of bounded variation
- ${f 26B35}$  Special properties of functions of several variables, Hölder conditions, etc.
- 26B40 Representation and superposition of functions
- 26B99 None of the above, but in this section

## 26Cxx Polynomials, rational functions in real analysis

- **26C05** Real polynomials: analytic properties, etc. [See also 12Dxx, 12Exx]
- 26C10 Real polynomials: location of zeros [See also 12D10, 30C15, 65H05]
- 26C15 Real rational functions [See also 14Pxx]
- 26C99 None of the above, but in this section

# 26Dxx Inequalities in real analysis {For maximal function inequalities, see 42B25; for functional inequalities, see 39B72; for probabilistic inequalities, see 60E15}

- 26D05 Inequalities for trigonometric functions and polynomials
- **26D07** Inequalities involving other types of functions
- 26D10 Inequalities involving derivatives and differential and integral operators
- 26D15 Inequalities for sums, series and integrals
- 26D20 Other analytical inequalities
- 26D99 None of the above, but in this section

## 26Exx Miscellaneous topics in real functions [See also 58Cxx]

- 26E05 Real-analytic functions [See also 32B05, 32C05]
- **26E10**  $C^{\infty}$ -functions, quasi-analytic functions [See also 58C25]
- **26E15** Calculus of functions on infinite-dimensional spaces [See also 46G05, 58Cxx]
- **26E20** Calculus of functions taking values in infinite-dimensional spaces [See also 46E40, 46G10, 58Cxx]
- **26E25** Set-valued functions [See also 28B20, 49J53, 54C60] {For nonsmooth analysis, see 49J52, 58Cxx, 90Cxx}
- **26E30** Non-Archimedean analysis [See also 12J25]
- **26E35** Nonstandard analysis [See also 03H05, 28E05, 54J05]
- 26E40 Constructive real analysis [See also 03F60]
- 26E50 Fuzzy real analysis [See also 03E72, 28E10]
- 26E60 Means [See also 47A64]
- 26E70 Real analysis on time scales or measure chains {For dynamic equations on time scales or measure chains, see 34N05}
- 26E99 None of the above, but in this section

# 28-XX Measure and integration $\{For analysis on manifolds, see 58-XX\}$

- 28-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to measure and integration
- 28-01 Introductory exposition (textbooks, tutorial papers, etc.) pertaining to measure and integration
- 28-02 Research exposition (monographs, survey articles) pertaining to measure and integration
- **28-03** History of measure and integration [Consider also classification numbers pertaining to Section 01]
- 28-04 Software, source code, etc. for problems pertaining to measure and integration
- ${f 28\text{-}06}$  Proceedings, conferences, collections, etc. pertaining to measure and integration
- ${f 28\text{-}08}$  Computational methods for problems pertaining to measure and integration
- ${f 28\text{-}11}$  Research data for problems pertaining to measure and integration

### 28Axx Classical measure theory

- **28A05** Classes of sets (Borel fields,  $\sigma$ -rings, etc.), measurable sets, Suslin sets, analytic sets [See also 03E15, 26A21, 54H05]
- 28A10 Real- or complex-valued set functions
- 28A12 Contents, measures, outer measures, capacities
- 28A15 Abstract differentiation theory, differentiation of set functions [See also 26A24]
- 28A20 Measurable and nonmeasurable functions, sequences of measurable functions, modes of convergence
- ${f 28A25}$  Integration with respect to measures and other set functions
- **28A33** Spaces of measures, convergence of measures [See also 46E27, 60Bxx]
- 28A35 Measures and integrals in product spaces
- 28A50 Integration and disintegration of measures
- **28A51** Lifting theory [See also 46G15]
- ${\bf 28A60}$  Measures on Boolean rings, measure algebras [See also  ${\bf 54H10}]$
- 28A75 Length, area, volume, other geometric measure theory [See also 26B15, 49Q15]
- 28A78 Hausdorff and packing measures
- 28A80 Fractals [See also 37Fxx]
- 28A99 None of the above, but in this section

### 28Bxx Set functions, measures and integrals with values in abstract spaces

- 28B05 Vector-valued set functions, measures and integrals [See also 46G10]
- ${f 28B10}$  Group- or semigroup-valued set functions, measures and integrals
- ${f 28B15}$  Set functions, measures and integrals with values in ordered spaces
- 28B20 Set-valued set functions and measures; integration of set-valued functions; measurable selections [See also 26E25, 54C60, 54C65, 91B14]
- 28B99 None of the above, but in this section

# 28Cxx Set functions and measures on spaces with additional structure [See also 46G12, 58C35, 58D20]

- 28C05 Integration theory via linear functionals (Radon measures, Daniell integrals, etc.), representing set functions and measures
- **28C10** Set functions and measures on topological groups or semigroups, Haar measures, invariant measures [See also 22Axx, 43A05]
- 28C15 Set functions and measures on topological spaces (regularity of measures, etc.)
- $\bf 28C20$  Set functions and measures and integrals in infinite-dimensional spaces (Wiener measure, Gaussian measure, etc.) [See also 46G12, 58C35, 58D20, 60B11]
- 28C99 None of the above, but in this section

# 28Dxx Measure-theoretic ergodic theory [See also 11K50, 11K55, 22D40, 37Axx, 47A35, 60Fxx, 60G10]

- $\bf 28D05$  Measure-preserving transformations {For measure-preserving transformations and dynamical systems, see  $\bf 37A05\}$
- **28D10** One-parameter continuous families of measure-preserving transformations {For dynamical systems aspect, see 37A10}
- **28D15** General groups of measure-preserving transformations {For dynamical systems aspects, see 37A15}
- 28D20 Entropy and other invariants
- 28D99 None of the above, but in this section

### 28Exx Miscellaneous topics in measure theory

- 28E05 Nonstandard measure theory [See also 03H05, 26E35]
- **28E10** Fuzzy measure theory [See also 03E72, 26E50, 94D05]
- 28E15 Other connections with logic and set theory
- 28E99 None of the above, but in this section

### 30-XX Functions of a complex variable

- **30-00** General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to functions of a complex variable
- **30-01** Introductory exposition (textbooks, tutorial papers, etc.) pertaining to functions of a complex variable
- **30-02** Research exposition (monographs, survey articles) pertaining to functions of a complex variable
- **30-03** History of functions of a complex variable [Consider also classification numbers pertaining to Section 01]
- **30-04** Software, source code, etc. for problems pertaining to functions of a complex variable
- **30-06** Proceedings, conferences, collections, etc. pertaining to functions of a complex variable
- 30-08 Computational methods for problems pertaining to functions of a complex variable [See also  $65\mathrm{Exx}]$
- ${f 30\text{--}11}$  Research data for problems pertaining to functions of a complex variable

### 30Axx General properties of functions of one complex variable

- **30A05** Monogenic and polygenic functions of one complex variable
- **30A10** Inequalities in the complex plane
- 30A99 None of the above, but in this section

### 30Bxx Series expansions of functions of one complex variable

- 30B10 Power series (including lacunary series) in one complex variable
- 30B20 Random power series in one complex variable
- **30B30** Boundary behavior of power series in one complex variable; over-convergence
- **30B40** Analytic continuation of functions of one complex variable
- **30B50** Dirichlet series, exponential series and other series in one complex variable [See also 11M41, 42-XX]
- ${f 30B60}$  Completeness problems, closure of a system of functions of one complex variable
- ${\bf 30B70}$  Continued fractions; complex-analytic aspects [See also 11A55, 40A15]
- 30B99 None of the above, but in this section

#### 30Cxx Geometric function theory

- **30C10** Polynomials and rational functions of one complex variable
- **30C15** Zeros of polynomials, rational functions, and other analytic functions of one complex variable (e.g., zeros of functions with bounded Dirichlet integral) {For algebraic theory, see 12D10; for real methods, see 26C10}
- 30C20 Conformal mappings of special domains
- 30C25 Covering theorems in conformal mapping theory
- **30C30** Schwarz-Christoffel-type mappings [See also 65E10]
- **30C35** General theory of conformal mappings
- **30C40** Kernel functions in one complex variable and applications
- **30C45** Special classes of univalent and multivalent functions of one complex variable (starlike, convex, bounded rotation, etc.)
- **30C50** Coefficient problems for univalent and multivalent functions of one complex variable
- **30C55** General theory of univalent and multivalent functions of one complex variable
- 30C62 Quasiconformal mappings in the complex plane
- **30C65** Quasiconformal mappings in  $\mathbb{R}^n$ , other generalizations
- **30C70** Extremal problems for conformal and quasiconformal mappings, variational methods
- **30C75** Extremal problems for conformal and quasiconformal mappings, other methods
- **30C80** Maximum principle, Schwarz's lemma, Lindelöf principle, analogues and generalizations; subordination
- 30C85 Capacity and harmonic measure in the complex plane [See also 31A15]
- 30C99 None of the above, but in this section

### 30Dxx Entire and meromorphic functions of one complex variable, and related topics

- 30D05 Functional equations in the complex plane, iteration and composition of analytic functions of one complex variable [See also 34Mxx, 37Fxx, 39-XX]
- **30D10** Representations of entire functions of one complex variable by series and integrals
- ${f 30D15}$  Special classes of entire functions of one complex variable and growth estimates
- **30D20** Entire functions of one complex variable, general theory
- ${f 30D30}$  Meromorphic functions of one complex variable, general theory
- **30D35** Value distribution of meromorphic functions of one complex variable, Nevanlinna theory
- 30D40 Cluster sets, prime ends, boundary behavior

- **30D45** Normal functions of one complex variable, normal families
- ${f 30D60}$  Quasi-analytic and other classes of functions of one complex variable
- 30D99 None of the above, but in this section

### 30Exx Miscellaneous topics of analysis in the complex plane

- 30E05 Moment problems and interpolation problems in the complex plane
- **30E10** Approximation in the complex plane
- **30E15** Asymptotic representations in the complex plane
- 30E20 Integration, integrals of Cauchy type, integral representations of analytic functions in the complex plane [See also  $45\mathrm{Exx}]$
- $\bf 30E25$  Boundary value problems in the complex plane [See also  $\bf 45Exx]$
- 30E99 None of the above, but in this section

#### 30Fxx Riemann surfaces

- **30F10** Compact Riemann surfaces and uniformization [See also 14H15, 32G15]
- 30F15 Harmonic functions on Riemann surfaces
- 30F20 Classification theory of Riemann surfaces
- 30F25 Ideal boundary theory for Riemann surfaces
- 30F30 Differentials on Riemann surfaces
- 30F35 Fuchsian groups and automorphic functions (aspects of compact Riemann surfaces and uniformization) [See also 11Fxx, 20H10, 22E40, 32Gxx, 32Nxx]
- **30F40** Kleinian groups (aspects of compact Riemann surfaces and uniformization) [See also 20H10]
- **30F45** Conformal metrics (hyperbolic, Poincaré, distance functions)
- 30F50 Klein surfaces
- **30F60** Teichmüller theory [See also 32G15]
- 30F99 None of the above, but in this section

#### 30Gxx Generalized function theory

- 30G06 Non-Archimedean function theory [See also 12J25]; nonstandard function theory [See also 03H05]
- 30G12 Finely holomorphic functions and topological function theory
- **30G20** Generalizations of Bers and Vekua type (pseudoanalytic, p-analytic, etc.)
- 30G25 Discrete analytic functions
- **30G30** Other generalizations of analytic functions (including abstract-valued functions)
- **30G35** Functions of hypercomplex variables and generalized variables
- 30G99 None of the above, but in this section

### 30Hxx Spaces and algebras of analytic 31-02 Research exposition (monographs, survey articles) perfunctions of one complex variable

- 30H05 Spaces of bounded analytic functions of one complex variable
- **30H10** Hardy spaces [See also 42B30, 46E30]
- 30H15 Nevanlinna spaces and Smirnov spaces
- **30H20** Bergman spaces and Fock spaces [See also 46E30, 46E35
- **30H25** Besov spaces and  $Q_p$ -spaces
- 30H30 Bloch spaces
- **30H35** BMO-spaces
- 30H40 Zygmund spaces
- 30H45 de Branges-Rovnyak spaces
- 30H50 Algebras of analytic functions of one complex variable
- 30H80 Corona theorems
- 30H99 None of the above, but in this section

#### 30Jxx Function theory on the disc

- **30J05** Inner functions of one complex variable
- **30J10** Blaschke products
- 30J15 Singular inner functions of one complex variable
- **30J99** None of the above, but in this section

#### 30Kxx Universal holomorphic functions of one complex variable

- 30K05 Universal Taylor series in one complex variable
- 30K10 Universal Dirichlet series in one complex variable
- 30K15 Universal functions of one complex variable
- **30K20** Compositional universality
- 30K99 None of the above, but in this section

#### 30Lxx Analysis on metric spaces

- 30L05 Geometric embeddings of metric spaces
- **30L10** Quasiconformal mappings in metric spaces
- 30L15 Inequalities in metric spaces
- 30L99 None of the above, but in this section

#### 31-XX Potential theory {For probabilistic potential theory, see 60J45}

- 31-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to potential theory
- 31-01 Introductory exposition (textbooks, tutorial papers, etc.) pertaining to potential theory

- taining to potential theory
- 31-03 History of potential theory [Consider also classification numbers pertaining to Section 01]
- **31-04** Software, source code, etc. for problems pertaining to potential theory
- **31-06** Proceedings, conferences, collections, etc. pertaining to potential theory
- 31-08 Computational methods for problems pertaining to potential theory [See also 65Exx]
- 31-11 Research data for problems pertaining to potential the-

#### 31Axx Two-dimensional potential theory

- 31A05 Harmonic, subharmonic, superharmonic functions in two dimensions
- 31A10 Integral representations, integral operators, integral equations methods in two dimensions
- **31A15** Potentials and capacity, harmonic measure, extremal length and related notions in two dimensions [See also 30C85
- **31A20** Boundary behavior (theorems of Fatou type, etc.) of harmonic functions in two dimensions
- 31A25 Boundary value and inverse problems for harmonic functions in two dimensions
- 31A30 Biharmonic, polyharmonic functions and equations, Poisson's equation in two dimensions
- 31A35 Connections of harmonic functions with differential equations in two dimensions
- 31A99 None of the above, but in this section

#### 31Bxx Higher-dimensional potential theory

- 31B05 Harmonic, subharmonic, superharmonic functions in higher dimensions
- 31B10 Integral representations, integral operators, integral equations methods in higher dimensions
- 31B15 Potentials and capacities, extremal length and related notions in higher dimensions
- **31B20** Boundary value and inverse problems for harmonic functions in higher dimensions
- 31B25 Boundary behavior of harmonic functions in higher dimensions
- 31B30 Biharmonic and polyharmonic equations and functions in higher dimensions
- 31B35 Connections of harmonic functions with differential equations in higher dimensions
- 31B99 None of the above, but in this section

#### 31Cxx Generalizations of potential theory

- 31C05 Harmonic, subharmonic, superharmonic functions on other spaces
- 31C10 Pluriharmonic and plurisubharmonic functions [See also 32U05]
- **31C12** Potential theory on Riemannian manifolds and other spaces [See also 53C20] {For Hodge theory, see 58A14}
- 31C15 Potentials and capacities on other spaces
- 31C20 Discrete potential theory
- 31C25 Dirichlet forms
- **31C35** Martin boundary theory [See also 60J50]
- ${f 31C40}$  Fine potential theory; fine properties of sets and functions
- ${f 31C45}$  Other generalizations (nonlinear potential theory, etc.)
- 31C99 None of the above, but in this section

#### 31Dxx Axiomatic potential theory

- 31D05 Axiomatic potential theory
- 31D99 None of the above, but in this section

### 31Exx Potential theory on fractals and metric spaces

- 31E05 Potential theory on fractals and metric spaces
- 31E99 None of the above, but in this section

# 32-XX Several complex variables and analytic spaces {For infinite-dimensional holomorphy, see also 46G20, 58B12}

- 32-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to several complex variables and analytic spaces
- **32-01** Introductory exposition (textbooks, tutorial papers, etc.) pertaining to several complex variables and analytic spaces
- **32-02** Research exposition (monographs, survey articles) pertaining to several complex variables and analytic spaces
- **32-03** History of several complex variables and analytic spaces [Consider also classification numbers pertaining to Section 01]
- **32-04** Software, source code, etc. for problems pertaining to several complex variables and analytic spaces
- **32-06** Proceedings, conferences, collections, etc. pertaining to several complex variables and analytic spaces
- 32-08 Computational methods for problems pertaining to several complex variables and analytic spaces [See also 65Exx]

**32-11** Research data for problems pertaining to several complex variables and analytic spaces

### 32Axx Holomorphic functions of several complex variables

- **32A05** Power series, series of functions of several complex variables
- ${\bf 32A08}\,$  Polynomials and rational functions of several complex variables
- 32A10 Holomorphic functions of several complex variables
- 32A12 Multifunctions of several complex variables
- 32A15 Entire functions of several complex variables
- **32A17** Special families of functions of several complex variables
- **32A18** Bloch functions, normal functions of several complex variables
- **32A19** Normal families of holomorphic functions, mappings of several complex variables, and related topics (taut manifolds etc.)
- 32A20 Meromorphic functions of several complex variables
- 32A22 Nevanlinna theory; growth estimates; other inequalities of several complex variables {For geometric theory, see 32H25, 32H30}
- 32A25 Integral representations; canonical kernels (Szegő, Bergman, etc.)
- **32A26** Integral representations, constructed kernels (e.g., Cauchy, Fantappiè-type kernels)
- 32A27 Residues for several complex variables [See also 32C30]
- **32A30** Other generalizations of function theory of one complex variable (should also be assigned at least one classification number from Section 30) {For functions of several hypercomplex variables, see 30G35}
- **32A35**  $H^p$ -spaces, Nevanlinna spaces of functions in several complex variables [See also 32M15, 42B30, 43A85, 46J15]
- **32A36** Bergman spaces of functions in several complex variables
- **32A37** Other spaces of holomorphic functions of several complex variables (e.g., bounded mean oscillation (BMOA), vanishing mean oscillation (VMOA)) [See also 46Exx]
- $\bf 32A38$  Algebras of holomorphic functions of several complex variables [See also 46J10, 46J15]
- **32A40** Boundary behavior of holomorphic functions of several complex variables
- **32A45** Hyperfunctions [See also 46F15]
- 32A50 Harmonic analysis of several complex variables [See mainly 43-XX]
- **32A55** Singular integrals of functions in several complex variables

- ${f 32A60}$  Zero sets of holomorphic functions of several complex variables
- 32A65~ Banach algebra techniques applied to functions of several complex variables [See also  $46\mathrm{Jxx}]$
- $32A70\,$  Functional analysis techniques applied to functions of several complex variables [See also  $46\mathrm{Exx}]$
- **32A99** None of the above, but in this section

### 32Bxx Local analytic geometry [See also 13-XX, 14-XX]

- ${f 32B05}$  Analytic algebras and generalizations, preparation theorems
- ${f 32B10}$  Germs of analytic sets, local parametrization
- 32B15 Analytic subsets of affine space
- 32B20 Semi-analytic sets, subanalytic sets, and generalizations [See also 14P15]
- **32B25** Triangulation and topological properties of semianalytic and subanalytic sets, and related questions
- 32B99 None of the above, but in this section

#### 32Cxx Analytic spaces

- 32C05 Real-analytic manifolds, real-analytic spaces [See also 14Pxx, 58A07]
- 32C07 Real-analytic sets, complex Nash functions [See also  $14P15,\ 14P20$ ]
- 32C09 Embedding of real-analytic manifolds
- $\bf 32C11$  Complex supergeometry [See also 14A22, 14M30, 58A50]
- 32C15 Complex spaces
- 32C18 Topology of analytic spaces
- 32C20 Normal analytic spaces
- 32C22 Embedding of analytic spaces
- 32C25 Analytic subsets and submanifolds
- 32C30 Integration on analytic sets and spaces, currents [See also 32A25, 32A27]
- **32C35** Analytic sheaves and cohomology groups [See also 14Fxx, 18F20, 55N30]
- ${f 32C36}$  Local cohomology of analytic spaces
- 32C37 Duality theorems for analytic spaces
- **32C38** Sheaves of differential operators and their modules, D-modules [See also 14F10, 16S32, 35A27, 58J15]
- 32C55 The Levi problem in complex spaces; generalizations
- 32C81 Applications of analytic spaces to physics and other areas of science
- 32C99 None of the above, but in this section

#### 32Dxx Analytic continuation

- **32D05** Domains of holomorphy
- **32D10** Envelopes of holomorphy
- **32D15** Continuation of analytic objects in several complex variables
- 32D20 Removable singularities in several complex variables
- 32D26 Riemann domains
- 32D99 None of the above, but in this section

#### 32Exx Holomorphic convexity

- ${f 32E05}$  Holomorphically convex complex spaces, reduction theory
- 32E10 Stein spaces, Stein manifolds
- **32E20** Polynomial convexity, rational convexity, meromorphic convexity in several complex variables
- **32E30** Holomorphic, polynomial and rational approximation, and interpolation in several complex variables; Runge pairs
- **32E35** Global boundary behavior of holomorphic functions of several complex variables
- 32E40 The Levi problem
- **32E99** None of the above, but in this section

### 32Fxx Geometric convexity in several complex variables

- **32F10** *q*-convexity, *q*-concavity
- **32F17** Other notions of convexity in relation to several complex variables
- 32F18 Finite-type conditions for the boundary of a domain
- 32F27 Topological consequences of geometric convexity
- **32F32** Analytical consequences of geometric convexity (vanishing theorems, etc.)
- ${f 32F45}$  Invariant metrics and pseudodistances in several complex variables
- 32F99 None of the above, but in this section

### 32Gxx Deformations of analytic structures

- $\bf 32G05$  Deformations of complex structures [See also 13D10,  $\bf 16S80,\, 58H10,\, 58H15]$
- ${\bf 32G07}\,$  Deformations of special (e.g., CR) structures
- 32G08 Deformations of fiber bundles
- **32G10** Deformations of submanifolds and subspaces
- **32G13** Complex-analytic moduli problems {For algebraic moduli problems, see 14D20, 14D22, 14H10, 14J10} [See also 14H15, 14J15]
- **32G15** Moduli of Riemann surfaces, Teichmüller theory (complex-analytic aspects in several variables) [See also 14H15, 30Fxx]

- **32G20** Period matrices, variation of Hodge structure; degenerations [See also 14D05, 14D07, 14K30]
- $\bf 32G34$  Moduli and deformations for ordinary differential equations (e.g., Knizhnik-Zamolodchikov equation) [See also  $\bf 34Mxx$ ]
- ${f 32G81}$  Applications of deformations of analytic structures to the sciences
- 32G99 None of the above, but in this section

### 32Hxx Holomorphic mappings and correspondences

- **32H02** Holomorphic mappings, (holomorphic) embeddings and related questions in several complex variables
- 32H04 Meromorphic mappings in several complex variables
- **32H12** Boundary uniqueness of mappings in several complex variables
- $\bf 32H25$  Picard-type theorems and generalizations for several complex variables {For function-theoretic properties, see  $\bf 32A22\}$
- 32H30 Value distribution theory in higher dimensions {For function-theoretic properties, see  $32A22\}$
- 32H35 Proper holomorphic mappings, finiteness theorems
- **32H40** Boundary regularity of mappings in several complex variables
- **32H50** Iteration of holomorphic maps, fixed points of holomorphic maps and related problems for several complex variables
- ${f 32H99}$  None of the above, but in this section

# 32Jxx Compact analytic spaces {For Riemann surfaces, see 14Hxx, 30Fxx; for algebraic theory, see 14Jxx}

- 32J05 Compactification of analytic spaces
- 32J10 Algebraic dependence theorems
- 32J15 Compact complex surfaces
- 32J17 Compact complex 3-folds
- **32J18** Compact complex n-folds
- 32J25 Transcendental methods of algebraic geometry (complex-analytic aspects) [See also 14C30]
- **32J27** Compact Kähler manifolds: generalizations, classification
- ${f 32J81}$  Applications of compact analytic spaces to the sciences
- 32J99 None of the above, but in this section

#### 32Kxx Generalizations of analytic spaces

- 32K05 Banach analytic manifolds and spaces [See also 46G20, 58Bxx]
- 32K07 Formal and graded complex spaces [See also 58C50]
- 32K12 Holomorphic maps with infinite-dimensional arguments or values [See also 46G20]
- 32K15 Differentiable functions on analytic spaces, differentiable spaces [See also 58C25]
- **32K99** None of the above, but in this section

### 32Lxx Holomorphic fiber spaces [See also 55Rxx]

- ${\bf 32L05}$  Holomorphic bundles and generalizations
- 32L10 Sheaves and cohomology of sections of holomorphic vector bundles, general results [See also 14F06, 14H60, 14J60, 18F20, 55N30]
- **32L15** Bundle convexity [See also 32F10]
- **32L20** Vanishing theorems
- 32L25 Twistor theory, double fibrations (complex-analytic aspects) [See also 53C28]
- **32L81** Applications of holomorphic fiber spaces to the sciences
- **32L99** None of the above, but in this section

### 32Mxx Complex spaces with a group of automorphisms

- **32M05** Complex Lie groups, group actions on complex spaces [See also 22E10]
- 32M10 Homogeneous complex manifolds [See also 14M17, 57T15]
- $32M12\,$  Almost homogeneous manifolds and spaces [See also 14M17]
- **32M15** Hermitian symmetric spaces, bounded symmetric domains, Jordan algebras (complex-analytic aspects) [See also 22E10, 22E40, 53C35, 57T15]
- **32M17** Automorphism groups of  $\mathbb{C}^n$  and affine manifolds
- 32M18 Automorphism groups of other complex spaces
- ${\bf 32M25}$  Complex vector fields, holomorphic foliations,  ${\mathbb C}\text{-}$  actions
- 32M99 None of the above, but in this section

### 32Nxx Automorphic functions [See also 11Fxx, 20H10, 22E40, 30F35]

- 32N05 General theory of automorphic functions of several complex variables
- 32N10 Automorphic forms in several complex variables
- 32N15 Automorphic functions in symmetric domains
- 32N99 None of the above, but in this section

32Pxx Non-Archimedean analysis (should also be assigned at least one other classification number from Section 32 describing the type of problem)

32P05 Non-Archimedean analysis (should also be assigned at least one other classification number from Section 32 describing the type of problem)

32P99 None of the above, but in this section

#### 32Qxx Complex manifolds

**32Q02** Special domains (Reinhardt, Hartogs, circular, tube, etc.) in  $\mathbb{C}^n$  and complex manifolds

32Q05 Negative curvature complex manifolds

32Q10 Positive curvature complex manifolds

32Q15 Kähler manifolds

32Q20 Kähler-Einstein manifolds [See also 53Cxx]

32Q25 Calabi-Yau theory (complex-analytic aspects) [See also 14J32]

32Q26 Notions of stability for complex manifolds

32Q28 Stein manifolds

32Q30 Uniformization of complex manifolds

 ${\bf 32Q35}$  Complex manifolds as subdomains of Euclidean space

32Q40 Embedding theorems for complex manifolds

32Q45 Hyperbolic and Kobayashi hyperbolic manifolds

32Q55 Topological aspects of complex manifolds

32Q56 Oka principle and Oka manifolds

32Q57 Classification theorems for complex manifolds

32Q60 Almost complex manifolds

32Q65 Pseudoholomorphic curves

32Q99 None of the above, but in this section

### 32Sxx Complex singularities [See also 58Kxx]

32S05 Local complex singularities [See also 14J17]

32S10 Invariants of analytic local rings

32S15 Equisingularity (topological and analytic) [See also 14E15]

 $\bf 32S20$  Global theory of complex singularities; cohomological properties [See also  $\bf 14E15$ ]

32S22 Relations with arrangements of hyperplanes [See also 52C35]

32S25 Complex surface and hypersurface singularities [See also 14J17]

32S30 Deformations of complex singularities; vanishing cycles [See also 14B07]

32S35 Mixed Hodge theory of singular varieties (complex-analytic aspects) [See also  $14C30,\,14D07]$ 

**32S40** Monodromy; relations with differential equations and *D*-modules (complex-analytic aspects)

**32S45** Modifications; resolution of singularities (complex-analytic aspects) [See also 14E15]

**32S50** Topological aspects of complex singularities: Lefschetz theorems, topological classification, invariants

32S55 Milnor fibration; relations with knot theory [See also 57K10, 57K45]

32S60 Stratifications; constructible sheaves; intersection cohomology (complex-analytic aspects) [See also 58Kxx]

**32S65** Singularities of holomorphic vector fields and foliations

32S70 Other operations on complex singularities

**32S99** None of the above, but in this section

#### 32Txx Pseudoconvex domains

32T05 Domains of holomorphy

32T15 Strongly pseudoconvex domains

32T20 Worm domains

32T25 Finite-type domains

**32T27** Geometric and analytic invariants on weakly pseudoconvex boundaries

32T35 Exhaustion functions

32T40 Peak functions

32T99 None of the above, but in this section

#### 32Uxx Pluripotential theory

32U05 Plurisubharmonic functions and generalizations [See also 31C10]

32U10 Plurisubharmonic exhaustion functions

32U15 General pluripotential theory

32U20 Capacity theory and generalizations

32U25 Lelong numbers

32U30 Removable sets in pluripotential theory

 ${f 32U35}$  Plurisubharmonic extremal functions, pluricomplex Green functions

32U40 Currents

32U99 None of the above, but in this section

#### 32Vxx CR manifolds

 ${f 32V05}$  CR structures, CR operators, and generalizations

32V10 CR functions

32V15 CR manifolds as boundaries of domains

32V20 Analysis on CR manifolds

32V25 Extension of functions and other analytic objects from CR manifolds

32V30 Embeddings of CR manifolds

32V35 Finite-type conditions on CR manifolds

32V40 Real submanifolds in complex manifolds

32V99 None of the above, but in this section

#### 32Wxx Differential operators in several 33Cxx Hypergeometric functions variables

- **32W05**  $\overline{\partial}$  and  $\overline{\partial}$ -Neumann operators
- **32W10**  $\overline{\partial}_b$  and  $\overline{\partial}_b$ -Neumann operators
- 32W20 Complex Monge-Ampère operators
- ${f 32W25}$  Pseudodifferential operators in several complex variables
- 32W30 Heat kernels in several complex variables
- 32W50 Other partial differential equations of complex analysis in several variables
- 32W99 None of the above, but in this section

### 33-XX Special functions (33-XX deals with the properties of functions as functions) {For orthogonal functions, see 42Cxx; for aspects of combinatorics, see 05Axx; for number-theoretic aspects, see 11-XX; for representation theory, see **22Exx**}

- 33-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to special functions
- **33-01** Introductory exposition (textbooks, tutorial papers, etc.) pertaining to special functions
- **33-02** Research exposition (monographs, survey articles) pertaining to special functions
- 33-03 History of special functions [Consider also classification numbers pertaining to Section 01]
- 33-04 Software, source code, etc. for problems pertaining to special functions
- **33-06** Proceedings, conferences, collections, etc. pertaining to special functions
- 33-11 Research data for problems pertaining to special functions

#### 33Bxx Elementary classical functions

- 33B10 Exponential and trigonometric functions
- 33B15 Gamma, beta and polygamma functions
- 33B20 Incomplete beta and gamma functions (error functions, probability integral, Fresnel integrals)
- 33B30 Higher logarithm functions
- 33B99 None of the above, but in this section

- **33C05** Classical hypergeometric functions,  ${}_{2}F_{1}$
- **33C10** Bessel and Airy functions, cylinder functions,  ${}_{0}F_{1}$
- 33C15 Confluent hypergeometric functions, Whittaker functions,  $_1F_1$
- **33C20** Generalized hypergeometric series,  $_pF_q$
- 33C45 Orthogonal polynomials and functions of hypergeometric type (Jacobi, Laguerre, Hermite, Askey scheme, etc.) {For general orthogonal polynomials and functions, see also 42C05}
- 33C47 Other special orthogonal polynomials and functions
- **33C50** Orthogonal polynomials and functions in several variables expressible in terms of special functions in one variable
- 33C52 Orthogonal polynomials and functions associated with root systems
- 33C55 Spherical harmonics
- 33C60 Hypergeometric integrals and functions defined by them (E, G, H and I functions)
- 33C65 Appell, Horn and Lauricella functions
- **33C67** Hypergeometric functions associated with root sys-
- 33C70 Other hypergeometric functions and integrals in several variables
- **33C75** Elliptic integrals as hypergeometric functions
- 33C80 Connections of hypergeometric functions with groups and algebras, and related topics
- **33C90** Applications of hypergeometric functions
- 33C99 None of the above, but in this section

#### 33Dxx Basic hypergeometric functions

- **33D05** q-gamma functions, q-beta functions and integrals
- **33D15** Basic hypergeometric functions in one variable,  $_r\phi_s$
- 33D45 Basic orthogonal polynomials and functions (Askey-Wilson polynomials, etc.)
- **33D50** Orthogonal polynomials and functions in several variables expressible in terms of basic hypergeometric functions in one variable
- 33D52 Basic orthogonal polynomials and functions associated with root systems (Macdonald polynomials, etc.)
- **33D60** Basic hypergeometric integrals and functions defined by them
- ${\bf 33D65}$  Bibasic functions and multiple bases
- **33D67** Basic hypergeometric functions associated with root
- 33D70 Other basic hypergeometric functions and integrals in several variables
- 33D80 Connections of basic hypergeometric functions with quantum groups, Chevalley groups, p-adic groups, Hecke algebras, and related topics
- **33D90** Applications of basic hypergeometric functions
- 33D99 None of the above, but in this section

#### 33Exx Other special functions

- 33E05 Elliptic functions and integrals
- 33E10 Lamé, Mathieu, and spheroidal wave functions
- 33E12 Mittag-Leffler functions and generalizations
- 33E15 Other wave functions
- 33E17 Painlevé-type functions
- 33E20 Other functions defined by series and integrals
- **33E30** Other functions coming from differential, difference and integral equations
- **33E50** Special functions in characteristic p (gamma functions, etc.)
- 33E99 None of the above, but in this section

### 33Fxx Computational aspects of special functions {For software etc., see 33-04}

- 33F05 Numerical approximation and evaluation of special functions [See also 65D20]
- **33F10** Symbolic computation of special functions (Gosper and Zeilberger algorithms, etc.) [See also 68W30]
- 33F99 None of the above, but in this section

### 34-XX Ordinary differential equations

- **34-00** General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to ordinary differential equations
- **34-01** Introductory exposition (textbooks, tutorial papers, etc.) pertaining to ordinary differential equations
- **34-02** Research exposition (monographs, survey articles) pertaining to ordinary differential equations
- 34-03 History of ordinary differential equations [Consider also classification numbers pertaining to Section 01]
- **34-04** Software, source code, etc. for problems pertaining to ordinary differential equations
- **34-06** Proceedings, conferences, collections, etc. pertaining to ordinary differential equations
- ${f 34\text{-}11}$  Research data for problems pertaining to ordinary differential equations

### 34Axx General theory for ordinary differential equations

- ${f 34A05}$  Explicit solutions, first integrals of ordinary differential equations
- $\bf 34A06$  Generalized ordinary differential equations (measure-differential equations, set-valued differential equations, etc.)
- ${\bf 34A07}$  Fuzzy ordinary differential equations

- **34A08** Fractional ordinary differential equations and fractional differential inclusions
- **34A09** Implicit ordinary differential equations, differential algebraic equations
- **34A12** Initial value problems, existence, uniqueness, continuous dependence and continuation of solutions to ordinary differential equations
- **34A25** Analytical theory of ordinary differential equations: series, transformations, transforms, operational calculus, etc. [See also 44-XX]
- 34A26 Geometric methods in ordinary differential equations
- **34A30** Linear ordinary differential equations and systems, general
- 34A33 Ordinary lattice differential equations
- **34A34** Nonlinear ordinary differential equations and systems, general theory
- 34A35 Ordinary differential equations of infinite order
- 34A36 Discontinuous ordinary differential equations
- 34A37 Ordinary differential equations with impulses
- 34A38 Hybrid systems of ordinary differential equations
- ${\bf 34A40} \ \, {\rm Differential\ inequalities\ involving\ functions\ of\ a\ single} \\ {\rm real\ variable\ [See\ also\ 26D20]}$
- 34A45 Theoretical approximation of solutions to ordinary differential equations {For numerical analysis, see 65Lxx}
- ${f 34A55}$  Inverse problems involving ordinary differential equations
- **34A60** Ordinary differential inclusions [See also 49J21, 49K21]
- ${\bf 34A99}$  None of the above, but in this section

# 34Bxx Boundary value problems for ordinary differential equations {For ordinary differential operators, see 34Lxx}

- ${f 34B05}$  Linear boundary value problems for ordinary differential equations
- **34B07** Linear boundary value problems for ordinary differential equations with nonlinear dependence on the spectral parameter
- **34B08** Parameter dependent boundary value problems for ordinary differential equations
- 34B09 Boundary eigenvalue problems for ordinary differential equations
- ${f 34B10}$  Nonlocal and multipoint boundary value problems for ordinary differential equations
- ${f 34B15}$  Nonlinear boundary value problems for ordinary differential equations
- **34B16** Singular nonlinear boundary value problems for ordinary differential equations
- **34B18** Positive solutions to nonlinear boundary value problems for ordinary differential equations

- **34B20** Weyl theory and its generalizations for ordinary differential equations
- **34B24** Sturm-Liouville theory [See also 34Lxx]
- 34B27 Green's functions for ordinary differential equations
- **34B30** Special ordinary differential equations (Mathieu, Hill, Bessel, etc.)
- **34B37** Boundary value problems with impulses for ordinary differential equations
- **34B40** Boundary value problems on infinite intervals for ordinary differential equations
- **34B45** Boundary value problems on graphs and networks for ordinary differential equations
- **34B60** Applications of boundary value problems involving ordinary differential equations
- 34B99 None of the above, but in this section

### 34Cxx Qualitative theory for ordinary differential equations [See also 37-XX]

- 34C05 Topological structure of integral curves, singular points, limit cycles of ordinary differential equations
- 34C07 Theory of limit cycles of polynomial and analytic vector fields (existence, uniqueness, bounds, Hilbert's 16th problem and ramifications) for ordinary differential equations
- **34C08** Ordinary differential equations and connections with real algebraic geometry (fewnomials, desingularization, zeros of abelian integrals, etc.)
- **34C10** Oscillation theory, zeros, disconjugacy and comparison theory for ordinary differential equations
- ${f 34C11}$  Growth and boundedness of solutions to ordinary differential equations
- ${f 34C12}$  Monotone systems involving ordinary differential equations
- 34C14 Symmetries, invariants of ordinary differential equations
- **34C15** Nonlinear oscillations and coupled oscillators for ordinary differential equations
- ${\bf 34C20}\,$  Transformation and reduction of ordinary differential equations and systems, normal forms
- 34C23 Bifurcation theory for ordinary differential equations [See also 37Gxx]
- **34C25** Periodic solutions to ordinary differential equations
- **34C26** Relaxation oscillations for ordinary differential equations
- **34C27** Almost and pseudo-almost periodic solutions to ordinary differential equations
- **34C28** Complex behavior and chaotic systems of ordinary differential equations [See also 37Dxx]
- ${f 34C29}$  Averaging method for ordinary differential equations

- **34C37** Homoclinic and heteroclinic solutions to ordinary differential equations
- 34C40 Ordinary differential equations and systems on manifolds
- **34C41** Equivalence and asymptotic equivalence of ordinary differential equations
- ${f 34C45}$  Invariant manifolds for ordinary differential equations
- **34C46** Multifrequency systems of ordinary differential equations
- **34C55** Hysteresis for ordinary differential equations
- **34C60** Qualitative investigation and simulation of ordinary differential equation models
- 34C99 None of the above, but in this section

### 34Dxx Stability theory for ordinary differential equations [See also 37C75, 93Dxx]

- **34D05** Asymptotic properties of solutions to ordinary differential equations
- **34D06** Synchronization of solutions to ordinary differential equations
- **34D08** Characteristic and Lyapunov exponents of ordinary differential equations
- **34D09** Dichotomy, trichotomy of solutions to ordinary differential equations
- **34D10** Perturbations of ordinary differential equations
- ${f 34D15}$  Singular perturbations of ordinary differential equations
- **34D20** Stability of solutions to ordinary differential equations
- **34D23** Global stability of solutions to ordinary differential equations
- 34D30 Structural stability and analogous concepts of solutions to ordinary differential equations [See also 37C20]
- ${f 34D35}$  Stability of manifolds of solutions to ordinary differential equations
- **34D45** Attractors of solutions to ordinary differential equations [See also 37C70, 37D45]
- 34D99 None of the above, but in this section

### 34Exx Asymptotic theory for ordinary differential equations

- ${f 34E05}$  Asymptotic expansions of solutions to ordinary differential equations
- **34E10** Perturbations, asymptotics of solutions to ordinary differential equations
- ${f 34E13}$  Multiple scale methods for ordinary differential equations
- **34E15** Singular perturbations, general theory for ordinary differential equations

- 34E17 Canard solutions to ordinary differential equations
- **34E18** Methods of nonstandard analysis for ordinary differential equations
- **34E20** Singular perturbations, turning point theory, WKB methods for ordinary differential equations
- 34E99 None of the above, but in this section

## 34Fxx Ordinary differential equations and systems with randomness [See also 34K50, 60H10, 93E03]

- **34F05** Ordinary differential equations and systems with randomness [See also 34K50, 60H10, 93E03]
- **34F10** Bifurcation of solutions to ordinary differential equations involving randomness
- **34F15** Resonance phenomena for ordinary differential equations involving randomness
- **34F99** None of the above, but in this section

# 34Gxx Differential equations in abstract spaces [See also 34Lxx, 37Kxx, 47Dxx, 47Hxx, 47Jxx, 58D25]

- 34G10 Linear differential equations in abstract spaces [See also 47D06, 47D09]
- **34G20** Nonlinear differential equations in abstract spaces [See also 47Hxx, 47Jxx]
- 34G25 Evolution inclusions
- 34G99 None of the above, but in this section

# 34Hxx Control problems including ordinary differential equations [See also 49J15, 49K15, 93C15]

- **34H05** Control problems involving ordinary differential equations [See also 49J15, 49K15, 93C15]
- ${f 34H10}$  Chaos control for problems involving ordinary differential equations
- ${f 34H15}$  Stabilization of solutions to ordinary differential equations
- 34H20 Bifurcation control of ordinary differential equations
- 34H99 None of the above, but in this section

# 34Kxx Functional-differential equations (including equations with delayed, advanced or state-dependent argument)

- 34K04 Symmetries, invariants of functional-differential equations [See also 37C80]
- ${f 34K05}$  General theory of functional-differential equations
- 34K06 Linear functional-differential equations

- **34K07** Theoretical approximation of solutions to functionaldifferential equations
- 34K08 Spectral theory of functional-differential operators
- 34K09 Functional-differential inclusions
- 34K10 Boundary value problems for functional-differential equations
- 34K11 Oscillation theory of functional-differential equations
- **34K12** Growth, boundedness, comparison of solutions to functional-differential equations [See also 37C35]
- 34K13 Periodic solutions to functional-differential equations [See also 37C27]
- **34K14** Almost and pseudo-almost periodic solutions to functional-differential equations
- **34K16** Heteroclinic and homoclinic orbits of functionaldifferential equations [See also 37C29]
- **34K17** Transformation and reduction of functionaldifferential equations and systems, normal forms
- 34K18 Bifurcation theory of functional-differential equations [See also 37Gxx]
- 34K19 Invariant manifolds of functional-differential equations
- 34K20 Stability theory of functional-differential equations [See also 37C75]
- 34K21 Stationary solutions of functional-differential equations
- 34K23 Complex (chaotic) behavior of solutions to functionaldifferential equations [See also 37D45]
- 34K24 Synchronization of functional-differential equations
- 34K25 Asymptotic theory of functional-differential equations
- ${f 34K26}$  Singular perturbations of functional-differential equations
- **34K27** Perturbations of functional-differential equations
- 34K29 Inverse problems for functional-differential equations
- 34K30 Functional-differential equations in abstract spaces [See also 34Gxx, 35R09, 35R10, 47Jxx]
- 34K31 Lattice functional-differential equations
- 34K32 Implicit functional-differential equations
- 34K33 Averaging for functional-differential equations
- 34K34 Hybrid systems of functional-differential equations
- **34K35** Control problems for functional-differential equations [See also 49J21, 49K21, 93C23]
- ${\bf 34K36} \ \ {\bf Fuzzy \ functional-differential \ equations}$
- 34K37 Functional-differential equations with fractional derivatives
- 34K38 Functional-differential inequalities
- 34K39 Discontinuous functional-differential equations
- 34K40 Neutral functional-differential equations
- ${f 34K41}$  Functional-differential equations in the complex domain

- 34K42 Functional-differential equations on time scales or measure chains
- **34K43** Functional-differential equations with statedependent arguments
- ${f 34K45}$  Functional-differential equations with impulses
- 34K50 Stochastic functional-differential equations [See also 34Fxx, 60Hxx]
- **34K60** Qualitative investigation and simulation of models involving functional-differential equations
- 34K99 None of the above, but in this section

### 34Lxx Ordinary differential operators [See also 47E05]

- ${f 34L05}$  General spectral theory of ordinary differential operators
- **34L10** Eigenfunctions, eigenfunction expansions, completeness of eigenfunctions of ordinary differential operators
- **34L15** Eigenvalues, estimation of eigenvalues, upper and lower bounds of ordinary differential operators
- **34L16** Numerical approximation of eigenvalues and of other parts of the spectrum of ordinary differential operators
- 34L20 Asymptotic distribution of eigenvalues, asymptotic theory of eigenfunctions for ordinary differential operators
- **34L25** Scattering theory, inverse scattering involving ordinary differential operators
- **34L30** Nonlinear ordinary differential operators
- **34L40** Particular ordinary differential operators (Dirac, onedimensional Schrödinger, etc.)
- 34L99 None of the above, but in this section

### 34Mxx Ordinary differential equations in the complex domain [See also 30Dxx, 32G34]

- 34M03 Linear ordinary differential equations and systems in the complex domain
- 34M04 Nonlinear ordinary differential equations and systems in the complex domain
- **34M05** Entire and meromorphic solutions to ordinary differential equations in the complex domain
- **34M10** Oscillation, growth of solutions to ordinary differential equations in the complex domain
- **34M15** Algebraic aspects (differential-algebraic, hypertranscendence, group-theoretical) of ordinary differential equations in the complex domain
- 34M25 Formal solutions and transform techniques for ordinary differential equations in the complex domain
- **34M30** Asymptotics and summation methods for ordinary differential equations in the complex domain

- **34M35** Singularities, monodromy and local behavior of solutions to ordinary differential equations in the complex domain, normal forms
- **34M40** Stokes phenomena and connection problems (linear and nonlinear) for ordinary differential equations in the complex domain
- 34M45 Ordinary differential equations on complex manifolds
- **34M46** Spectral theory for ordinary differential operators in the complex domain
- **34M50** Inverse problems (Riemann-Hilbert, inverse differential Galois, etc.) for ordinary differential equations in the complex domain
- **34M55** Painlevé and other special ordinary differential equations in the complex domain; classification, hierarchies;
- **34M56** Isomonodromic deformations for ordinary differential equations in the complex domain
- 34M60 Singular perturbation problems for ordinary differential equations in the complex domain (complex WKB, turning points, steepest descent) [See also 34E20]
- 34M65 Topological structure of trajectories of ordinary differential equations in the complex domain
- 34M99 None of the above, but in this section

## 34Nxx Dynamic equations on time scales or measure chains {For real analysis on time scales, see 26E70}

- $34N05\,$  Dynamic equations on time scales or measure chains {For real analysis on time scales or measure chains, see  $26E70\}$
- 34N99 None of the above, but in this section

### 35-XX Partial differential equations

- 35-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to partial differential equations
- **35-01** Introductory exposition (textbooks, tutorial papers, etc.) pertaining to partial differential equations
- **35-02** Research exposition (monographs, survey articles) pertaining to partial differential equations
- 35-03 History of partial differential equations [Consider also classification numbers pertaining to Section 01]
- 35-04 Software, source code, etc. for problems pertaining to partial differential equations
- **35-06** Proceedings, conferences, collections, etc. pertaining to partial differential equations
- **35-11** Research data for problems pertaining to partial differential equations

### 35Axx General topics in partial differential equations

- **35A01** Existence problems for PDEs: global existence, local existence, non-existence
- **35A02** Uniqueness problems for PDEs: global uniqueness, local uniqueness, non-uniqueness
- 35A08 Fundamental solutions to PDEs
- 35A09 Classical solutions to PDEs
- 35A10 Cauchy-Kovalevskaya theorems
- 35A15 Variational methods applied to PDEs
- 35A16 Topological and monotonicity methods applied to PDEs
- **35A17** Parametrices in context of PDEs
- 35A18 Wave front sets in context of PDEs
- 35A20 Analyticity in context of PDEs
- 35A21 Singularity in context of PDEs
- ${f 35A22}$  Transform methods (e.g., integral transforms) applied to PDEs
- **35A23** Inequalities applied to PDEs involving derivatives, differential and integral operators, or integrals
- 35A24 Methods of ordinary differential equations applied to PDEs
- 35A25 Other special methods applied to PDEs
- 35A27 Microlocal methods and methods of sheaf theory and homological algebra applied to PDEs [See also 32C38, 58J15]
- **35A30** Geometric theory, characteristics, transformations in context of PDEs [See also 58J70, 58J72]
- **35A35** Theoretical approximation in context of PDEs {For numerical analysis, see 65Mxx, 65Nxx}
- 35A99 None of the above, but in this section

### 35Bxx Qualitative properties of solutions to partial differential equations

- ${f 35B05}$  Oscillation, zeros of solutions, mean value theorems, etc. in context of PDEs
- 35B06 Symmetries, invariants, etc. in context of PDEs
- 35B07 Axially symmetric solutions to PDEs
- **35B08** Entire solutions to PDEs
- **35B09** Positive solutions to PDEs
- 35B10 Periodic solutions to PDEs
- **35B15** Almost and pseudo-almost periodic solutions to PDEs
- **35B20** Perturbations in context of PDEs
- 35B25 Singular perturbations in context of PDEs
- 35B27 Homogenization in context of PDEs; PDEs in media with periodic structure [See also 74Q05, 74Q10, 76M50, 78M40, 80M40]

- 35B30 Dependence of solutions to PDEs on initial and/or boundary data and/or on parameters of PDEs [See also 37Cxx]
- **35B32** Bifurcations in context of PDEs [See also 34C23, 34F10, 34H20, 37F46, 37Gxx, 37H20, 35J20, 37L10, 37M20, 47J15, 58E05, 58E07, 58J55, 74G60, 74H60]
- 35B33 Critical exponents in context of PDEs
- **35B34** Resonance in context of PDEs [See also 34F15, 70J40, 70K28, 70K30, 81U24]
- **35B35** Stability in context of PDEs [See also 34Dxx, 37B25, 37C20, 37C75, 37F15, 37J25, 37K45, 37L15, 49K40, 58K25, 93Dxx]
- **35B36** Pattern formations in context of PDEs [See also 92C15]
- **35B38** Critical points of functionals in context of PDEs (e.g., energy functionals) [See also 57R70, 58K05, 58E05]
- 35B40 Asymptotic behavior of solutions to PDEs
- **35B41** Attractors [See also 34D45, 37B35, 37C70, 37D45, 37G35, 37L30, 37M22]
- **35B42** Inertial manifolds [See also 37L25]
- 35B44 Blow-up in context of PDEs
- 35B45 A priori estimates in context of PDEs
- **35B50** Maximum principles in context of PDEs
- 35B51 Comparison principles in context of PDEs
- ${f 35B53}$  Liouville theorems and Phragmén-Lindelöf theorems in context of PDEs
- **35B60** Continuation and prolongation of solutions to PDEs [See also 58A15, 58A17, 58Hxx]
- 35B65 Smoothness and regularity of solutions to PDEs
- 35B99 None of the above, but in this section

### 35Cxx Representations of solutions to partial differential equations

- ${\bf 35C05}\,$  Solutions to PDEs in closed form
- 35C06 Self-similar solutions to PDEs
- 35C07 Traveling wave solutions
- **35C08** Soliton solutions [See also 37K40]
- **35C09** Trigonometric solutions to PDEs
- **35C10** Series solutions to PDEs
- **35C11** Polynomial solutions to PDEs
- 35C15 Integral representations of solutions to PDEs
- 35C20 Asymptotic expansions of solutions to PDEs
- 35C99 None of the above, but in this section

### 35Dxx Generalized solutions to partial differential equations

- 35D30 Weak solutions to PDEs
- **35D35** Strong solutions to PDEs
- 35D40 Viscosity solutions to PDEs
- 35D99 None of the above, but in this section

### systems of partial differential equations with constant coefficients [See also 35N05]

- **35E05** Fundamental solutions to PDEs and systems of PDEs with constant coefficients
- **35E10** Convexity properties of solutions to PDEs and systems of PDEs with constant coefficients
- 35E15 Initial value problems for PDEs and systems of PDEs with constant coefficients
- 35E20 General theory of PDEs and systems of PDEs with constant coefficients
- 35E99 None of the above, but in this section

### 35Fxx General first-order partial differential equations and systems of first-order partial differential equations

- 35F05 Linear first-order PDEs
- **35F10** Initial value problems for linear first-order PDEs
- **35F15** Boundary value problems for linear first-order PDEs
- 35F16 Initial-boundary value problems for linear first-order **PDEs**
- 35F20 Nonlinear first-order PDEs
- **35F21** Hamilton-Jacobi equations {For calculus of variations and optimal control, see 49Lxx; for mechanics of particles and systems, see 70H20}
- **35F25** Initial value problems for nonlinear first-order PDEs
- 35F30 Boundary value problems for nonlinear first-order
- 35F31 Initial-boundary value problems for nonlinear firstorder PDEs
- 35F35 Systems of linear first-order PDEs
- 35F40 Initial value problems for systems of linear first-order **PDEs**
- 35F45 Boundary value problems for systems of linear firstorder PDEs
- 35F46 Initial-boundary value problems for systems of linear first-order PDEs
- 35F50 Systems of nonlinear first-order PDEs
- 35F55 Initial value problems for systems of nonlinear firstorder PDEs
- 35F60 Boundary value problems for systems of nonlinear first-order PDEs
- 35F61 Initial-boundary value problems for systems of nonlinear first-order PDEs
- 35F99 None of the above, but in this section

### 35Exx Partial differential equations and 35Gxx General higher-order partial differential equations and systems of higherorder partial differential equations

- **35G05** Linear higher-order PDEs
- **35G10** Initial value problems for linear higher-order PDEs
- 35G15 Boundary value problems for linear higher-order
- 35G16 Initial-boundary value problems for linear higherorder PDEs
- 35G20 Nonlinear higher-order PDEs
- 35G25 Initial value problems for nonlinear higher-order **PDEs**
- 35G30 Boundary value problems for nonlinear higher-order **PDEs**
- 35G31 Initial-boundary value problems for nonlinear higher-
- 35G35 Systems of linear higher-order PDEs
- 35G40 Initial value problems for systems of linear higherorder PDEs
- 35G45 Boundary value problems for systems of linear higherorder PDEs
- 35G46 Initial-boundary value problems for systems of linear higher-order PDEs
- **35G50** Systems of nonlinear higher-order PDEs
- 35G55 Initial value problems for systems of nonlinear higherorder PDEs
- 35G60 Boundary value problems for systems of nonlinear higher-order PDEs
- 35G61 Initial-boundary value problems for systems of nonlinear higher-order PDEs
- 35G99 None of the above, but in this section

#### 35Hxx Close-to-elliptic equations

- 35H10 Hypoelliptic equations
- 35H20 Subelliptic equations
- 35H30 Quasielliptic equations
- 35H99 None of the above, but in this section

### 35Jxx Elliptic equations and elliptic systems {For global analysis, analysis on manifolds, see 58J10, 58J20}

- 35J05 Laplace operator, Helmholtz equation (reduced wave equation), Poisson equation [See also 31Axx, 31Bxx]
- 35J08 Green's functions for elliptic equations
- 35J10 Schrödinger operator, Schrödinger equation {For ordinary differential equations, see 34L40; for operator theory, see 47D08; for quantum theory, see 81Q05; for statistical mechanics, see 82B44}

- 35J15 Second-order elliptic equations
- ${f 35J20}$  Variational methods for second-order elliptic equations
- ${f 35J25}$  Boundary value problems for second-order elliptic equations
- 35J30 Higher-order elliptic equations [See also 31A30, 31B30]
- **35J35** Variational methods for higher-order elliptic equations
- ${\bf 35J40}$  Boundary value problems for higher-order elliptic equations
- 35J46 First-order elliptic systems
- 35J47 Second-order elliptic systems
- 35J48 Higher-order elliptic systems
- 35J50 Variational methods for elliptic systems
- ${f 35J56}$  Boundary value problems for first-order elliptic systems
- 35J57 Boundary value problems for second-order elliptic systems
- 35J58 Boundary value problems for higher-order elliptic systems
- 35J60 Nonlinear elliptic equations
- 35J61 Semilinear elliptic equations
- 35J62 Quasilinear elliptic equations
- ${f 35J65}$  Nonlinear boundary value problems for linear elliptic equations
- **35J66** Nonlinear boundary value problems for nonlinear elliptic equations
- **35J67** Boundary values of solutions to elliptic equations and elliptic systems
- 35J70 Degenerate elliptic equations
- 35J75 Singular elliptic equations
- **35J86** Unilateral problems for linear elliptic equations and variational inequalities with linear elliptic operators [See also 35R35, 49J40]
- 35J87 Unilateral problems for nonlinear elliptic equations and variational inequalities with nonlinear elliptic operators [See also 35R35, 49J40]
- 35J88 Unilateral problems for elliptic systems and systems of variational inequalities with elliptic operators [See also  $35R35,\ 49J40]$
- **35J91** Semilinear elliptic equations with Laplacian, bi-Laplacian or poly-Laplacian
- ${f 35J92}$  Quasilinear elliptic equations with  $p ext{-Laplacian}$
- ${f 35J93}$  Quasilinear elliptic equations with mean curvature operator
- 35J94 Elliptic equations with infinity-Laplacian
- **35J96** Monge-Ampère equations {For complex Monge-Ampère operators, see 32W20; for parabolic Monge-Ampère equations, see 35K96}
- 35J99 None of the above, but in this section

# 35 Kxx Parabolic equations and parabolic systems {For global analysis, analysis on manifolds, see 58 J 35}

- 35K05 Heat equation
- 35K08 Heat kernel
- 35K10 Second-order parabolic equations
- 35K15 Initial value problems for second-order parabolic equations
- 35K20 Initial-boundary value problems for second-order parabolic equations
- 35K25 Higher-order parabolic equations
- 35K30 Initial value problems for higher-order parabolic equations
- 35K35 Initial-boundary value problems for higher-order parabolic equations
- 35K40 Second-order parabolic systems
- 35K41 Higher-order parabolic systems
- ${f 35K45}$  Initial value problems for second-order parabolic systems
- 35K46 Initial value problems for higher-order parabolic systems
- 35K51 Initial-boundary value problems for second-order parabolic systems
- **35K52** Initial-boundary value problems for higher-order parabolic systems
- 35K55 Nonlinear parabolic equations
- **35K57** Reaction-diffusion equations {For diffusion processes and reaction effects, see 47D07, 58J65, 60J60, 60J70, 74N25, 76R50, 76V05, 80A23, 82B24, 82C24, 92E20}
- 35K58 Semilinear parabolic equations
- 35K59 Quasilinear parabolic equations
- **35K60** Nonlinear initial, boundary and initial-boundary value problems for linear parabolic equations
- 35K61 Nonlinear initial, boundary and initial-boundary value problems for nonlinear parabolic equations
- 35K65 Degenerate parabolic equations
- 35K67 Singular parabolic equations
- ${f 35K70}$  Ultraparabolic equations, pseudoparabolic equations, etc.
- $\bf 35K85$  Unilateral problems for linear parabolic equations and variational inequalities with linear parabolic operators [See also  $\bf 35R35,\, 49J40]$
- $35K86\,$  Unilateral problems for nonlinear parabolic equations and variational inequalities with nonlinear parabolic operators [See also  $35R35,\,49J40]$
- 35K87 Unilateral problems for parabolic systems and systems of variational inequalities with parabolic operators [See also 35R35, 49J40]
- 35K90 Abstract parabolic equations

- **35K91** Semilinear parabolic equations with Laplacian, bi-Laplacian or poly-Laplacian
- 35K92 Quasilinear parabolic equations with p-Laplacian
- 35K93 Quasilinear parabolic equations with mean curvature operator
- 35K96 Parabolic Monge-Ampère equations
- 35K99 None of the above, but in this section

## 35Lxx Hyperbolic equations and hyperbolic systems {For global analysis, see 58J45}

- 35L02 First-order hyperbolic equations
- ${f 35L03}$  Initial value problems for first-order hyperbolic equations
- **35L04** Initial-boundary value problems for first-order hyperbolic equations
- 35L05 Wave equation
- 35L10 Second-order hyperbolic equations
- ${\bf 35L15}$  Initial value problems for second-order hyperbolic equations
- **35L20** Initial-boundary value problems for second-order hyperbolic equations
- 35L25 Higher-order hyperbolic equations
- 35L30 Initial value problems for higher-order hyperbolic equations
- **35L35** Initial-boundary value problems for higher-order hyperbolic equations
- 35L40 First-order hyperbolic systems
- 35L45 Initial value problems for first-order hyperbolic systems
- ${\bf 35L50}$  Initial-boundary value problems for first-order hyperbolic systems
- ${f 35L51}$  Second-order hyperbolic systems
- ${f 35L52}$  Initial value problems for second-order hyperbolic systems
- 35L53 Initial-boundary value problems for second-order hyperbolic systems
- 35L55 Higher-order hyperbolic systems
- ${f 35L56}$  Initial value problems for higher-order hyperbolic systems
- 35L57 Initial-boundary value problems for higher-order hyperbolic systems
- 35L60 First-order nonlinear hyperbolic equations
- ${f 35L65}$  Hyperbolic conservation laws
- **35L67** Shocks and singularities for hyperbolic equations [See also 58Kxx, 74J40, 76L05]
- 35L70 Second-order nonlinear hyperbolic equations
- ${f 35L71}$  Second-order semilinear hyperbolic equations

- 35L72 Second-order quasilinear hyperbolic equations
- 35L75 Higher-order nonlinear hyperbolic equations
- ${f 35L76}$  Higher-order semilinear hyperbolic equations
- 35L77 Higher-order quasilinear hyperbolic equations
- 35L80 Degenerate hyperbolic equations
- 35L81 Singular hyperbolic equations
- 35L82 Pseudohyperbolic equations
- **35L85** Unilateral problems for linear hyperbolic equations and variational inequalities with linear hyperbolic operators [See also 35R35, 49J40]
- 35L86 Unilateral problems for nonlinear hyperbolic equations and variational inequalities with nonlinear hyperbolic operators [See also 35R35, 49J40]
- 35L87 Unilateral problems for hyperbolic systems and systems of variational inequalities with hyperbolic operators [See also 35R35, 49J40]
- 35L90 Abstract hyperbolic equations
- 35L99 None of the above, but in this section

### 35Mxx Partial differential equations of mixed type and mixed-type systems of partial differential equations

- 35M10 PDEs of mixed type
- 35M11 Initial value problems for PDEs of mixed type
- 35M12 Boundary value problems for PDEs of mixed type
- **35M13** Initial-boundary value problems for PDEs of mixed type
- 35M30 Mixed-type systems of PDEs
- 35M31 Initial value problems for mixed-type systems of PDEs
- **35M32** Boundary value problems for mixed-type systems of PDEs
- 35M33 Initial-boundary value problems for mixed-type systems of PDEs
- 35M85 Unilateral problems for linear PDEs of mixed type and variational inequalities with partial differential operators of mixed type [See also 35R35, 49J40]
- 35M86 Unilateral problems for nonlinear PDEs of mixed type and variational inequalities with nonlinear partial differential operators of mixed type [See also 35R35, 49J40]
- ${\bf 35M87} \ \ {\bf Unilateral\ problems} \ \ {\bf for\ mixed-type\ systems} \ \ {\bf of\ PDEs} \\ {\bf and\ systems} \ \ {\bf of\ variational\ inequalities\ with\ partial\ differential\ operators\ of\ mixed\ type\ [See\ also\ 35R35,\ 49J40]$
- 35M99 None of the above, but in this section

- 35Nxx Overdetermined problems for partial differential equations and systems of partial differential equations {For global analysis, see 58Hxx, 58J10, 58J15}
- **35N05** Overdetermined systems of PDEs with constant coefficients
- **35N10** Overdetermined systems of PDEs with variable coefficients
- **35N15**  $\overline{\partial}$ -Neumann problems and formal complexes in context of PDEs [See also 32W05, 32W10, 58J10]
- 35N20 Overdetermined initial value problems for PDEs and systems of PDEs
- **35N25** Overdetermined boundary value problems for PDEs and systems of PDEs
- **35N30** Overdetermined initial-boundary value problems for PDEs and systems of PDEs
- 35N99 None of the above, but in this section

# 35Pxx Spectral theory and eigenvalue problems for partial differential equations $\{\text{For operator theory, see 47Axx, 47Bxx, 47F05}\}$

- **35P05** General topics in linear spectral theory for PDEs
- **35P10** Completeness of eigenfunctions and eigenfunction expansions in context of PDEs
- 35P15 Estimates of eigenvalues in context of PDEs
- **35P20** Asymptotic distributions of eigenvalues in context of PDEs
- **35P25** Scattering theory for PDEs [See also 47A40]
- 35P30 Nonlinear eigenvalue problems and nonlinear spectral theory for PDEs
- 35P99 None of the above, but in this section

# 35Qxx Partial differential equations of mathematical physics and other areas of application [See also 35J05, 35J10, 35K05, 35L05]

- 35Q05 Euler-Poisson-Darboux equations
- 35Q07 Fuchsian PDEs
- **35Q15** Riemann-Hilbert problems in context of PDEs [See also 30E25, 31A25, 31B20]
- $35\mathbf{Q20}$  Boltzmann equations {For fluid mechanics, see  $76\mathbf{P}05;$  for statistical mechanics, see  $82\mathbf{B}40,~82\mathbf{C}40,~82\mathbf{D}05\}$
- 35Q30 Navier-Stokes equations {For fluid mechanics, see  $76D05,\,76D07,\,76N10\}$
- **35Q31** Euler equations {For fluid mechanics, see 76D05, 76D07, 76N10}

- 35Q35 PDEs in connection with fluid mechanics
- $35Q40\,$  PDEs in connection with quantum mechanics
- **35Q41** Time-dependent Schrödinger equations and Dirac equations {For quantum theory, see 81Q05; for relativity and gravitational theory, see 83A05, 83C10}
- **35Q51** Soliton equations {For dynamical systems and ergodic theory, see 37K40}
- **35Q53** KdV equations (Korteweg-de Vries equations) {For dynamical systems and ergodic theory, see 37K10}
- **35Q55** NLS equations (nonlinear Schrödinger equations) {For dynamical systems and ergodic theory, see 37K10}
- **35Q56** Ginzburg-Landau equations {For optics and electromagnetic theory, see 78A25}
- **35Q60** PDEs in connection with optics and electromagnetic theory
- **35Q61** Maxwell equations {For optics and electromagnetic theory, see 78A25; for relativity and gravitational theory, see 83C22}
- 35Q62 PDEs in connection with statistics
- 35Q68 PDEs in connection with computer science
- **35Q70** PDEs in connection with mechanics of particles and systems of particles
- **35Q74** PDEs in connection with mechanics of deformable solids
- 35Q75 PDEs in connection with relativity and gravitational theory
- 35Q76 Einstein equations {For several complex variables and analytic spaces, see 32Q40; for differential geometry, see 53C07; for relativity and gravitational theory, see 83C05, 83C25, 83D05}
- **35Q79** PDEs in connection with classical thermodynamics and heat transfer
- 35Q80 Transport equations {For calculus of variations and optimal control, see 49Q20; for fluid mechanics, see 76F25; for statistical mechanics, see 82C70, 82D75; for operations research, see 90B06; for mathematical programming, see 90C08}
- $\bf 35Q81~$  PDEs in connection with semiconductor devices {For statistical mechanics, see 82D37}
- 35Q82 PDEs in connection with statistical mechanics
- $\bf 35Q83$  Vlasov equations {For statistical mechanics, see  $\bf 82C70,\,82D75\}$
- **35Q84** Fokker-Planck equations {For fluid mechanics, see 76X05, 76W05; for statistical mechanics, see 82C31}
- **35Q85** PDEs in connection with astronomy and astrophysics
- 35Q86 PDEs in connection with geophysics
- **35Q89** PDEs in connection with mean field game theory {For calculus of variations and optimal control, see 49N80; for game theory, see 91A16}
- 35Q90 PDEs in connection with mathematical programming

- **35Q91** PDEs in connection with game theory, economics, social and behavioral sciences
- 35Q92 PDEs in connection with biology, chemistry and other natural sciences
- 35Q93 PDEs in connection with control and optimization
- 35Q94 PDEs in connection with information and communication
- 35Q99 None of the above, but in this section
- 35Rxx Miscellaneous topics in partial differential equations {For equations on manifolds, see 32Wxx, 58Jxx; for manifolds of solutions, see 58Bxx; for stochastic PDEs, see 60H15}
- 35R01 PDEs on manifolds [See also 32Wxx, 53Cxx, 58Jxx]
- **35R02** PDEs on graphs and networks (ramified or polygonal spaces)
- **35R03** PDEs on Heisenberg groups, Lie groups, Carnot groups, etc.
- 35R05 PDEs with low regular coefficients and/or low regular data
- **35R06** PDEs with measure
- 35R07 PDEs on time scales
- 35R09 Integral partial differential equations [See also 45Kxx]
- 35R10 Functional partial differential equations
- 35R11 Fractional partial differential equations
- 35R12 Impulsive partial differential equations
- 35R13 Fuzzy partial differential equations
- 35R15 PDEs on infinite-dimensional (e.g., function) spaces (= PDEs in infinitely many variables) [See also 46Gxx, 58D25]
- 35R20 Operator partial differential equations (= PDEs on finite-dimensional spaces for abstract space valued functions) [See also  $34\mathrm{Gxx}$ ,  $47\mathrm{A}50$ ,  $47\mathrm{D}03$ ,  $47\mathrm{D}06$ ,  $47\mathrm{D}09$ ,  $47\mathrm{H}20$ ,  $47\mathrm{Jxx}$ ]
- 35R25 Ill-posed problems for PDEs
- 35R30 Inverse problems for PDEs
- **35R35** Free boundary problems for PDEs
- 35R37 Moving boundary problems for PDEs
- 35R45 Partial differential inequalities and systems of partial differential inequalities
- 35R50 PDEs of infinite order
- $\bf 35R60~PDEs$  with randomness, stochastic partial differential equations [See also  $\bf 60H15$ ]
- ${\bf 35R70}\,$  PDEs with multivalued right-hand sides
- 35R99 None of the above, but in this section

- 35 Sxx Pseudodifferential operators and other generalizations of partial differential operators {For operator theory, see 47 G30, 58J40}
- $\bf 35S05$  Pseudodifferential operators as generalizations of partial differential operators [See also 32W25, 47G30, 47L80, 58J40]
- **35S10** Initial value problems for PDEs with pseudodifferential operators
- 35S15 Boundary value problems for PDEs with pseudodifferential operators
- **35S16** Initial-boundary value problems for PDEs with pseudodifferential operators
- 35S30 Fourier integral operators applied to PDEs [See also 43A32, 58J40]
- **35S35** Topological aspects for pseudodifferential operators in context of PDEs: intersection cohomology, stratified sets, etc. [See also 32C38, 32S40, 32S60, 58J15]
- **35S50** Paradifferential operators as generalizations of partial differential operators in context of PDEs
- 35S99 None of the above, but in this section
- 37-XX Dynamical systems and ergodic theory [See also 26A18, 28Dxx, 34Cxx, 34Dxx, 35Bxx, 46Lxx, 58Jxx, 70-XX]
- **37-00** General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to dynamical systems and ergodic theory
- 37-01 Introductory exposition (textbooks, tutorial papers, etc.) pertaining to dynamical systems and ergodic theory
- $\bf 37\text{-}02$  Research exposition (monographs, survey articles) pertaining to dynamical systems and ergodic theory
- 37-03 History of dynamical systems and ergodic theory [Consider also classification numbers pertaining to Section 01]
- **37-04** Software, source code, etc. for problems pertaining to dynamical systems and ergodic theory
- **37-06** Proceedings, conferences, collections, etc. pertaining to dynamical systems and ergodic theory
- **37-11** Research data for problems pertaining to dynamical systems and ergodic theory

### 37Axx Ergodic theory [See also 28Dxx]

- ${f 37A05}$  Dynamical aspects of measure-preserving transformations
- **37A10** Dynamical systems involving one-parameter continuous families of measure-preserving transformations
- **37A15** General groups of measure-preserving transformations and dynamical systems [See mainly 22Fxx]
- 37A17 Homogeneous flows [See also 22Fxx]
- **37A20** Algebraic ergodic theory, cocycles, orbit equivalence, ergodic equivalence relations
- 37A25 Ergodicity, mixing, rates of mixing
- **37A30** Ergodic theorems, spectral theory, Markov operators {For operator ergodic theory, see mainly 47A35}
- **37A35** Entropy and other invariants, isomorphism, classification in ergodic theory
- 37A40 Nonsingular (and infinite-measure preserving) transformations
- 37A45 Relations between ergodic theory and number theory [See also 11Kxx]
- 37A46 Relations between ergodic theory and harmonic analysis
- 37A50 Dynamical systems and their relations with probability theory and stochastic processes [See also 60Fxx, 60G10]
- **37A55** Dynamical systems and the theory of  $C^*$ -algebras [See mainly 46L55]
- 37A60 Dynamical aspects of statistical mechanics [See also 82Cxx]
- 37A99 None of the above, but in this section

#### 37Bxx Topological dynamics

- 37B02 Dynamics in general topological spaces
- **37B05** Dynamical systems involving transformations and group actions with special properties (minimality, distality, proximality, expansivity, etc.)
- 37B10 Symbolic dynamics
- 37B15 Dynamical aspects of cellular automata {For computational aspects, see 68Q80}
- **37B20** Notions of recurrence and recurrent behavior in dynamical systems
- 37B25 Stability of topological dynamical systems
- 37B30 Index theory for dynamical systems, Morse-Conley indices
- 37B35 Gradient-like and recurrent behavior; isolated (locally maximal) invariant sets; attractors, repellers for topological dynamical systems
- 37B40 Topological entropy
- **37B45** Continua theory in dynamics
- 37B50 Multidimensional shifts of finite type

- 37B52 Tiling dynamics
- 37B55 Topological dynamics of nonautonomous systems
- **37B65** Approximate trajectories, pseudotrajectories, shadowing and related notions for topological dynamical systems
- 37B99 None of the above, but in this section

### 37Cxx Smooth dynamical systems: general theory [See also 34Cxx, 34Dxx]

- **37C05** Dynamical systems involving smooth mappings and diffeomorphisms
- **37C10** Dynamics induced by flows and semiflows
- 37C15 Topological and differentiable equivalence, conjugacy, moduli, classification of dynamical systems
- 37C20 Generic properties, structural stability of dynamical systems
- **37C25** Fixed points and periodic points of dynamical systems; fixed-point index theory, local dynamics
- 37C27 Periodic orbits of vector fields and flows
- 37C29 Homoclinic and heteroclinic orbits for dynamical systems
- **37C30** Functional analytic techniques in dynamical systems; zeta functions, (Ruelle-Frobenius) transfer operators, etc.
- **37C35** Orbit growth in dynamical systems
- 37C40 Smooth ergodic theory, invariant measures for smooth dynamical systems [See also 37Dxx]
- 37C45 Dimension theory of smooth dynamical systems
- **37C50** Approximate trajectories (pseudotrajectories, shadowing, etc.) in smooth dynamics
- 37C55 Periodic and quasi-periodic flows and diffeomorphisms
- 37C60 Nonautonomous smooth dynamical systems [See also 37B55]
- 37C65 Monotone flows as dynamical systems
- 37C70 Attractors and repellers of smooth dynamical systems and their topological structure
- 37C75 Stability theory for smooth dynamical systems
- 37C80 Symmetries and invariants of dynamical systems
- 37C81 Equivariant dynamical systems
- **37C83** Dynamical systems with singularities (billiards, etc.)
- **37C85** Dynamics induced by group actions other than  $\mathbb{Z}$  and  $\mathbb{R}$ , and  $\mathbb{C}$  [See mainly 22Fxx, and also 32M25, 57R30, 57Sxx]
- 37C86 Foliations generated by dynamical systems
- 37C99 None of the above, but in this section

#### 37Dxx Dynamical systems with hyperbolic 37F30 Quasiconformal methods in holomorphic dynamics; behavior

- 37D05 Dynamical systems with hyperbolic orbits and sets
- 37D10 Invariant manifold theory for dynamical systems
- 37D15 Morse-Smale systems
- 37D20 Uniformly hyperbolic systems (expanding, Anosov, Axiom A, etc.)
- 37D25 Nonuniformly hyperbolic systems (Lyapunov exponents, Pesin theory, etc.)
- 37D30 Partially hyperbolic systems and dominated splittings
- 37D35 Thermodynamic formalism, variational principles, equilibrium states for dynamical systems
- **37D40** Dynamical systems of geometric origin and hyperbolicity (geodesic and horocycle flows, etc.)
- 37D45 Strange attractors, chaotic dynamics of systems with hyperbolic behavior
- **37D99** None of the above, but in this section

#### 37Exx Low-dimensional dynamical systems

- 37E05 Dynamical systems involving maps of the interval (piecewise continuous, continuous, smooth)
- 37E10 Dynamical systems involving maps of the circle
- **37E15** Combinatorial dynamics (types of periodic orbits)
- 37E20 Universality and renormalization of dynamical systems [See also 37F25]
- 37E25 Dynamical systems involving maps of trees and graphs
- 37E30 Dynamical systems involving homeomorphisms and diffeomorphisms of planes and surfaces
- 37E35 Flows on surfaces
- 37E40 Dynamical aspects of twist maps
- **37E45** Rotation numbers and vectors
- 37E99 None of the above, but in this section

#### 37Fxx Dynamical systems over complex numbers [See also 30D05, 32H50]

- **37F05** Dynamical systems involving relations and correspondences in one complex variable
- 37F10 Dynamics of complex polynomials, rational maps, entire and meromorphic functions; Fatou and Julia sets [See also 32A10, 32A20, 32H02, 32H04]
- 37F12 Critical orbits for holomorphic dynamical systems
- 37F15 Expanding holomorphic maps; hyperbolicity; structural stability of holomorphic dynamical systems
- 37F20 Combinatorics and topology in relation with holomorphic dynamical systems
- 37F25 Renormalization of holomorphic dynamical systems

- quasiconformal dynamics
- 37F32 Fuchsian and Kleinian groups as dynamical systems
- 37F34 Teichmüller theory; moduli spaces of holomorphic dynamical systems
- 37F35 Conformal densities and Hausdorff dimension for holomorphic dynamical systems
- 37F40 Geometric limits in holomorphic dynamics
- 37F45 Holomorphic families of dynamical systems; holomorphic motions; semigroups of holomorphic maps
- 37F46 Bifurcations; parameter spaces in holomorphic dynamics; the Mandelbrot and Multibrot sets
- 37F50 Small divisors, rotation domains and linearization in holomorphic dynamics
- 37F75 Dynamical aspects of holomorphic foliations and vector fields [See also 32M25, 32S65, 34Mxx]
- 37F80 Higher-dimensional holomorphic and meromorphic dynamics
- **37F99** None of the above, but in this section

### 37Gxx Local and nonlocal bifurcation theory for dynamical systems [See also 34C23, 34K18

- 37G05 Normal forms for dynamical systems
- **37G10** Bifurcations of singular points in dynamical systems
- **37G15** Bifurcations of limit cycles and periodic orbits in dynamical systems
- 37G20 Hyperbolic singular points with homoclinic trajectories in dynamical systems
- 37G25 Bifurcations connected with nontransversal intersection in dynamical systems
- 37G30 Infinite nonwandering sets arising in bifurcations of dynamical systems
- 37G35 Dynamical aspects of attractors and their bifurca-
- 37G40 Dynamical aspects of symmetries, equivariant bifurcation theory
- 37G99 None of the above, but in this section

### 37Hxx Random dynamical systems [See also 15B52, 34D08, 34F05, 47B80, 70L05, 82C05, 93Exx

- 37H05 General theory of random and stochastic dynamical systems
- 37H10 Generation, random and stochastic difference and differential equations [See also 34F05, 34K50, 60H10, 60H15
- 37H12 Random iteration

- **37H15** Random dynamical systems aspects of multiplicative ergodic theory, Lyapunov exponents [See also 34D08, 37Axx, 37Cxx, 37Dxx]
- 37H20 Bifurcation theory for random and stochastic dynamical systems [See also 37Gxx]
- 37H30 Stability theory for random and stochastic dynamical systems
- 37H99 None of the above, but in this section

### 37Jxx Dynamical aspects of finitedimensional Hamiltonian and Lagrangian systems [See also 53Dxx, 70Fxx, 70Hxx]

- **37J05** General theory of finite-dimensional Hamiltonian and Lagrangian systems, Hamiltonian and Lagrangian structures, symmetries, invariants
- 37J10 Symplectic and canonical mappings
- **37J12** Fixed points and periodic points of finite-dimensional Hamiltonian and Lagrangian systems
- **37J20** Bifurcation problems for finite-dimensional Hamiltonian and Lagrangian systems
- 37J25 Stability problems for finite-dimensional Hamiltonian and Lagrangian systems
- **37J30** Obstructions to integrability for finite-dimensional Hamiltonian and Lagrangian systems (nonintegrability criteria)
- 37J35 Completely integrable finite-dimensional Hamiltonian systems, integration methods, integrability tests
- **37J37** Relations of finite-dimensional Hamiltonian and Lagrangian systems with Lie algebras and other algebraic structures
- **37J38** Relations of finite-dimensional Hamiltonian and Lagrangian systems with algebraic geometry, complex analysis, special functions
- **37J39** Relations of finite-dimensional Hamiltonian and Lagrangian systems with topology, geometry and differential geometry (symplectic geometry, Poisson geometry, etc.) [See also 53D20]
- **37J40** Perturbations of finite-dimensional Hamiltonian systems, normal forms, small divisors, KAM theory, Arnol'd diffusion
- **37J45** Periodic, homoclinic and heteroclinic orbits of finite-dimensional Hamiltonian systems
- **37J50** Action-minimizing orbits and measures for finitedimensional Hamiltonian and Lagrangian systems; variational principles; degree-theoretic methods
- **37J55** Contact systems [See also 53D10]
- **37J60** Nonholonomic dynamical systems [See also 70F25]
- **37J65** Nonautonomous Hamiltonian dynamical systems (Painlevé equations, etc.)
- 37J70 Completely integrable discrete dynamical systems
- 37J99 None of the above, but in this section

# 37Kxx Dynamical system aspects of infinite-dimensional Hamiltonian and Lagrangian systems [See also 35Axx, 35Qxx]

- 37K05 General theory of infinite-dimensional Hamiltonian and Lagrangian systems, Hamiltonian and Lagrangian structures, symmetries, conservation laws
- 37K10 Completely integrable infinite-dimensional Hamiltonian and Lagrangian systems, integration methods, integrability tests, integrable hierarchies (KdV, KP, Toda, etc.)
- 37K15 Inverse spectral and scattering methods for infinitedimensional Hamiltonian and Lagrangian systems
- 37K20 Relations of infinite-dimensional Hamiltonian and Lagrangian dynamical systems with algebraic geometry, complex analysis, and special functions [See also 14H70]
- 37K25 Relations of infinite-dimensional Hamiltonian and Lagrangian dynamical systems with topology, geometry and differential geometry
- 37K30 Relations of infinite-dimensional Hamiltonian and Lagrangian dynamical systems with infinite-dimensional Lie algebras and other algebraic structures
- **37K35** Lie-Bäcklund and other transformations for infinitedimensional Hamiltonian and Lagrangian systems
- 37K40 Soliton theory, asymptotic behavior of solutions of infinite-dimensional Hamiltonian systems
- 37K45 Stability problems for infinite-dimensional Hamiltonian and Lagrangian systems
- 37K50 Bifurcation problems for infinite-dimensional Hamiltonian and Lagrangian systems
- 37K55 Perturbations, KAM for infinite-dimensional Hamiltonian and Lagrangian systems
- 37K58 Variational principles and methods for infinitedimensional Hamiltonian and Lagrangian systems
- 37K60 Lattice dynamics; integrable lattice equations [See also 37L60]
- 37K99 None of the above, but in this section

### 37Lxx Infinite-dimensional dissipative dynamical systems [See also 35Bxx, 35Qxx]

- **37L05** General theory of infinite-dimensional dissipative dynamical systems, nonlinear semigroups, evolution equations
- 37L10 Normal forms, center manifold theory, bifurcation theory for infinite-dimensional dissipative dynamical systems
- 37L15 Stability problems for infinite-dimensional dissipative dynamical systems
- **37L20** Symmetries of infinite-dimensional dissipative dynamical systems
- 37L25 Inertial manifolds and other invariant attracting sets of infinite-dimensional dissipative dynamical systems

- **37L30** Infinite-dimensional dissipative dynamical systems–attractors and their dimensions, Lyapunov exponents
- **37L40** Invariant measures for infinite-dimensional dissipative dynamical systems
- 37L45 Hyperbolicity; Lyapunov functions for infinitedimensional dissipative dynamical systems
- **37L50** Noncompact semigroups; dispersive equations; perturbations of infinite-dimensional dissipative dynamical systems
- **37L55** Infinite-dimensional random dynamical systems; stochastic equations [See also 35R60, 60H10, 60H15]
- 37L60 Lattice dynamics and infinite-dimensional dissipative dynamical systems [See also 37K60]
- **37L65** Special approximation methods (nonlinear Galerkin, etc.) for infinite-dimensional dissipative dynamical systems
- 37L99 None of the above, but in this section

# 37Mxx Approximation methods and numerical treatment of dynamical systems {For numerical analysis, see also 65Pxx; for software etc., see 37-04}

- 37M05 Simulation of dynamical systems
- 37M10 Time series analysis of dynamical systems
- 37M15 Discretization methods and integrators (symplectic, variational, geometric, etc.) for dynamical systems
- 37M20 Computational methods for bifurcation problems in dynamical systems
- 37M21 Computational methods for invariant manifolds of dynamical systems
- 37M22 Computational methods for attractors of dynamical systems
- **37M25** Computational methods for ergodic theory (approximation of invariant measures, computation of Lyapunov exponents, entropy, etc.)
- 37M99 None of the above, but in this section

#### 37Nxx Applications of dynamical systems

- 37N05 Dynamical systems in classical and celestial mechanics [See mainly 70Fxx, 70Hxx, 70Kxx]
- $37N10\,$  Dynamical systems in fluid mechanics, oceanography and meteorology [See mainly 76-XX, especially 76D05,  $76F20,\,86A05,\,86A10]$
- 37N15 Dynamical systems in solid mechanics [See mainly 74Hxx]
- **37N20** Dynamical systems in other branches of physics (quantum mechanics, general relativity, laser physics)
- 37N25 Dynamical systems in biology [See also 92-XX]
- **37N30** Dynamical systems in numerical analysis [See also 65- XX]

- **37N35** Dynamical systems in control [See also 93-XX]
- **37N40** Dynamical systems in optimization and economics [See also 90-XX, 91-XX]
- 37N99 None of the above, but in this section

### 37Pxx Arithmetic and non-Archimedean dynamical systems [See also 11S82, 37A45]

- **37P05** Arithmetic and non-Archimedean dynamical systems involving polynomial and rational maps
- **37P10** Arithmetic and non-Archimedean dynamical systems involving analytic and meromorphic maps
- 37P15 Dynamical systems over global ground fields
- **37P20** Dynamical systems over non-Archimedean local ground fields
- 37P25 Dynamical systems over finite ground fields
- 37P30 Height functions; Green functions; invariant measures in arithmetic and non-Archimedean dynamical systems [See also 11G50, 14G40]
- 37P35 Arithmetic properties of periodic points
- 37P40 Non-Archimedean Fatou and Julia sets
- **37P45** Families and moduli spaces in arithmetic and non-Archimedean dynamical systems
- 37P50 Dynamical systems on Berkovich spaces
- 37P55 Arithmetic dynamics on general algebraic varieties
- **37P99** None of the above, but in this section

### 39-XX Difference and functional equations

- 39-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to difference and functional equations
- **39-01** Introductory exposition (textbooks, tutorial papers, etc.) pertaining to difference and functional equations
- **39-02** Research exposition (monographs, survey articles) pertaining to difference and functional equations
- 39-03 History of difference and functional equations [Consider also classification numbers pertaining to Section 01]
- **39-04** Software, source code, etc. for problems pertaining to difference and functional equations
- 39-06 Proceedings, conferences, collections, etc. pertaining to difference and functional equations
- ${f 39\text{-}08}$  Computational methods for problems pertaining to difference and functional equations
- ${f 39\text{-}11}$  Research data for problems pertaining to difference and functional equations

### 39Axx Difference equations {For dynamic 39B72 Systems of functional equations and inequalities equations on time scales, see 34N05; for dynamical systems, see 37-XX

39A05 General theory of difference equations

**39A06** Linear difference equations

**39A10** Additive difference equations

39A12 Discrete version of topics in analysis

**39A13** Difference equations, scaling (q-differences) [See also 33Dxx

**39A14** Partial difference equations

39A20 Multiplicative and other generalized difference equations, e.g., of Lyness type

39A21 Oscillation theory for difference equations

39A22 Growth, boundedness, comparison of solutions to difference equations

**39A23** Periodic solutions of difference equations

**39A24** Almost periodic solutions of difference equations

39A26 Fuzzy difference equations

**39A27** Boundary value problems for difference equations

39A28 Bifurcation theory for difference equations

39A30 Stability theory for difference equations

39A33 Chaotic behavior of solutions of difference equations

39A35 Integrable difference and lattice equations; integrabil-

39A45 Difference equations in the complex domain

39A50 Stochastic difference equations

39A60 Applications of difference equations

**39A70** Difference operators [See also 47B39]

39A99 None of the above, but in this section

#### 39Bxx Functional equations and inequalities [See also 30D05]

39B05 General theory of functional equations and inequali-

39B12 Iteration theory, iterative and composite equations [See also 26A18, 30D05, 37-XX]

39B22 Functional equations for real functions [See also 26A51, 26B25

**39B32** Functional equations for complex functions [See also 30D05

39B42 Matrix and operator functional equations [See also 47 Jxx

**39B52** Functional equations for functions with more general domains and/or ranges

39B55 Orthogonal additivity and other conditional functional equations

39B62 Functional inequalities, including subadditivity, convexity, etc. [See also 26A51, 26B25, 26Dxx]

39B82 Stability, separation, extension, and related topics for functional equations [See also 46A22]

39B99 None of the above, but in this section

### 40-XX Sequences, series, summability

40-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to sequences, series, summability

40-01 Introductory exposition (textbooks, tutorial papers, etc.) pertaining to sequences, series, summability

**40-02** Research exposition (monographs, survey articles) pertaining to sequences, series, summability

40-03 History of sequences, series, summability [Consider also classification numbers pertaining to Section 01]

40-04 Software, source code, etc. for problems pertaining to sequences, series, summability

40-06 Proceedings, conferences, collections, etc. pertaining to sequences, series, summability

40-08 Computational methods for problems pertaining to sequences, series, summability

40-11 Research data for problems pertaining to sequences, series, summability

#### 40Axx Convergence and divergence of infinite limiting processes

40A05 Convergence and divergence of series and sequences

40A10 Convergence and divergence of integrals

40A15 Convergence and divergence of continued fractions [See also 30B70]

40A20 Convergence and divergence of infinite products

40A25 Approximation to limiting values (summation of series, etc.) {For the Euler-Maclaurin summation formula, see 65B15}

40A30 Convergence and divergence of series and sequences of functions

**40A35** Ideal and statistical convergence [See also 40G15]

40A99 None of the above, but in this section

#### 40Bxx Multiple sequences and series

40B05 Multiple sequences and series (should also be assigned at least one other classification number in this section)

40B99 None of the above, but in this section

#### 40Cxx General summability methods

- 40C05 Matrix methods for summability
- 40C10 Integral methods for summability
- **40C15** Function-theoretic methods (including power series methods and semicontinuous methods) for summability
- 40C99 None of the above, but in this section

#### 40Dxx Direct theorems on summability

- 40D05 General theorems on summability
- 40D09 Structure of summability fields
- 40D10 Tauberian constants and oscillation limits in summability theory
- 40D15 Convergence factors and summability factors
- 40D20 Summability and bounded fields of methods
- 40D25 Inclusion and equivalence theorems in summability theory
- 40D99 None of the above, but in this section

#### 40Exx Inversion theorems

- 40E05 Tauberian theorems, general
- 40E10 Growth estimates
- 40E15 Lacunary inversion theorems
- 40E20 Tauberian constants
- 40E99 None of the above, but in this section

# 40Fxx Absolute and strong summability (should also be assigned at least one other classification number in Section 40)

- ${f 40F05}$  Absolute and strong summability (should also be assigned at least one other classification number in Section  ${f 40}$ )
- ${f 40F99}$  None of the above, but in this section

#### 40Gxx Special methods of summability

- ${f 40G05}$  Cesàro, Euler, Nörlund and Hausdorff methods
- 40G10 Abel, Borel and power series methods
- ${f 40G15}$  Summability methods using statistical convergence [See also  ${f 40A35}$ ]
- 40G99 None of the above, but in this section

### 40Hxx Functional analytic methods in summability

- 40H05 Functional analytic methods in summability
- 40H99 None of the above, but in this section

40Jxx Summability in abstract structures (should also be assigned at least one other classification number from Section 40) [See also 43A55, 46A35, 46B15]

**40J05** Summability in abstract structures (should also be assigned at least one other classification number from Section 40) [See also 43A55, 46A35, 46B15]

40J99 None of the above, but in this section

41-XX Approximations and expansions {For approximation theory in the complex domain, see 30E05, 30E10; for trigonometric approximation and interpolation, see 42A10, 42A15; for numerical approximation, see 65Dxx}

- 41-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to approximations and expansions
- **41-01** Introductory exposition (textbooks, tutorial papers, etc.) pertaining to approximations and expansions
- **41-02** Research exposition (monographs, survey articles) pertaining to approximations and expansions
- **41-03** History of approximations and expansions [Consider also classification numbers pertaining to Section 01]
- ${f 41\text{-}04}$  Software, source code, etc. for problems pertaining to approximations and expansions
- **41-06** Proceedings, conferences, collections, etc. pertaining to approximations and expansions
- **41-11** Research data for problems pertaining to approximations and expansions

41Axx Approximations and expansions {For approximation theory in the complex domain, see 30E05, 30E10; for trigonometric approximation and interpolation, see 42A10, 42A15; for numerical approximation, see 65Dxx}

- **41A05** Interpolation in approximation theory [See also 42A15, 65D05]
- **41A10** Approximation by polynomials {For approximation by trigonometric polynomials, see 42A10}
- 41A15 Spline approximation
- **41A17** Inequalities in approximation (Bernstein, Jackson, Nikol'skiĭ-type inequalities)
- 41A20 Approximation by rational functions

- 41A21 Padé approximation
- 41A25 Rate of convergence, degree of approximation
- 41A27 Inverse theorems in approximation theory
- 41A28 Simultaneous approximation
- 41A29 Approximation with constraints
- 41A30 Approximation by other special function classes
- **41A35** Approximation by operators (in particular, by integral operators)
- **41A36** Approximation by positive operators
- 41A40 Saturation in approximation theory
- 41A44 Best constants in approximation theory
- ${\bf 41A45}$  Approximation by arbitrary linear expressions
- **41A46** Approximation by arbitrary nonlinear expressions; widths and entropy
- 41A50 Best approximation, Chebyshev systems
- 41A52 Uniqueness of best approximation
- 41A55 Approximate quadratures
- 41A58 Series expansions (e.g., Taylor, Lidstone series, but not Fourier series)
- **41A60** Asymptotic approximations, asymptotic expansions (steepest descent, etc.) [See also 30E15]
- **41A63** Multidimensional problems (should also be assigned at least one other classification number from Section 41)
- **41A65** Abstract approximation theory (approximation in normed linear spaces and other abstract spaces)
- 41A80 Remainders in approximation formulas
- 41A81 Weighted approximation
- 41A99 None of the above, but in this section

### 42-XX Harmonic analysis on Euclidean spaces

- **42-00** General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to harmonic analysis on Euclidean spaces
- $\bf 42\text{-}01$  Introductory exposition (textbooks, tutorial papers, etc.) pertaining to harmonic analysis on Euclidean spaces
- **42-02** Research exposition (monographs, survey articles) pertaining to harmonic analysis on Euclidean spaces
- **42-03** History of harmonic analysis on Euclidean spaces [Consider also classification numbers pertaining to Section 01]
- **42-04** Software, source code, etc. for problems pertaining to harmonic analysis on Euclidean spaces
- **42-06** Proceedings, conferences, collections, etc. pertaining to harmonic analysis on Euclidean spaces
- **42-08** Computational methods for problems pertaining to harmonic analysis on Euclidean spaces
- **42-11** Research data for problems pertaining to harmonic analysis on Euclidean spaces

#### 42Axx Harmonic analysis in one variable

- **42A05** Trigonometric polynomials, inequalities, extremal problems
- 42A10 Trigonometric approximation
- 42A15 Trigonometric interpolation
- **42A16** Fourier coefficients, Fourier series of functions with special properties, special Fourier series {For automorphic theory, see mainly 11F30}
- **42A20** Convergence and absolute convergence of Fourier and trigonometric series
- ${\bf 42A24}\,$  Summability and absolute summability of Fourier and trigonometric series
- **42A32** Trigonometric series of special types (positive coefficients, monotonic coefficients, etc.)
- **42A38** Fourier and Fourier-Stieltjes transforms and other transforms of Fourier type
- 42A45 Multipliers in one variable harmonic analysis
- **42A50** Conjugate functions, conjugate series, singular integrals
- ${f 42A55}$  Lacunary series of trigonometric and other functions; Riesz products
- 42A61 Probabilistic methods for one variable harmonic analysis
- **42A63** Uniqueness of trigonometric expansions, uniqueness of Fourier expansions, Riemann theory, localization
- **42A65** Completeness of sets of functions in one variable harmonic analysis
- **42A70** Trigonometric moment problems in one variable harmonic analysis
- $\bf 42A75$  Classical almost periodic functions, mean periodic functions [See also  $\bf 43A60$ ]
- **42A82** Positive definite functions in one variable harmonic analysis
- ${f 42A85}$  Convolution, factorization for one variable harmonic analysis
- 42A99 None of the above, but in this section

# 42Bxx Harmonic analysis in several variables {For automorphic theory, see mainly 11F30}

- **42B05** Fourier series and coefficients in several variables
- 42B08 Summability in several variables
- ${\bf 42B10}$  Fourier and Fourier-Stieltjes transforms and other transforms of Fourier type
- 42B15 Multipliers for harmonic analysis in several variables
- $\bf 42B20$  Singular and oscillatory integrals (Calderón-Zygmund, etc.)
- 42B25 Maximal functions, Littlewood-Paley theory
- **42B30**  $H^p$ -spaces
- 42B35 Function spaces arising in harmonic analysis
- 42B37 Harmonic analysis and PDEs [See also 35-XX]
- 42B99 None of the above, but in this section

### 42Cxx Nontrigonometric harmonic analysis

- **42C05** Orthogonal functions and polynomials, general theory of nontrigonometric harmonic analysis [See also 33C45, 33C50, 33D45]
- **42C10** Fourier series in special orthogonal functions (Legendre polynomials, Walsh functions, etc.)
- 42C15 General harmonic expansions, frames
- 42C20 Other transformations of harmonic type
- 42C25 Uniqueness and localization for orthogonal series
- **42C30** Completeness of sets of functions in nontrigonometric harmonic analysis
- **42C40** Nontrigonometric harmonic analysis involving wavelets and other special systems
- 42C99 None of the above, but in this section

# 43-XX Abstract harmonic analysis {For other analysis on topological and Lie groups, see 22Exx}

- **43-00** General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to abstract harmonic analysis
- **43-01** Introductory exposition (textbooks, tutorial papers, etc.) pertaining to abstract harmonic analysis
- **43-02** Research exposition (monographs, survey articles) pertaining to abstract harmonic analysis
- 43-03 History of abstract harmonic analysis [Consider also classification numbers pertaining to Section 01]
- **43-04** Software, source code, etc. for problems pertaining to abstract harmonic analysis
- **43-06** Proceedings, conferences, collections, etc. pertaining to abstract harmonic analysis
- **43-08** Computational methods for problems pertaining to abstract harmonic analysis
- **43-11** Research data for problems pertaining to abstract harmonic analysis

# 43Axx Abstract harmonic analysis {For other analysis on topological and Lie groups, see 22Exx}

- 43A05 Measures on groups and semigroups, etc.
- 43A07 Means on groups, semigroups, etc.; amenable groups
- 43A10 Measure algebras on groups, semigroups, etc.
- **43A15**  $L^p$ -spaces and other function spaces on groups, semigroups, etc.
- **43A17** Analysis on ordered groups,  $H^p$ -theory
- **43A20**  $L^1$ -algebras on groups, semigroups, etc.

- **43A22** Homomorphisms and multipliers of function spaces on groups, semigroups, etc.
- **43A25** Fourier and Fourier-Stieltjes transforms on locally compact and other abelian groups
- **43A30** Fourier and Fourier-Stieltjes transforms on non-abelian groups and on semigroups, etc.
- 43A32 Other transforms and operators of Fourier type
- 43A35 Positive definite functions on groups, semigroups, etc.
- 43A40 Character groups and dual objects
- 43A45 Spectral synthesis on groups, semigroups, etc.
- **43A46** Special sets (thin sets, Kronecker sets, Helson sets, Ditkin sets, Sidon sets, etc.)
- ${f 43A50}$  Convergence of Fourier series and of inverse transforms
- 43A55 Summability methods on groups, semigroups, etc. [See also 40J05]
- 43A60 Almost periodic functions on groups and semigroups and their generalizations (recurrent functions, distal functions, etc.); almost automorphic functions
- 43A62 Harmonic analysis on hypergroups
- 43A65 Representations of groups, semigroups, etc. (aspects of abstract harmonic analysis) [See also 22A10, 22A20, 22Dxx, 22E45]
- 43A70 Analysis on specific locally compact and other abelian groups [See also 11R56, 22B05]
- 43A75 Harmonic analysis on specific compact groups
- 43A77 Harmonic analysis on general compact groups
- 43A80 Analysis on other specific Lie groups [See also 22Exx]
- 43A85 Harmonic analysis on homogeneous spaces
- **43A90** Harmonic analysis and spherical functions [See also 22E45, 22E46, 33C55]
- $\bf 43A95$  Categorical methods for abstract harmonic analysis [See also  $\bf 46Mxx$ ]
- 43A99 None of the above, but in this section

44-XX Integral transforms, operational calculus {For fractional derivatives and integrals, see 26A33; for Fourier transforms, see 42A38, 42B10; for integral transforms in distribution spaces, see 46F12; for numerical methods, see 65R10}

- **44-00** General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to integral transforms
- **44-01** Introductory exposition (textbooks, tutorial papers, etc.) pertaining to integral transforms

- **44-02** Research exposition (monographs, survey articles) pertaining to integral transforms
- **44-03** History of integral transforms [Consider also classification numbers pertaining to Section 01]
- **44-04** Software, source code, etc. for problems pertaining to integral transforms
- **44-06** Proceedings, conferences, collections, etc. pertaining to integral transforms
- **44-11** Research data for problems pertaining to integral transforms

44Axx Integral transforms, operational calculus {For fractional derivatives and integrals, see 26A33; for Fourier transforms, see 42A38, 42B10; for integral transforms in distribution spaces, see 46F12; for numerical methods, see 65R10}

- 44A05 General integral transforms [See also 42A38]
- 44A10 Laplace transform
- 44A12 Radon transform [See also 92C55]
- 44A15 Special integral transforms (Legendre, Hilbert, etc.)
- 44A20 Integral transforms of special functions
- 44A30 Multiple integral transforms
- 44A35 Convolution as an integral transform
- 44A40 Calculus of Mikusiński and other operational calculi
- 44A45 Classical operational calculus
- 44A55 Discrete operational calculus
- **44A60** Moment problems {For trigonometric moment problems, see 42A70}
- 44A99 None of the above, but in this section

### 45-XX Integral equations

- **45-00** General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to integral equations
- **45-01** Introductory exposition (textbooks, tutorial papers, etc.) pertaining to integral equations
- **45-02** Research exposition (monographs, survey articles) pertaining to integral equations
- **45-03** History of integral equations [Consider also classification numbers pertaining to Section 01]
- ${f 45\text{-}04}$  Software, source code, etc. for problems pertaining to integral equations
- ${f 45\text{-}06}$  Proceedings, conferences, collections, etc. pertaining to integral equations
- ${f 45\text{--}11}$  Research data for problems pertaining to integral equations

#### 45Axx Linear integral equations

45A05 Linear integral equations

45A99 None of the above, but in this section

#### 45Bxx Fredholm integral equations

45B05 Fredholm integral equations

45B99 None of the above, but in this section

# 45Cxx Eigenvalue problems for integral equations [See also 34Lxx, 35Pxx, 45P05, 47A75]

**45C05** Eigenvalue problems for integral equations [See also 34Lxx, 35Pxx, 45P05, 47A75]

45C99 None of the above, but in this section

### 45Dxx Volterra integral equations [See also 34A12]

45D05 Volterra integral equations [See also 34A12]

45D99 None of the above, but in this section

### 45Exx Singular integral equations [See also 30E20, 30E25, 44A15, 44A35]

**45E05** Integral equations with kernels of Cauchy type [See also 35J15]

**45E10** Integral equations of the convolution type (Abel, Picard, Toeplitz and Wiener-Hopf type) [See also 47B35]

45E99 None of the above, but in this section

#### 45Fxx Systems of linear integral equations

45F05 Systems of nonsingular linear integral equations

45F10 Dual, triple, etc., integral and series equations

45F15 Systems of singular linear integral equations

**45F99** None of the above, but in this section

### 45Gxx Nonlinear integral equations [See also 47H30, 47Jxx]

 ${f 45G05}$  Singular nonlinear integral equations

45G10 Other nonlinear integral equations

45G15 Systems of nonlinear integral equations

45G99 None of the above, but in this section

### 45Hxx Integral equations with miscellaneous special kernels [See also 44A15]

 ${f 45H05}$  Integral equations with miscellaneous special kernels [See also  ${f 44A15}$ ]

45H99 None of the above, but in this section

### tions [See also 34K05, 34K30, 47G20]

45J05 Integro-ordinary differential equations [See also 34K05, 34K30, 47G20]

45J99 None of the above, but in this section

#### 45Kxx Integro-partial differential equations [See also 34K30, 35R09, 35R10, 47G20]

45K05 Integro-partial differential equations [See also 34K30, 35R09, 35R10, 47G20

45K99 None of the above, but in this section

#### 45Lxx Theoretical approximation of solutions to integral equations {For numerical analysis, see 65Rxx}

45L05 Theoretical approximation of solutions to integral equations {For numerical analysis, see 65Rxx}

45L99 None of the above, but in this section

#### 45Mxx Qualitative behavior of solutions to integral equations

45M05 Asymptotics of solutions to integral equations

45M10 Stability theory for integral equations

45M15 Periodic solutions of integral equations

45M20 Positive solutions of integral equations

45M99 None of the above, but in this section

#### 45Nxx Abstract integral equations, integral equations in abstract spaces

45N05 Abstract integral equations, integral equations in abstract spaces

**45N99** None of the above, but in this section

### 45Pxx Integral operators [See also 47B38, 47G10

45P05 Integral operators [See also 47B38, 47G10]

45P99 None of the above, but in this section

#### 45Qxx Inverse problems for integral equations

45Q05 Inverse problems for integral equations

45Q99 None of the above, but in this section

### 45Jxx Integro-ordinary differential equa- 45Rxx Random integral equations [See also 60H20

**45R05** Random integral equations [See also 60H20]

45R99 None of the above, but in this section

### 46-XX Functional analysis {For manifolds modeled on topological linear spaces, see 57Nxx, 58Bxx}

46-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to functional analysis

**46-01** Introductory exposition (textbooks, tutorial papers, etc.) pertaining to functional analysis

46-02 Research exposition (monographs, survey articles) pertaining to functional analysis

46-03 History of functional analysis [Consider also classification numbers pertaining to Section 01]

**46-04** Software, source code, etc. for problems pertaining to functional analysis

46-06 Proceedings, conferences, collections, etc. pertaining to functional analysis

46-08 Computational methods for problems pertaining to functional analysis

46-11 Research data for problems pertaining to functional analysis

### 46Axx Topological linear spaces and related structures {For function spaces, see 46Exx}

46A03 General theory of locally convex spaces

46A04 Locally convex Fréchet spaces and (DF)-spaces

46A08 Barrelled spaces, bornological spaces

46A11 Spaces determined by compactness or summability properties (nuclear spaces, Schwartz spaces, Montel spaces, etc.)

46A13 Spaces defined by inductive or projective limits (LB, LF, etc.) [See also 46M40]

46A16 Not locally convex spaces (metrizable topological linear spaces, locally bounded spaces, quasi-Banach spaces, etc.)

46A17 Bornologies and related structures; Mackey convergence, etc.

46A19 Other "topological" linear spaces (convergence spaces, ranked spaces, spaces with a metric taking values in an ordered structure more general than  $\mathbb{R}$ , etc.)

46A20 Duality theory for topological vector spaces

46A22 Theorems of Hahn-Banach type; extension and lifting of functionals and operators [See also 46M10]

**46A25** Reflexivity and semi-reflexivity [See also 46B10]

46A30 Open mapping and closed graph theorems; completeness (including B-,  $B_r$ -completeness)

- **46A32** Spaces of linear operators; topological tensor products; approximation properties [See also 46B28, 46M05, 47L05, 47L20]
- 46A35 Summability and bases in topological vector spaces [See also 46B15]
- **46A40** Ordered topological linear spaces, vector lattices [See also 06F20, 46B40, 46B42]
- 46A45 Sequence spaces (including Köthe sequence spaces) [See also 46B45]
- **46A50** Compactness in topological linear spaces; angelic spaces, etc.
- 46A55 Convex sets in topological linear spaces; Choquet theory [See also 52A07]
- 46A61 Graded Fréchet spaces and tame operators
- **46A63** Topological invariants ((DN),  $(\Omega)$ , etc.) for locally convex spaces
- **46A70** Saks spaces and their duals (strict topologies, mixed topologies, two-norm spaces, co-Saks spaces, etc.)
- 46A80 Modular spaces
- 46A99 None of the above, but in this section

## 46Bxx Normed linear spaces and Banach spaces; Banach lattices {For function spaces, see 46Exx}

- ${\bf 46B03}$  Isomorphic theory (including renorming) of Banach spaces
- 46B04 Isometric theory of Banach spaces
- 46B06 Asymptotic theory of Banach spaces [See also 52A23]
- 46B07 Local theory of Banach spaces
- 46B08 Ultraproduct techniques in Banach space theory [See also 46M07]
- 46B09 Probabilistic methods in Banach space theory [See also 60Bxx]
- **46B10** Duality and reflexivity in normed linear and Banach spaces [See also 46A25]
- **46B15** Summability and bases; functional analytic aspects of frames in Banach and Hilbert spaces [See also 46A35, 42C15]
- 46B20 Geometry and structure of normed linear spaces
- **46B22** Radon-Nikodým, Kreĭn-Milman and related properties [See also 46G10]
- 46B25 Classical Banach spaces in the general theory
- 46B26 Nonseparable Banach spaces
- **46B28** Spaces of operators; tensor products; approximation properties [See also 46A32, 46M05, 47L05, 47L20]
- $\bf 46B40$  Ordered normed spaces [See also  $\bf 46A40,\, 46B42]$
- **46B42** Banach lattices [See also 46A40, 46B40]
- **46B45** Banach sequence spaces [See also 46A45]
- 46B50 Compactness in Banach (or normed) spaces

- **46B70** Interpolation between normed linear spaces [See also 46M35]
- **46B80** Nonlinear classification of Banach spaces; nonlinear quotients
- **46B85** Embeddings of discrete metric spaces into Banach spaces; applications in topology and computer science [See also 05C12, 68Rxx]
- 46B87 Lineability in functional analysis [See also 15A03]
- 46B99 None of the above, but in this section

# 46Cxx Inner product spaces and their generalizations, Hilbert spaces {For function spaces, see 46Exx}

- **46C05** Hilbert and pre-Hilbert spaces: geometry and topology (including spaces with semidefinite inner product)
- **46C07** Hilbert subspaces (= operator ranges); complementation (Aronszajn, de Branges, etc.) [See also 46B70, 46M35]
- 46C15 Characterizations of Hilbert spaces
- 46C20 Spaces with indefinite inner product (Kreĭn spaces, Pontryagin spaces, etc.) [See also 47B50]
- **46C50** Generalizations of inner products (semi-inner products, partial inner products, etc.)
- 46C99 None of the above, but in this section

# 46Exx Linear function spaces and their duals [See also 30H05, 32A38, 46F05] {For function algebras, see 46J10}

- ${f 46E05}$  Lattices of continuous, differentiable or analytic functions
- **46E10** Topological linear spaces of continuous, differentiable or analytic functions
- 46E15 Banach spaces of continuous, differentiable or analytic functions
- ${f 46E20}$  Hilbert spaces of continuous, differentiable or analytic functions
- **46E22** Hilbert spaces with reproducing kernels (= (proper) functional Hilbert spaces, including de Branges-Rovnyak and other structured spaces) [See also 47B32]
- $\bf 46E25$  Rings and algebras of continuous, differentiable or analytic functions {For Banach function algebras, see  $\bf 46J10,\, 46J15\}$
- 46E27 Spaces of measures [See also 28A33, 46Gxx]
- **46E30** Spaces of measurable functions ( $L^p$ -spaces, Orlicz spaces, Köthe function spaces, Lorentz spaces, rearrangement invariant spaces, ideal spaces, etc.)
- $\bf 46E35$  Sobolev spaces and other spaces of "smooth" functions, embedding theorems, trace theorems
- **46E36** Sobolev (and similar kinds of) spaces of functions on metric spaces; analysis on metric spaces

- ${f 46E39}$  Sobolev (and similar kinds of) spaces of functions of discrete variables
- 46E40 Spaces of vector- and operator-valued functions
- **46E50** Spaces of differentiable or holomorphic functions on infinite-dimensional spaces [See also 46G20, 46G25, 47H60]
- 46E99 None of the above, but in this section

### 46Fxx Distributions, generalized functions, distribution spaces [See also 46T30]

- $\bf 46F05$  Topological linear spaces of test functions, distributions and ultradistributions [See also  $\bf 46E10,\, 46E35]$
- 46F10 Operations with distributions and generalized functions
- **46F12** Integral transforms in distribution spaces [See also 42- XX, 44-XX]
- **46F15** Hyperfunctions, analytic functionals [See also 32A25, 32A45, 32C35, 58J15]
- **46F20** Distributions and ultradistributions as boundary values of analytic functions [See also 30D40, 30E25, 32A40]
- 46F25 Distributions on infinite-dimensional spaces [See also 58C35]
- **46F30** Generalized functions for nonlinear analysis (Rosinger, Colombeau, nonstandard, etc.)
- 46F99 None of the above, but in this section

# 46Gxx Measures, integration, derivative, holomorphy (all involving infinite-dimensional spaces) [See also 28-XX, 46Txx]

- **46G05** Derivatives of functions in infinite-dimensional spaces [See also 46T20, 58C20, 58C25]
- $\bf 46G10$  Vector-valued measures and integration [See also  $\bf 28Bxx,\, 46B22]$
- **46G12** Measures and integration on abstract linear spaces [See also 28C20, 46T12]
- **46G15** Functional analytic lifting theory [See also 28A51]
- **46G20** Infinite-dimensional holomorphy [See also 32-XX, 46E50, 46T25, 58B12, 58C10]
- 46G25 (Spaces of) multilinear mappings, polynomials [See also 46E50, 46G20, 47H60]
- 46G99 None of the above, but in this section

# 46Hxx Topological algebras, normed rings and algebras, Banach algebras {For group algebras, convolution algebras and measure algebras, see 43A10, 43A20}

46H05 General theory of topological algebras

- 46H10 Ideals and subalgebras
- 46H15 Representations of topological algebras
- 46H20 Structure, classification of topological algebras
- **46H25** Normed modules and Banach modules, topological modules (if not placed in 13-XX or 16-XX)
- **46H30** Functional calculus in topological algebras [See also 47A60]
- 46H35 Topological algebras of operators [See mainly 47Lxx]
- **46H40** Automatic continuity
- **46H70** Nonassociative topological algebras [See also 46K70, 46L70]
- 46H99 None of the above, but in this section

## 46Jxx Commutative Banach algebras and commutative topological algebras [See also 46E25]

- 46J05 General theory of commutative topological algebras
- **46J10** Banach algebras of continuous functions, function algebras [See also 46E25]
- **46J15** Banach algebras of differentiable or analytic functions,  $H^p$ -spaces [See also 30H10, 32A35, 32A37, 32A38, 42B30]
- 46J20 Ideals, maximal ideals, boundaries
- 46J25 Representations of commutative topological algebras
- 46J30 Subalgebras of commutative topological algebras
- **46J40** Structure and classification of commutative topological algebras
- 46J45 Radical Banach algebras
- 46J99 None of the above, but in this section

### 46Kxx Topological (rings and) algebras with an involution [See also 16W10]

- 46K05 General theory of topological algebras with involution
- ${f 46K10}$  Representations of topological algebras with involution
- 46K15 Hilbert algebras
- ${f 46K50}$  Nonselfadjoint (sub)algebras in algebras with involution
- **46K70** Nonassociative topological algebras with an involution [See also 46H70, 46L70]
- 46K99 None of the above, but in this section

# 46Lxx Selfadjoint operator algebras ( $C^*$ -algebras, von Neumann ( $W^*$ -) algebras, etc.) [See also 22D25, 47Lxx]

- **46L05** General theory of  $C^*$ -algebras
- **46L06** Tensor products of  $C^*$ -algebras
- **46L07** Operator spaces and completely bounded maps [See also 47L25]
- **46L08**  $C^*$ -modules
- **46L09** Free products of  $C^*$ -algebras
- 46L10 General theory of von Neumann algebras
- 46L30 States of selfadjoint operator algebras
- **46L35** Classifications of  $C^*$ -algebras
- 46L36 Classification of factors
- 46L37 Subfactors and their classification
- 46L40 Automorphisms of selfadjoint operator algebras
- **46L45** Decomposition theory for  $C^*$ -algebras
- 46L51 Noncommutative measure and integration
- 46L52 Noncommutative function spaces
- 46L53 Noncommutative probability and statistics
- 46L54 Free probability and free operator algebras
- 46L55 Noncommutative dynamical systems [See also 28Dxx, 37Kxx, 37Lxx, 37A55]
- **46L57** Derivations, dissipations and positive semigroups in  $C^*$ -algebras
- **46L60** Applications of selfadjoint operator algebras to physics [See also 46N50, 46N55, 47L90, 81T05, 82B10, 82C10]
- **46L65** Quantizations, deformations for selfadjoint operator algebras
- 46L67 Quantum groups (operator algebraic aspects)
- **46L70** Nonassociative selfadjoint operator algebras [See also  $46H70, \ 46K70$ ]
- **46L80** K-theory and operator algebras (including cyclic theory) [See also 18F25, 19Kxx, 46M20, 55Rxx, 58J22]
- **46L85** Noncommutative topology [See also 58B32, 58B34, 58J22]
- **46L87** Noncommutative differential geometry [See also 58B32, 58B34, 58J22]
- **46L89** Other "noncommutative" mathematics based on  $C^*$ -algebra theory [See also 58B32, 58B34, 58J22]
- 46L99 None of the above, but in this section

### 46Mxx Methods of category theory in functional analysis [See also 18-XX]

- 46M05 Tensor products in functional analysis [See also  $46A32,\,46B28,\,47A80$ ]
- 46M07 Ultraproducts in functional analysis [See also 46B08, 46S20]

- ${\bf 46M10} \ \ {\bf Projective} \ {\bf and injective} \ {\bf objects} \ {\bf in} \ {\bf functional} \ {\bf analysis} \\ [{\bf See} \ {\bf also} \ \ {\bf 46A22}]$
- **46M15** Categories, functors in functional analysis {For *K*-theory, Ext, etc., see 19K33, 46L80, 46M18, 46M20}
- **46M18** Homological methods in functional analysis (exact sequences, right inverses, lifting, etc.)
- 46M20 Methods of algebraic topology in functional analysis (cohomology, sheaf and bundle theory, etc.) [See also 14F06, 18Fxx, 19Kxx, 32Cxx, 32Lxx, 46L80, 46M15, 46M18, 55Rxx]
- 46M35 Abstract interpolation of topological vector spaces [See also 46B70]
- ${\bf 46M40}\,$  Inductive and projective limits in functional analysis [See also  ${\bf 46A13}]$
- 46M99 None of the above, but in this section

### 46Nxx Miscellaneous applications of functional analysis [See also 47Nxx]

- **46N10** Applications of functional analysis in optimization, convex analysis, mathematical programming, economics
- 46N20 Applications of functional analysis to differential and integral equations
- **46N30** Applications of functional analysis in probability theory and statistics
- 46N40 Applications of functional analysis in numerical analysis [See also 65Jxx]
- **46N50** Applications of functional analysis in quantum physics
- ${f 46N55}$  Applications of functional analysis in statistical physics
- 46N60 Applications of functional analysis in biology and other sciences
- 46N99 None of the above, but in this section

### 46Sxx Other (nonclassical) types of functional analysis [See also 47Sxx]

- 46S05 Quaternionic functional analysis
- **46S10** Functional analysis over fields other than  $\mathbb{R}$  or  $\mathbb{C}$  or the quaternions; non-Archimedean functional analysis [See also 12J25, 32P05]
- 46S20 Nonstandard functional analysis [See also 03H05]
- **46S30** Constructive functional analysis [See also 03F60]
- **46S40** Fuzzy functional analysis [See also 03E72]
- 46S50 Functional analysis in probabilistic metric linear spaces
- $\bf 46S60$  Functional analysis on superspaces (supermanifolds) or graded spaces [See also  $58A50,\,58C50]$
- 46S99 None of the above, but in this section

### 46Txx Nonlinear functional analysis [See also 47Hxx, 47Jxx, 58Cxx, 58Dxx]

- **46T05** Infinite-dimensional manifolds [See also 53Axx, 57N20, 58Bxx, 58Dxx]
- 46T10 Manifolds of mappings
- **46T12** Measure (Gaussian, cylindrical, etc.) and integrals (Feynman, path, Fresnel, etc.) on manifolds [See also 28Cxx, 46G12, 60-XX]
- **46T20** Continuous and differentiable maps in nonlinear functional analysis [See also 46G05]
- ${\bf 46T25}$  Holomorphic maps in nonlinear functional analysis [See also  ${\bf 46G20}$ ]
- **46T30** Distributions and generalized functions on nonlinear spaces [See also 46Fxx]
- 46T99 None of the above, but in this section

### 47-XX Operator theory

- **47-00** General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to operator theory
- **47-01** Introductory exposition (textbooks, tutorial papers, etc.) pertaining to operator theory
- **47-02** Research exposition (monographs, survey articles) pertaining to operator theory
- 47-03 History of operator theory [Consider also classification numbers pertaining to Section 01]
- ${f 47\text{-}04}$  Software, source code, etc. for problems pertaining to operator theory
- **47-06** Proceedings, conferences, collections, etc. pertaining to operator theory
- ${\bf 47\text{-}08}\,$  Computational methods for problems pertaining to operator theory
- ${f 47\text{-}11}$  Research data for problems pertaining to operator theory

#### 47Axx General theory of linear operators

- **47A05** General (adjoints, conjugates, products, inverses, domains, ranges, etc.)
- **47A06** Linear relations (multivalued linear operators)
- 47A07 Forms (bilinear, sesquilinear, multilinear)
- **47A08** Operator matrices [See also 47A13]
- 47A10 Spectrum, resolvent
- 47A11 Local spectral properties of linear operators
- 47A12 Numerical range, numerical radius
- **47A13** Several-variable operator theory (spectral, Fredholm, etc.)
- **47A46**] Invariant subspaces of linear operators [See also 47A46]
- 47A16 Cyclic vectors, hypercyclic and chaotic operators

- **47A20** Dilations, extensions, compressions of linear operators
- 47A25 Spectral sets of linear operators
- **47A30** Norms (inequalities, more than one norm, etc.) of linear operators
- 47A35 Ergodic theory of linear operators [See also 28Dxx, 37Axx]
- 47A40 Scattering theory of linear operators [See also 34L25, 35P25, 37K15, 58J50, 81Uxx]
- 47A45 Canonical models for contractions and nonselfadjoint linear operators
- **47A46** Chains (nests) of projections or of invariant subspaces, integrals along chains, etc.
- **47A48** Operator colligations (= nodes), vessels, linear systems, characteristic functions, realizations, etc.
- 47A50 Equations and inequalities involving linear operators, with vector unknowns
- **47A52** Linear operators and ill-posed problems, regularization [See also 35R25, 47J06, 65F22, 65J20, 65L08, 65M30, 65R30]
- $\bf 47A53$  (Semi-) Fredholm operators; index theories [See also  $\bf 58B15,\, 58J20]$
- **47A55** Perturbation theory of linear operators [See also 47H14, 58J37, 70H09, 81Q15]
- 47A56 Functions whose values are linear operators (operator- and matrix-valued functions, etc., including analytic and meromorphic ones)
- 47A57 Linear operator methods in interpolation, moment and extension problems [See also 30E05, 42A70, 42A82, 44A60]
- 47A58 Linear operator approximation theory
- **47A60** Functional calculus for linear operators
- **47A62** Equations involving linear operators, with operator unknowns
- 47A63 Linear operator inequalities
- **47A64** Operator means involving linear operators, shorted linear operators, etc.
- 47A65 Structure theory of linear operators
- ${\bf 47A66} \ \ {\bf Quasitriangular} \ \ {\bf and} \ \ {\bf nonquasidiagonal} \ \ {\bf linear} \ \ {\bf operators}$  nal and nonquasidiagonal linear operators
- ${\bf 47A67}$  Representation theory of linear operators
- **47A68** Factorization theory (including Wiener-Hopf and spectral factorizations) of linear operators
- **47A70** (Generalized) eigenfunction expansions of linear operators; rigged Hilbert spaces
- **47A75** Eigenvalue problems for linear operators [See also 47J10, 49R05]
- 47A80 Tensor products of linear operators [See also 46M05]
- 47A99 None of the above, but in this section

#### 47Bxx Special classes of linear operators

- 47B01 Operators on Banach spaces
- 47B02 Operators on Hilbert spaces (general)
- 47B06 Riesz operators; eigenvalue distributions; approximation numbers, s-numbers, Kolmogorov numbers, entropy numbers, etc. of operators
- 47B07 Linear operators defined by compactness properties
- 47B10 Linear operators belonging to operator ideals (nuclear, p-summing, in the Schatten-von Neumann classes, etc.) [See also 47L20]
- 47B12 Sectorial operators
- 47B13 Cowen-Douglas operators
- **47B15** Hermitian and normal operators (spectral measures, functional calculus, etc.)
- 47B20 Subnormal operators, hyponormal operators, etc.
- 47B25 Linear symmetric and selfadjoint operators (unbounded)
- 47B28 Nonselfadjoint operators [See also 47A45, 81Q12]
- 47B32 Linear operators in reproducing-kernel Hilbert spaces (including de Branges, de Branges-Rovnyak, and other structured spaces) [See also 46E22]
- 47B33 Linear composition operators
- 47B34 Kernel operators
- **47B35** Toeplitz operators, Hankel operators, Wiener-Hopf operators {For other integral operators, see also 45P05, 47G10} [See also 32A25, 32M15]
- 47B36 Jacobi (tridiagonal) operators (matrices) and generalizations
- **47B37** Linear operators on special spaces (weighted shifts, operators on sequence spaces, etc.)
- 47B38 Linear operators on function spaces (general)
- **47B39** Linear difference operators [See also 39A70]
- 47B40 Spectral operators, decomposable operators, well-bounded operators, etc.
- 47B44 Linear accretive operators, dissipative operators, etc.
- 47B47 Commutators, derivations, elementary operators, etc.
- 47B48 Linear operators on Banach algebras
- **47B49** Transformers, preservers (linear operators on spaces of linear operators)
- $\bf 47B50$  Linear operators on spaces with an indefinite metric [See also  $\bf 46C20]$
- 47B60 Linear operators on ordered spaces
- ${f 47B65}$  Positive linear operators and order-bounded operators
- 47B80 Random linear operators [See also 47H40, 60H25]
- 47B90 Operator theory and harmonic analysis [See also 42-XX, 43-XX, 44-XX]
- 47B91 Operators on complex function spaces
- 47B92 Operators on real function spaces
- 47B93 Operators arising in mathematical physics
- 47B99 None of the above, but in this section

### 47Cxx Individual linear operators as elements of algebraic systems

- 47C05 Linear operators in algebras
- 47C10 Linear operators in \*-algebras
- **47C15** Linear operators in  $C^*$  or von Neumann algebras
- 47C99 None of the above, but in this section

## 47Dxx Groups and semigroups of linear operators, their generalizations and applications

- 47D03 Groups and semigroups of linear operators [See also 20M20] {For nonlinear operators, see 47H20}
- **47D06** One-parameter semigroups and linear evolution equations [See also 34G10, 34K30]
- 47D07 Markov semigroups and applications to diffusion processes {For Markov processes, see 60Jxx}
- 47D08 Schrödinger and Feynman-Kac semigroups
- **47D09** Operator sine and cosine functions and higher-order Cauchy problems [See also 34G10]
- **47D60** C-semigroups, regularized semigroups
- 47D62 Integrated semigroups
- **47D99** None of the above, but in this section

### 47Exx Ordinary differential operators [See also 34Bxx, 34Lxx]

- 47E05 Ordinary differential operators (should also be assigned at least one other classification number in Section 47) [See also 34Bxx, 34Lxx]
- **47E07** Functional-differential and differential-difference operators [See also 34K08]
- 47E99 None of the above, but in this section

### 47Fxx Partial differential operators [See also 35Pxx, 58Jxx]

- 47F05 Partial differential operators (should also be assigned at least one other classification number in Section 47) [See also 35Pxx, 58Jxx]
- 47F10 Elliptic operators and their generalizations {For elliptic complexes, see 58J10}
- 47F99 None of the above, but in this section

#### 47Gxx Integral, integro-differential, and 47J07 Abstract inverse mapping and implicit function thepseudodifferential operators also 58Jxx

- **47G10** Integral operators [See also 45P05]
- 47G20 Integro-differential operators [See also 34K30, 35R09, 35R10, 45Jxx, 45Kxx
- 47G30 Pseudodifferential operators [See also 35Sxx, 58Jxx]
- 47G40 Potential operators [See also 31-XX]
- 47G99 None of the above, but in this section

#### 47Hxx Nonlinear operators and their {For global properties and geometric see 49J53, 58-XX, especially aspects, **58Cxx**}

- **47H04** Set-valued operators [See also 28B20, 54C60, 58C06]
- 47H05 Monotone operators and generalizations
- 47H06 Nonlinear accretive operators, dissipative operators, etc.
- 47H07 Monotone and positive operators on ordered Banach spaces or other ordered topological vector spaces
- 47H08 Measures of noncompactness and condensing mappings, K-set contractions, etc.
- 47H09 Contraction-type mappings, nonexpansive mappings, A-proper mappings, etc.
- 47H10 Fixed-point theorems [See also 37C25, 54H25, 55M20, 58C301
- 47H11 Degree theory for nonlinear operators [See also 55M25, 58C30
- 47H14 Perturbations of nonlinear operators [See also 47A55, 58J37, 70H09, 70K60, 81Q15
- 47H20 Semigroups of nonlinear operators [See also 37L05, 47J35, 54H15, 58D07
- 47H25 Nonlinear ergodic theorems [See also 28Dxx, 37Axx, 47A35
- 47H30 Particular nonlinear operators (superposition, Hammerstein, Nemytskiĭ, Uryson, etc.) [See also 45Gxx, 45P05
- 47H40 Random nonlinear operators [See also 47B80, 60H25]
- 47H60 Multilinear and polynomial operators [See also 46G25]
- 47H99 None of the above, but in this section

### 47Jxx Equations and inequalities involving nonlinear operators [See also 46Txx] {For global and geometric aspects, see 58-XX

- **47J05** Equations involving nonlinear operators (general) [See also 47H10, 47J25]
- 47J06 Nonlinear ill-posed problems [See also 35R25, 47A52, 65F22, 65J20, 65L08, 65M30, 65R30]

- orems involving nonlinear operators [See also 46T20, 58C15
- 47J10 Nonlinear spectral theory, nonlinear eigenvalue problems [See also 49R05]
- 47J15 Abstract bifurcation theory involving nonlinear operators [See also 34C23, 37Gxx, 58E07, 58E09]
- 47J20 Variational and other types of inequalities involving nonlinear operators (general) [See also 49J40]
- 47J22 Variational and other types of inclusions [See also 34A60, 49J21, 49K21
- **47J25** Iterative procedures involving nonlinear operators [See also 47J26, 65J15]
- **47J26** Fixed-point iterations [See also 47J25]
- 47J30 Variational methods involving nonlinear operators [See also 58Exx]
- 47J35 Nonlinear evolution equations [See also 34G20, 35K90, 35L90, 35Qxx, 35R20, 37Kxx, 37Lxx, 47H20, 58D25
- 47J40 Equations with nonlinear hysteresis operators [See also 34C55, 74N30]
- 47J99 None of the above, but in this section

#### 47Lxx Linear spaces and algebras of operators [See also 46Lxx]

- 47L05 Linear spaces of operators [See also 46A32, 46B28]
- 47L07 Convex sets and cones of operators [See also 46A55]
- 47L10 Algebras of operators on Banach spaces and other topological linear spaces
- 47L15 Operator algebras with symbol structure
- **47L20** Operator ideals [See also 47B10]
- 47L22 Ideals of polynomials and of multilinear mappings in operator theory
- 47L25 Operator spaces (= matricially normed spaces) [See also 46L07
- 47L30 Abstract operator algebras on Hilbert spaces
- 47L35 Nest algebras, CSL algebras
- **47L40** Limit algebras, subalgebras of  $C^*$ -algebras
- 47L45 Dual algebras; weakly closed singly generated operator algebras
- **47L50** Dual spaces of operator algebras
- 47L55 Representations of (nonselfadjoint) operator algebras
- 47L60 Algebras of unbounded operators; partial algebras of operators
- 47L65 Crossed product algebras (analytic crossed products)
- 47L70 Nonassociative nonselfadjoint operator algebras
- 47L75 Other nonselfadjoint operator algebras
- 47L80 Algebras of specific types of operators (Toeplitz, integral, pseudodifferential, etc.)
- 47L90 Applications of operator algebras to the sciences
- 47L99 None of the above, but in this section

### 47Nxx Miscellaneous applications of operator theory [See also 46Nxx]

- **47N10** Applications of operator theory in optimization, convex analysis, mathematical programming, economics
- 47N20 Applications of operator theory to differential and integral equations
- 47N30 Applications of operator theory in probability theory and statistics
- **47N40** Applications of operator theory in numerical analysis [See also 65Jxx]
- 47N50 Applications of operator theory in the physical sciences
- 47N60 Applications of operator theory in chemistry and life sciences
- 47N70 Applications of operator theory in systems, signals, circuits, and control theory
- 47N99 None of the above, but in this section

### 47Sxx Other (nonclassical) types of operator theory [See also 46Sxx]

- 47S05 Quaternionic operator theory
- **47S10** Operator theory over fields other than  $\mathbb{R}$ ,  $\mathbb{C}$  or the quaternions; non-Archimedean operator theory
- 47S20 Nonstandard operator theory [See also 03H05]
- 47S30 Constructive operator theory [See also 03F60]
- **47S40** Fuzzy operator theory [See also 03E72]
- 47S50 Operator theory in probabilistic metric linear spaces [See also 54E70]
- 47S99 None of the above, but in this section

# 49-XX Calculus of variations and optimal control; optimization [See also 34H05, 34K35, 65Kxx, 90Cxx, 93-XX]

- **49-00** General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to calculus of variations and optimal control
- **49-01** Introductory exposition (textbooks, tutorial papers, etc.) pertaining to calculus of variations and optimal control
- **49-02** Research exposition (monographs, survey articles) pertaining to calculus of variations and optimal control
- **49-03** History of calculus of variations and optimal control [Consider also classification numbers pertaining to Section 01]
- **49-04** Software, source code, etc. for problems pertaining to calculus of variations and optimal control

- **49-06** Proceedings, conferences, collections, etc. pertaining to calculus of variations and optimal control
- **49-11** Research data for problems pertaining to calculus of variations and optimal control

### 49Jxx Existence theories in calculus of variations and optimal control

- **49J05** Existence theories for free problems in one independent variable
- **49J10** Existence theories for free problems in two or more independent variables
- 49J15 Existence theories for optimal control problems involving ordinary differential equations
- **49J20** Existence theories for optimal control problems involving partial differential equations
- **49J21** Existence theories for optimal control problems involving relations other than differential equations
- **49J27** Existence theories for problems in abstract spaces [See also 90C48, 93C25]
- **49J30** Existence of optimal solutions belonging to restricted classes (Lipschitz controls, bang-bang controls, etc.)
- 49J35 Existence of solutions for minimax problems
- 49J40 Variational inequalities [See also 47J20]
- 49J45 Methods involving semicontinuity and convergence; relaxation
- **49J50** Fréchet and Gateaux differentiability in optimization [See also 46G05, 58C20]
- 49J52 Nonsmooth analysis [See also 46G05, 58C50, 90C56]
- **49J53** Set-valued and variational analysis [See also 28B20, 47H04, 54C60, 58C06]
- **49J55** Existence of optimal solutions to problems involving randomness [See also 93E20]
- 49J99 None of the above, but in this section

#### 49Kxx Optimality conditions

- 49K05 Optimality conditions for free problems in one independent variable
- **49K10** Optimality conditions for free problems in two or more independent variables
- ${f 49K15}$  Optimality conditions for problems involving ordinary differential equations
- **49K20** Optimality conditions for problems involving partial differential equations
- 49K21 Optimality conditions for problems involving relations other than differential equations
- **49K27** Optimality conditions for problems in abstract spaces [See also 90C48, 93C25]
- 49K30 Optimality conditions for solutions belonging to restricted classes (Lipschitz controls, bang-bang controls, etc.)

- 49K35 Optimality conditions for minimax problems
- 49K40 Sensitivity, stability, well-posedness [See also 90C31]
- 49K45 Optimality conditions for problems involving randomness [See also 93E20]
- 49K99 None of the above, but in this section

### 49Lxx Hamilton-Jacobi theories [See also 70H20, 35F21]

- **49L05** Hamilton-Jacobi equations in optimal control and differential games
- ${f 49L20}$  Dynamic programming in optimal control and differential games
- **49L25** Viscosity solutions to Hamilton-Jacobi equations in optimal control and differential games
- 49L99 None of the above, but in this section

### 49Mxx Numerical methods in optimal control [See also 65Kxx, 90-08, 90Cxx]

- 49M05 Numerical methods based on necessary conditions
- 49M15 Newton-type methods [See also 90C53]
- 49M20 Numerical methods of relaxation type
- 49M25 Discrete approximations in optimal control
- 49M27 Decomposition methods
- 49M29 Numerical methods involving duality
- **49M37** Numerical methods based on nonlinear programming [See also 65Kxx, 90C30]
- 49M40 PDE constrained optimization
- 49M99 None of the above, but in this section

### 49Nxx Miscellaneous topics in calculus of variations and optimal control

- 49N05 Linear optimal control problems [See also 93C05]
- 49N10 Linear-quadratic optimal control problems
- 49N15 Duality theory (optimization) [See also 90C46]
- 49N20 Periodic optimal control problems
- 49N25 Impulsive optimal control problems
- **49N30** Problems with incomplete information (optimization) [See also 93C41]
- 49N35 Optimal feedback synthesis [See also 93B52]
- 49N45 Inverse problems in optimal control
- 49N60 Regularity of solutions in optimal control
- 49N70 Differential games and control [See also 91A23]
- 49N75 Pursuit and evasion games [See also 91A24]
- 49N80 Mean field games and control [See also 91A16]
- **49N90** Applications of optimal control and differential games [See also 90C90, 91A80, 93C95]
- 49N99 None of the above, but in this section

### 49Qxx Manifolds and measure-geometric topics [See also 58Exx]

- $\bf 49Q05$  Minimal surfaces and optimization [See also 53A10,  $\bf 58E12]$
- **49Q10** Optimization of shapes other than minimal surfaces [See also 90C90]
- ${f 49Q12}$  Sensitivity analysis for optimization problems on manifolds
- **49Q15** Geometric measure and integration theory, integral and normal currents in optimization [See also 28A75, 32C30, 58A25, 58C35]
- 49Q20 Variational problems in a geometric measuretheoretic setting
- 49Q25 Optimal transportation [See also 90B06]
- 49Q99 None of the above, but in this section

# 49Rxx Variational methods for eigenvalues of operators (should also be assigned at least one other classification number in Section 49) [See also 47A75]

- **49R05** Variational methods for eigenvalues of operators (should also be assigned at least one other classification number in Section 49) [See also 47A75]
- 49R99 None of the above, but in this section

# 49Sxx Variational principles of physics (should also be assigned at least one other classification number in Section 49)

- **49S05** Variational principles of physics (should also be assigned at least one other classification number in Section 49)
- 49S99 None of the above, but in this section

# 51-XX Geometry {For algebraic geometry, see 14-XX; for differential geometry, see 53-XX}

- **51-00** General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to geometry
- 51-01 Introductory exposition (textbooks, tutorial papers, etc.) pertaining to geometry
- ${f 51\text{-}02}$  Research exposition (monographs, survey articles) pertaining to geometry
- 51-03 History of geometry [Consider also classification numbers pertaining to Section 01]
- ${f 51\text{-}04}$  Software, source code, etc. for problems pertaining to geometry
- ${f 51\text{-}06}$  Proceedings, conferences, collections, etc. pertaining to geometry

- ${\bf 51\text{-}08}\,$  Computational methods for problems pertaining to geometry
- 51-11 Research data for problems pertaining to geometry

#### 51Axx Linear incidence geometry

- 51A05 General theory of linear incidence geometry and projective geometries
- 51A10 Homomorphism, automorphism and dualities in linear incidence geometry
- 51A15 Linear incidence geometric structures with parallelism
- **51A20** Configuration theorems in linear incidence geometry
- 51A25 Algebraization in linear incidence geometry [See also 12Kxx, 20N05]
- **51A30** Desarguesian and Pappian geometries
- 51A35 Non-Desarguesian affine and projective planes
- 51A40 Translation planes and spreads in linear incidence geometry
- 51A45 Incidence structures embeddable into projective geometries
- 51A50 Polar geometry, symplectic spaces, orthogonal spaces
- 51A99 None of the above, but in this section

#### 51Bxx Nonlinear incidence geometry

- 51B05 General theory of nonlinear incidence geometry
- 51B10 Möbius geometries
- 51B15 Laguerre geometries
- ${f 51B20}$  Minkowski geometries in nonlinear incidence geometry
- 51B25 Lie geometries in nonlinear incidence geometry
- 51B99 None of the above, but in this section

# 51Cxx Ring geometry (Hjelmslev, Barbilian, etc.)

- 51C05 Ring geometry (Hjelmslev, Barbilian, etc.)
- 51C99 None of the above, but in this section

#### 51Dxx Geometric closure systems

- 51D05 Abstract (Maeda) geometries
- 51D10 Abstract geometries with exchange axiom
- 51D15 Abstract geometries with parallelism
- 51D20 Combinatorial geometries and geometric closure systems [See also  $05B25,\,05B35$ ]
- 51D25 Lattices of subspaces and geometric closure systems [See also 05B35]
- 51D30 Continuous geometries, geometric closure systems and related topics [See also 06Cxx]
- 51D99 None of the above, but in this section

# 51Exx Finite geometry and special incidence structures

- 51E05 General block designs in finite geometry [See also 05B05]
- 51E10 Steiner systems in finite geometry [See also 05B05]
- ${f 51E12}$  Generalized quadrangles and generalized polygons in finite geometry
- ${f 51E14}$  Finite partial geometries (general), nets, partial spreads
- 51E15 Finite affine and projective planes (geometric aspects)
- 51E20 Combinatorial structures in finite projective spaces [See also 05Bxx]
- 51E21 Blocking sets, ovals, k-arcs
- $\bf 51E22$  Linear codes and caps in Galois spaces [See also 94B05]
- 51E23 Spreads and packing problems in finite geometry
- 51E24 Buildings and the geometry of diagrams
- 51E25 Other finite nonlinear geometries
- 51E26 Other finite linear geometries
- 51E30 Other finite incidence structures (geometric aspects) [See also 05B30]
- 51E99 None of the above, but in this section

#### 51Fxx Metric geometry

- **51F05** Absolute planes in metric geometry
- **51F10** Absolute spaces in metric geometry
- $\bf 51F15$  Reflection groups, reflection geometries [See also 20H10, 20H15] {For Coxeter groups, see 20F55}
- 51F20 Congruence and orthogonality in metric geometry [See also 20H05]
- 51F25 Orthogonal and unitary groups in metric geometry [See also 20H05]
- 51F30 Lipschitz and coarse geometry of metric spaces [See also 53C23]
- 51F99 None of the above, but in this section

# 51Gxx Ordered geometries (ordered incidence structures, etc.)

- **51G05** Ordered geometries (ordered incidence structures, etc.)
- 51G99 None of the above, but in this section

#### 51Hxx Topological geometry

- 51H05 General theory of topological geometry
- 51H10 Topological linear incidence structures
- 51H15 Topological nonlinear incidence structures
- 51H20 Topological geometries on manifolds [See also 57-XX]
- 51H25 Geometries with differentiable structure [See also 53Cxx, especially 53C70]
- ${\bf 51H30}$  Geometries with algebraic manifold structure [See also 14-XX]
- 51H99 None of the above, but in this section

#### 51Jxx Incidence groups

- ${f 51J05}$  General theory of incidence groups
- ${f 51J10}$  Projective incidence groups
- 51J15 Kinematic spaces
- 51J20 Representation by near-fields and near-algebras [See also 12K05, 16Y30]
- 51J99 None of the above, but in this section

#### 51Kxx Distance geometry

- 51K05 General theory of distance geometry
- 51K10 Synthetic differential geometry
- 51K99 None of the above, but in this section

# 51Lxx Geometric order structures [See also 53C75]

- 51L05 Geometry of orders of nondifferentiable curves
- 51L10 Directly differentiable curves in geometric order structures
- 51L15 *n*-vertex theorems via direct methods
- 51L20 Geometry of orders of surfaces
- 51L99 None of the above, but in this section

#### 51Mxx Real and complex geometry

- 51M04 Elementary problems in Euclidean geometries
- **51M05** Euclidean geometries (general) and generalizations
- 51M09 Elementary problems in hyperbolic and elliptic geometries
- 51M10 Hyperbolic and elliptic geometries (general) and generalizations
- 51M15 Geometric constructions in real or complex geometry
- **51M16** Inequalities and extremum problems in real or complex geometry {For convex problems, see 52A40}
- 51M20 Polyhedra and polytopes; regular figures, division of spaces [See also 51F15]
- ${\bf 51M25}\;$  Length, area and volume in real or complex geometry [See also  $26{\rm B15}]$

- 51M30 Line geometries and their generalizations [See also 53A25]
- **51M35** Synthetic treatment of fundamental manifolds in projective geometries (Grassmannians, Veronesians and their generalizations) [See also 14M15]
- 51M99 None of the above, but in this section

#### 51Nxx Analytic and descriptive geometry

- 51N05 Descriptive geometry [See also 65D17, 68U07]
- 51N10 Affine analytic geometry
- 51N15 Projective analytic geometry
- 51N20 Euclidean analytic geometry
- 51N25 Analytic geometry with other transformation groups
- 51N30 Geometry of classical groups [See also 14L35, 20Gxx]
- 51N35 Questions of classical algebraic geometry [See also 14Nxx]
- 51N99 None of the above, but in this section

#### 51Pxx Classical or axiomatic geometry and physics (should also be assigned at least one other classification number from Sections 70–86)

- **51P05** Classical or axiomatic geometry and physics (should also be assigned at least one other classification number from Sections 70–86)
- 51P99 None of the above, but in this section

# 52-XX Convex and discrete geometry

- 52-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to convex and discrete geometry
- **52-01** Introductory exposition (textbooks, tutorial papers, etc.) pertaining to convex and discrete geometry
- **52-02** Research exposition (monographs, survey articles) pertaining to convex and discrete geometry
- **52-03** History of convex and discrete geometry [Consider also classification numbers pertaining to Section 01]
- **52-04** Software, source code, etc. for problems pertaining to convex and discrete geometry
- **52-06** Proceedings, conferences, collections, etc. pertaining to convex and discrete geometry
- **52-08** Computational methods for problems pertaining to convex and discrete geometry
- ${f 52\text{-}11}$  Research data for problems pertaining to convex and discrete geometry

#### 52Axx General convexity

- 52A01 Axiomatic and generalized convexity
- **52A05** Convex sets without dimension restrictions (aspects of convex geometry)
- **52A07** Convex sets in topological vector spaces (aspects of convex geometry) [See also 46A55]
- 52A10 Convex sets in 2 dimensions (including convex curves) [See also 53A04]
- **52A15** Convex sets in 3 dimensions (including convex surfaces) [See also 53A05, 53C45]
- **52A20** Convex sets in n dimensions (including convex hypersurfaces) [See also 53A07, 53C45]
- 52A21 Convexity and finite-dimensional Banach spaces (including special norms, zonoids, etc.) (aspects of convex geometry) [See also 46Bxx]
- **52A22** Random convex sets and integral geometry (aspects of convex geometry) [See also 53C65, 60D05]
- **52A23** Asymptotic theory of convex bodies [See also 46B06]
- 52A27 Approximation by convex sets
- **52A30** Variants of convex sets (star-shaped, (m, n)-convex, etc.)
- 52A35 Helly-type theorems and geometric transversal theory
- 52A37 Other problems of combinatorial convexity
- **52A38** Length, area, volume and convex sets (aspects of convex geometry) [See also 26B15, 28A75, 49Q20]
- **52A39** Mixed volumes and related topics in convex geometry
- **52A40** Inequalities and extremum problems involving convexity in convex geometry
- **52A41** Convex functions and convex programs in convex geometry [See also 26B25, 90C25]
- 52A55 Spherical and hyperbolic convexity
- 52A99 None of the above, but in this section

#### 52Bxx Polytopes and polyhedra

- **52B05** Combinatorial properties of polytopes and polyhedra (number of faces, shortest paths, etc.) [See also 05Cxx]
- 52B10 Three-dimensional polytopes
- **52B11** *n*-dimensional polytopes
- **52B12** Special polytopes (linear programming, centrally symmetric, etc.)
- **52B15** Symmetry properties of polytopes
- 52B20 Lattice polytopes in convex geometry (including relations with commutative algebra and algebraic geometry) [See also 06A11, 13F20, 13F55, 13Hxx, 52C05, 52C07]
- ${\bf 52B22}\,$  Shellability for polytopes and polyhedra
- 52B35 Gale and other diagrams

- **52B40** Matroids in convex geometry (realizations in the context of convex polytopes, convexity in combinatorial structures, etc.) [See also 05B35, 52Cxx]
- **52B45** Dissections and valuations (Hilbert's third problem, etc.)
- **52B55** Computational aspects related to convexity {For computational methods, see 52-08; for computational geometry and algorithms, see 68Q25, 68U05; for numerical algorithms, see 65Yxx} [See also 68Uxx]
- **52B60** Isoperimetric problems for polytopes
- 52B70 Polyhedral manifolds
- 52B99 None of the above, but in this section

#### 52Cxx Discrete geometry

- **52C05** Lattices and convex bodies in 2 dimensions (aspects of discrete geometry) [See also 11H06, 11H31, 11P21]
- **52C07** Lattices and convex bodies in n dimensions (aspects of discrete geometry) [See also 11H06, 11H31, 11P21]
- 52C10 Erdős problems and related topics of discrete geometry [See also 11Hxx]
- **52C15** Packing and covering in 2 dimensions (aspects of discrete geometry) [See also 05B40, 11H31]
- **52C17** Packing and covering in n dimensions (aspects of discrete geometry) [See also 05B40, 11H31]
- 52C20 Tilings in 2 dimensions (aspects of discrete geometry) [See also 05B45, 51M20]
- **52C22** Tilings in n dimensions (aspects of discrete geometry) [See also 05B45, 51M20]
- **52C23** Quasicrystals and aperiodic tilings in discrete geometry
- 52C25 Rigidity and flexibility of structures (aspects of discrete geometry) [See also 70B15]
- 52C26 Circle packings and discrete conformal geometry
- **52C30** Planar arrangements of lines and pseudolines (aspects of discrete geometry)
- $\bf 52C35$  Arrangements of points, flats, hyperplanes (aspects of discrete geometry) [See also  $14N20,\,32S22]$
- **52C40** Oriented matroids in discrete geometry
- ${f 52C45}$  Combinatorial complexity of geometric structures [See also  ${f 68U05}$ ]
- 52C99 None of the above, but in this section

# 53-XX Differential geometry {For differential topology, see 57Rxx; for foundational questions of differentiable manifolds, see 58Axx}

- 53-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to differential geometry
- **53-01** Introductory exposition (textbooks, tutorial papers, etc.) pertaining to differential geometry

- **53-02** Research exposition (monographs, survey articles) pertaining to differential geometry
- **53-03** History of differential geometry [Consider also classification numbers pertaining to Section 01]
- **53-04** Software, source code, etc. for problems pertaining to differential geometry
- **53-06** Proceedings, conferences, collections, etc. pertaining to differential geometry
- **53-08** Computational methods for problems pertaining to differential geometry
- **53-11** Research data for problems pertaining to differential geometry

#### 53Axx Classical differential geometry

- 53A04 Curves in Euclidean and related spaces
- 53A05 Surfaces in Euclidean and related spaces
- 53A07 Higher-dimensional and -codimensional surfaces in Euclidean and related n-spaces
- 53A10 Minimal surfaces in differential geometry, surfaces with prescribed mean curvature [See also 49Q05, 49Q10, 53C42]
- **53A15** Affine differential geometry
- **53A17** Differential geometric aspects in kinematics
- 53A20 Projective differential geometry
- **53A25** Differential line geometry
- ${f 53A30}$  Differential geometry of submanifolds of Möbius space
- 53A35 Non-Euclidean differential geometry
- 53A40 Other special differential geometries
- ${f 53A45}$  Differential geometric aspects in vector and tensor analysis
- ${f 53A55}$  Differential invariants (local theory), geometric objects
- **53A60** Differential geometry of webs [See also 14C21, 20N05]
- 53A70 Discrete differential geometry
- 53A99 None of the above, but in this section

#### 53Bxx Local differential geometry

- 53B05 Linear and affine connections
- **53B10** Projective connections
- **53B12** Differential geometric aspects of statistical manifolds and information geometry
- **53B15** Other connections
- 53B20 Local Riemannian geometry
- 53B21 Methods of local Riemannian geometry
- **53B25** Local submanifolds [See also 53C40]
- **53B30** Local differential geometry of Lorentz metrics, indefinite metrics

- **53B35** Local differential geometry of Hermitian and Kählerian structures [See also 32Qxx]
- **53B40** Local differential geometry of Finsler spaces and generalizations (areal metrics)
- ${f 53B50}$  Applications of local differential geometry to the sciences
- **53B99** None of the above, but in this section

# 53Cxx Global differential geometry [See also 51H25, 58-XX] {For related bundle theory, see 55Rxx, 57Rxx]

- **53C05** Connections, general theory
- **53C07** Special connections and metrics on vector bundles (Hermite-Einstein, Yang-Mills) [See also 32Q20]
- 53C08 Differential geometric aspects of gerbes and differential characters
- **53C10** *G*-structures
- 53C12 Foliations (differential geometric aspects) [See also 57R30, 57R32]
- **53C15** General geometric structures on manifolds (almost complex, almost product structures, etc.)
- **53C17** Sub-Riemannian geometry
- 53C18 Conformal structures on manifolds
- 53C20 Global Riemannian geometry, including pinching [See also 31C12, 58B20]
- 53C21 Methods of global Riemannian geometry, including PDE methods; curvature restrictions [See also 58J60]
- 53C22 Geodesics in global differential geometry [See also 58E10]
- 53C23 Global geometric and topological methods (à la Gromov); differential geometric analysis on metric spaces
- 53C24 Rigidity results
- 53C25 Special Riemannian manifolds (Einstein, Sasakian, etc.)
- 53C26 Hyper-Kähler and quaternionic Kähler geometry, "special" geometry
- 53C27 Spin and Spin<sup>c</sup> geometry
- 53C28 Twistor methods in differential geometry [See also 32L25]
- **53C29** Issues of holonomy in differential geometry
- **53C30** Differential geometry of homogeneous manifolds [See also 14M15, 14M17, 32M10, 57T15]
- **53C35** Differential geometry of symmetric spaces [See also 32M15, 57T15]
- 53C38 Calibrations and calibrated geometries
- **53C40** Global submanifolds [See also 53B25]
- 53C42 Differential geometry of immersions (minimal, prescribed curvature, tight, etc.) [See also 49Q05, 49Q10, 53A10, 57R40, 57R42]
- 53C43 Differential geometric aspects of harmonic maps [See also 58E20]

- **53C45** Global surface theory (convex surfaces à la A. D. Aleksandrov)
- ${f 53C50}$  Global differential geometry of Lorentz manifolds, manifolds with indefinite metrics
- 53C55 Global differential geometry of Hermitian and Kählerian manifolds [See also 32Qxx]
- **53C56** Other complex differential geometry [See also 32Qxx]
- **53C60** Global differential geometry of Finsler spaces and generalizations (areal metrics) [See also 58B20]
- **53C65** Integral geometry [See also 52A22, 60D05]; differential forms, currents, etc. [See mainly 58Axx]
- **53C70** Direct methods (*G*-spaces of Busemann, etc.)
- **53C75** Geometric orders, order geometry [See also 51Lxx]
- **53C80** Applications of global differential geometry to the sciences
- 53C99 None of the above, but in this section

# 53Dxx Symplectic geometry, contact geometry [See also 37Jxx, 70Gxx, 70Hxx]

- 53D05 Symplectic manifolds, general
- 53D10 Contact manifolds, general
- 53D12 Lagrangian submanifolds; Maslov index
- 53D15 Almost contact and almost symplectic manifolds
- 53D17 Poisson manifolds; Poisson groupoids and algebroids
- 53D18 Generalized geometries (à la Hitchin)
- **53D20** Momentum maps; symplectic reduction
- **53D22** Canonical transformations in symplectic and contact geometry
- **53D25** Geodesic flows in symplectic geometry and contact geometry
- 53D30 Symplectic structures of moduli spaces
- 53D35 Global theory of symplectic and contact manifolds [See also 57Rxx]
- 53D37 Symplectic aspects of mirror symmetry, homological mirror symmetry, and Fukaya category [See also 14J33]
- 53D40 Symplectic aspects of Floer homology and cohomology
- **53D42** Symplectic field theory; contact homology
- **53D45** Gromov-Witten invariants, quantum cohomology, Frobenius manifolds [See also 14N35]
- 53D50 Geometric quantization
- **53D55** Deformation quantization, star products
- 53D99 None of the above, but in this section

#### 53Exx Geometric evolution equations

- 53E10 Flows related to mean curvature
- 53E20 Ricci flows
- **53E30** Flows related to complex manifolds (e.g., Kähler-Ricci flows, Chern-Ricci flows)
- **53E40** Higher-order geometric flows
- **53E50** Flows related to symplectic and contact structures
- 53E99 None of the above, but in this section

# 53Zxx Applications of differential geometry to sciences and engineering

- **53Z05** Applications of differential geometry to physics
- **53Z10** Applications of differential geometry to biology
- 53Z15 Applications of differential geometry to chemistry
- **53Z30** Applications of differential geometry to engineering
- ${f 53Z50}$  Applications of differential geometry to data and computer science
- 53Z99 None of the above, but in this section

# 54-XX General topology {For the topology of manifolds of all dimensions, see 57Nxx}

- **54-00** General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to general topology
- 54-01 Introductory exposition (textbooks, tutorial papers, etc.) pertaining to general topology
- **54-02** Research exposition (monographs, survey articles) pertaining to general topology
- ${\bf 54\text{-}03}$  History of general topology [Consider also classification numbers pertaining to Section 01]
- ${f 54\text{-}04}$  Software, source code, etc. for problems pertaining to general topology
- ${\bf 54\text{-}06}$  Proceedings, conferences, collections, etc. pertaining to general topology
- **54-08** Computational methods for problems pertaining to general topology
- **54-11** Research data for problems pertaining to general topology

#### 54Axx Generalities in topology

- ${f 54A05}$  Topological spaces and generalizations (closure spaces, etc.)
- **54A10** Several topologies on one set (change of topology, comparison of topologies, lattices of topologies)
- **54A15** Syntopogeneous structures
- **54A20** Convergence in general topology (sequences, filters, limits, convergence spaces, nets, etc.)

- $\bf 54A25$  Cardinality properties (cardinal functions and inequalities, discrete subsets) [See also 03Exx] {For ultrafilters, see 54D80}
- **54A35** Consistency and independence results in general topology [See also 03E35]
- **54A40** Fuzzy topology [See also 03E72]
- 54A99 None of the above, but in this section

## 54Bxx Basic constructions in general topology

- 54B05 Subspaces in general topology
- **54B10** Product spaces in general topology
- **54B15** Quotient spaces, decompositions in general topology
- 54B17 Adjunction spaces and similar constructions in general topology
- 54B20 Hyperspaces in general topology
- 54B30 Categorical methods in general topology [See also 18F60]
- 54B35 Spectra in general topology
- 54B40 Presheaves and sheaves in general topology [See also 18F20]
- ${\bf 54B99}$  None of the above, but in this section

# 54Cxx Maps and general types of topological spaces defined by maps

- **54C05** Continuous maps
- **54C08** Weak and generalized continuity
- 54C10 Special maps on topological spaces (open, closed, perfect, etc.)
- 54C15 Retraction
- **54C20** Extension of maps
- 54C25 Embedding
- **54C30** Real-valued functions in general topology [See also 26-XX]
- 54C35 Function spaces in general topology [See also 46Exx, 58D15]
- $\bf 54C40$  Algebraic properties of function spaces in general topology [See also  $\bf 46J10$ ]
- **54C45** C- and C\*-embedding
- 54C50 Topology of special sets defined by functions [See also 26A21]
- $\bf 54C55$  Absolute neighborhood extensor, absolute extensor, absolute neighborhood retract (ANR), absolute retract spaces (general properties) [See also 55M15]
- **54C56** Shape theory in general topology [See also 55P55, 57N25]
- 54C60 Set-valued maps in general topology [See also 26E25, 28B20, 47H04, 58C06]
- **54C65** Selections in general topology [See also 28B20]
- **54C70** Entropy in general topology
- 54C99 None of the above, but in this section

# 54Dxx Fairly general properties of topological spaces

- **54D05** Connected and locally connected spaces (general aspects)
- **54D10** Lower separation axioms  $(T_0-T_3, \text{ etc.})$
- **54D15** Higher separation axioms (completely regular, normal, perfectly or collectionwise normal, etc.)
- 54D20 Noncompact covering properties (paracompact, Lindelöf, etc.)
- **54D25** "P-minimal" and "P-closed" spaces
- 54D30 Compactness
- **54D35** Extensions of spaces (compactifications, supercompactifications, completions, etc.)
- 54D40 Remainders in general topology
- **54D45** Local compactness,  $\sigma$ -compactness
- 54D50 k-spaces
- **54D55** Sequential spaces
- 54D60 Realcompactness and realcompactification
- 54D65 Separability of topological spaces
- 54D70 Base properties of topological spaces
- **54D80** Special constructions of topological spaces (spaces of ultrafilters, etc.)
- 54D99 None of the above, but in this section

## 54Exx Topological spaces with richer structures

- ${\bf 54E05}$  Proximity structures and generalizations
- 54E15 Uniform structures and generalizations
- **54E17** Nearness spaces
- **54E18** *p*-spaces, M-spaces,  $\sigma$ -spaces, etc.
- **54E20** Stratifiable spaces, cosmic spaces, etc.
- **54E25** Semimetric spaces
- **54E30** Moore spaces
- **54E35** Metric spaces, metrizability
- **54E40** Special maps on metric spaces
- 54E45 Compact (locally compact) metric spaces
- **54E50** Complete metric spaces
- 54E52 Baire category, Baire spaces
- ${\bf 54E55}$  Bitopologies
- **54E70** Probabilistic metric spaces
- **54E99** None of the above, but in this section

#### 54Fxx Special properties of topological 54Jxx Nonstandard topology [See also spaces

- 54F05 Linearly ordered topological spaces, generalized ordered spaces, and partially ordered spaces [See also 06B30, 06F30
- **54F15** Continua and generalizations
- **54F16** Hyperspaces of continua
- **54F17** Inverse limits of set-valued functions
- 54F35 Higher-dimensional local connectedness [See also 55Mxx, 55Nxx
- 54F45 Dimension theory in general topology [See also 55M10
- **54F50** Topological spaces of dimension  $\leq 1$ ; curves, dendrites [See also 26A03]
- **54F55** Unicoherence, multicoherence
- **54F65** Topological characterizations of particular spaces
- 54F99 None of the above, but in this section

#### 54Gxx Peculiar topological spaces

- **54G05** Extremally disconnected spaces, F-spaces, etc.
- 54G10 P-spaces
- **54G12** Scattered spaces
- 54G15 Pathological topological spaces
- **54G20** Counterexamples in general topology
- 54G99 None of the above, but in this section

#### 54Hxx Connections of general topology with other structures, applications

- **54H05** Descriptive set theory (topological aspects of Borel, analytic, projective, etc. sets) [See also 03E15, 26A21, 28A05]
- **54H10** Topological representations of algebraic systems [See also 22-XX]
- **54H11** Topological groups (topological aspects) [See also 22A05
- **54H12** Topological lattices, etc. (topological aspects) [See also 06B30, 06F30]
- 54H13 Topological fields, rings, etc. (topological aspects) [See also 12Jxx] {For algebraic aspects, see 13Jxx, 16W80}
- 54H15 Transformation groups and semigroups (topological aspects) [See also 20M20, 22-XX, 57Sxx]
- 54H25 Fixed-point and coincidence theorems (topological aspects) [See also 47H10, 55M20]
- 54H30 Applications of general topology to computer science (e.g., digital topology, image processing) [See also 68U03
- 54H99 None of the above, but in this section

# 03H05

- **54J05** Nonstandard topology [See also 03H05]
- **54J99** None of the above, but in this section

#### 55-XX Algebraic topology

- **55-00** General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to algebraic topology
- 55-01 Introductory exposition (textbooks, tutorial papers, etc.) pertaining to algebraic topology
- 55-02 Research exposition (monographs, survey articles) pertaining to algebraic topology
- **55-03** History of algebraic topology [Consider also classification numbers pertaining to Section 01]
- 55-04 Software, source code, etc. for problems pertaining to algebraic topology
- 55-06 Proceedings, conferences, collections, etc. pertaining to algebraic topology
- **55-08** Computational methods for problems pertaining to algebraic topology
- 55-11 Research data for problems pertaining to algebraic topology

#### 55Mxx Classical topics in algebraic topology {For the topology of Euclidean spaces and manifolds, see 57Nxx}

- 55M05 Duality in algebraic topology
- 55M10 Dimension theory in algebraic topology [See also 54F45
- **55M15** Absolute neighborhood retracts [See also 54C55]
- 55M20 Fixed points and coincidences in algebraic topology [See also 54H25]
- 55M25 Degree, winding number
- **55M30** Lyusternik-Shnirel'man category of a space, topological complexity à la Farber, topological robotics (topological aspects)
- **55M35** Finite groups of transformations in algebraic topology (including Smith theory) [See also 57S17]
- 55M99 None of the above, but in this section

# 55Nxx Homology and cohomology theories in algebraic topology [See also 57Txx]

55N05 Čech types

55N07 Steenrod-Sitnikov homologies

 ${f 55N10}$  Singular homology and cohomology theory

**55N15** Topological K-theory [See also 19Lxx] {For algebraic K-theory, see 18F25, 19-XX}

**55N20** Generalized (extraordinary) homology and cohomology theories in algebraic topology

 $\bf 55N22$  Bordism and cobordism theories and formal group laws in algebraic topology [See also 14L05, 19L41, 57R75, 57R77, 57R85, 57R90]

55N25 Homology with local coefficients, equivariant cohomology

55N30 Sheaf cohomology in algebraic topology [See also  $18F20,\ 32C35,\ 32L10$ ]

55N31 Persistent homology and applications, topological data analysis [See also 62R40, 68T09]

55N32 Orbifold cohomology

**55N33** Intersection homology and cohomology in algebraic topology

55N34 Elliptic cohomology

55N35 Other homology theories in algebraic topology

**55N40** Axioms for homology theory and uniqueness theorems in algebraic topology

55N45 Products and intersections in homology and cohomology

55N91 Equivariant homology and cohomology in algebraic topology [See also 19L47]

55N99 None of the above, but in this section

# 55Pxx Homotopy theory {For simple homotopy type, see 57Q10}

 ${f 55P05}$  Homotopy extension properties, cofibrations in algebraic topology

**55P10** Homotopy equivalences in algebraic topology

**55P15** Classification of homotopy type

**55P20** Eilenberg-Mac Lane spaces

55P25 Spanier-Whitehead duality

**55P30** Eckmann-Hilton duality

**55P35** Loop spaces

55P40 Suspensions

55P42 Stable homotopy theory, spectra

**55P43** Spectra with additional structure  $(E_{\infty}, A_{\infty}, \text{ ring spectra, etc.})$ 

 ${f 55P45}$  H-spaces and duals

55P47 Infinite loop spaces

**55P48** Loop space machines and operads in algebraic topology [See also 18Mxx]

55P50 String topology

**55P55** Shape theory [See also 54C56, 55Q07]

**55P57** Proper homotopy theory

55P60 Localization and completion in homotopy theory

55P62 Rational homotopy theory

55P65 Homotopy functors in algebraic topology

**55P91** Equivariant homotopy theory in algebraic topology [See also 19L47]

**55P92** Relations between equivariant and nonequivariant homotopy theory in algebraic topology

55P99 None of the above, but in this section

#### 55Qxx Homotopy groups

55Q05 Homotopy groups, general; sets of homotopy classes

55Q07 Shape groups

55Q10 Stable homotopy groups

55Q15 Whitehead products and generalizations

55Q20 Homotopy groups of wedges, joins, and simple spaces

55Q25 Hopf invariants

55Q35 Operations in homotopy groups

55Q40 Homotopy groups of spheres

55Q45 Stable homotopy of spheres

**55Q50** *J*-morphism [See also 19L20]

**55Q51**  $v_n$ -periodicity

55Q52 Homotopy groups of special spaces

**55Q55** Cohomotopy groups

55Q70 Homotopy groups of special types [See also 55N05, 55N07]

**55Q91** Equivariant homotopy groups [See also 19L47]

55Q99 None of the above, but in this section

# 55Rxx Fiber spaces and bundles in algebraic topology [See also 18F15, 32Lxx, 46M20, 57R20, 57R22, 57R25]

55R05 Fiber spaces in algebraic topology

55R10 Fiber bundles in algebraic topology

 ${f 55R12}$  Transfer for fiber spaces and bundles in algebraic topology

 ${f 55R15}$  Classification of fiber spaces or bundles in algebraic topology

55R20 Spectral sequences and homology of fiber spaces in algebraic topology [See also 55Txx]

55R25 Sphere bundles and vector bundles in algebraic topology

 ${\bf 55R35}$  Classifying spaces of groups and  $H{\text{-}}{\text{spaces}}$  in algebraic topology

55R37 Maps between classifying spaces in algebraic topology

- **55R40** Homology of classifying spaces and characteristic classes in algebraic topology [See also 57Txx, 57R20]
- $55\mathbf{R}45$  Homology and homotopy of BO and BU; Bott periodicity
- **55R50** Stable classes of vector space bundles in algebraic topology and relations to K-theory [See also 19Lxx] {For algebraic K-theory, see 18F25, 19-XX}
- 55R55 Fiberings with singularities in algebraic topology
- **55R60** Microbundles and block bundles in algebraic topology [See also 57N55, 57Q50]
- 55R65 Generalizations of fiber spaces and bundles in algebraic topology
- **55R70** Fibrewise topology
- 55R80 Discriminantal varieties and configuration spaces in algebraic topology
- **55R91** Equivariant fiber spaces and bundles in algebraic topology [See also 19L47]
- 55R99 None of the above, but in this section

## 55Sxx Operations and obstructions in algebraic topology

- 55S05 Primary cohomology operations in algebraic topology
- **55S10** Steenrod algebra
- 55S12 Dyer-Lashof operations
- ${f 55S15}$  Symmetric products and cyclic products in algebraic topology
- **55S20** Secondary and higher cohomology operations in algebraic topology
- **55S25** K-theory operations and generalized cohomology operations in algebraic topology [See also 19D55, 19Lxx]
- **55S30** Massey products
- 55S35 Obstruction theory in algebraic topology
- ${f 55S36}$  Extension and compression of mappings in algebraic topology
- 55S37 Classification of mappings in algebraic topology
- ${f 55S40}$  Sectioning fiber spaces and bundles in algebraic topology
- 55S45 Postnikov systems, k-invariants
- 55S91 Equivariant operations and obstructions in algebraic topology [See also 19L47]
- 55S99 None of the above, but in this section

# 55Txx Spectral sequences in algebraic topology [See also 18G40, 55R20]

- ${\bf 55T05}$  General theory of spectral sequences in algebraic topology
- **55T10** Serre spectral sequences
- 55T15 Adams spectral sequences
- **55T20** Eilenberg-Moore spectral sequences [See also 57T35]
- ${f 55T25}$  Generalized cohomology and spectral sequences in algebraic topology
- 55T99 None of the above, but in this section

# 55Uxx Applied homological algebra and category theory in algebraic topology [See also 18Gxx]

- 55U05 Abstract complexes in algebraic topology
- 55U10 Simplicial sets and complexes in algebraic topology
- 55U15 Chain complexes in algebraic topology
- 55U20 Universal coefficient theorems, Bockstein operator
- 55U25 Homology of a product, Künneth formula
- **55U30** Duality in applied homological algebra and category theory (aspects of algebraic topology)
- ${f 55U35}$  Abstract and axiomatic homotopy theory in algebraic topology
- ${f 55U40}$  Topological categories, foundations of homotopy theory
- 55U99 None of the above, but in this section

# 57-XX Manifolds and cell complexes {For complex manifolds, see 32Qxx}

- **57-00** General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to manifolds and cell complexes
- **57-01** Introductory exposition (textbooks, tutorial papers, etc.) pertaining to manifolds and cell complexes
- **57-02** Research exposition (monographs, survey articles) pertaining to manifolds and cell complexes
- **57-03** History of manifolds and cell complexes [Consider also classification numbers pertaining to Section 01]
- **57-04** Software, source code, etc. for problems pertaining to manifolds and cell complexes
- **57-06** Proceedings, conferences, collections, etc. pertaining to manifolds and cell complexes
- ${f 57\text{-}08}$  Computational methods for problems pertaining to manifolds and cell complexes
- ${f 57\text{-}11}$  Research data for problems pertaining to manifolds and cell complexes

#### 57Kxx Low-dimensional topology in spe- 57Nxx Topological manifolds cific dimensions

- 57K10 Knot theory
- 57K12 Generalized knots (virtual knots, welded knots, quandles, etc.)
- 57K14 Knot polynomials
- 57K16 Finite-type and quantum invariants, topological quantum field theories (TQFT)
- 57K18 Homology theories in knot theory (Khovanov, Heegaard-Floer, etc.)
- 57K20 2-dimensional topology (including mapping class groups of surfaces, Teichmüller theory, curve complexes,
- **57K30** General topology of 3-manifolds
- 57K31 Invariants of 3-manifolds (also skein modules; character varieties)
- **57K32** Hyperbolic 3-manifolds
- **57K33** Contact structures in 3 dimensions [See also 57R17]
- 57K35 Other geometric structures on 3-manifolds
- 57K40 General topology of 4-manifolds
- 57K41 Invariants of 4-manifolds (e.g., Donaldson and Seiberg-Witten invariants)
- **57K43** Symplectic structures in 4 dimensions [See also 57R17
- 57K45 Higher-dimensional knots and links
- 57K50 Low-dimensional manifolds of specific dimension 5 or higher
- 57K99 None of the above, but in this section

#### 57Mxx General low-dimensional topology

- **57M05** Fundamental group, presentations, free differential
- **57M07** Topological methods in group theory
- **57M10** Covering spaces and low-dimensional topology
- **57M12** Low-dimensional topology of special (e.g., branched) coverings
- 57M15 Relations of low-dimensional topology with graph theory [See also 05Cxx]
- 57M30 Wild embeddings
- 57M50 General geometric structures on low-dimensional manifolds
- 57M60 Group actions on manifolds and cell complexes in low
- 57M99 None of the above, but in this section

- 57N16 Geometric structures on manifolds of high or arbitrary dimension [See also 57M50]
- **57N17** Topology of topological vector spaces
- 57N20 Topology of infinite-dimensional manifolds [See also 58Bxx
- 57N25 Shapes (aspects of topological manifolds) [See also 54C56, 55P55, 55Q07
- **57N30** Engulfing in topological manifolds
- **57N35** Embeddings and immersions in topological manifolds
- 57N37 Isotopy and pseudo-isotopy
- 57N40 Neighborhoods of submanifolds
- 57N45 Flatness and tameness of topological manifolds
- **57N50**  $S^{n-1} \subset E^n$ , Schoenflies problem
- 57N55 Microbundles and block bundles [See also 55R60,
- 57N60 Cellularity in topological manifolds
- 57N65 Algebraic topology of manifolds
- 57N70 Cobordism and concordance in topological manifolds
- **57N75** General position and transversality
- **57N80** Stratifications in topological manifolds
- 57N99 None of the above, but in this section

#### 57Pxx Generalized manifolds [See also 18F15

- 57P05 Local properties of generalized manifolds
- 57P10 Poincaré duality spaces
- 57P99 None of the above, but in this section

#### 57Qxx PL-topology

- 57Q05 General topology of complexes
- **57Q10** Simple Whitehead homotopy type. torsion. Reidemeister-Franz torsion, etc. [See also 19B28]
- **57Q12** Wall finiteness obstruction for CW-complexes
- 57Q15 Triangulating manifolds
- **57Q20** Cobordism in PL-topology
- **57Q25** Comparison of PL-structures: classification, Hauptvermutung
- 57Q30 Engulfing
- **57Q35** Embeddings and immersions in PL-topology
- **57Q37** Isotopy in PL-topology
- 57Q40 Regular neighborhoods in PL-topology
- **57Q50** Microbundles and block bundles [See also 55R60, 57N551
- **57Q55** Approximations in PL-topology
- **57Q60** Cobordism and concordance in PL-topology

- 57Q65 General position and transversality
- 57Q70 Discrete Morse theory and related ideas in manifold topology
- 57Q91 Equivariant PL-topology
- 57Q99 None of the above, but in this section

# 57Rxx Differential topology {For foundational questions of differentiable manifolds, see 58Axx; for infinite-dimensional manifolds, see 58Bxx}

- 57R05 Triangulating
- **57R10** Smoothing in differential topology
- **57R12** Smooth approximations in differential topology
- ${f 57R15}$  Specialized structures on manifolds (spin manifolds, framed manifolds, etc.)
- 57R17 Symplectic and contact topology in high or arbitrary dimension [See also 57K33, 57K43]
- **57R18** Topology and geometry of orbifolds
- 57R19 Algebraic topology on manifolds and differential topology
- 57R20 Characteristic classes and numbers in differential topology
- 57R22 Topology of vector bundles and fiber bundles [See also 55Rxx]
- 57R25 Vector fields, frame fields in differential topology
- **57R27** Controllability of vector fields on  $C^{\infty}$  and real-analytic manifolds [See also 49Qxx, 37C10, 93B05]
- 57R30 Foliations in differential topology; geometric theory [See also 53C12]
- 57R32 Classifying spaces for foliations; Gelfand-Fuks cohomology [See also 58H10]
- **57R35** Differentiable mappings in differential topology
- 57R40 Embeddings in differential topology
- **57R42** Immersions in differential topology
- ${f 57R45}$  Singularities of differentiable mappings in differential topology
- **57R50** Differential topological aspects of diffeomorphisms
- **57R52** Isotopy in differential topology
- **57R55** Differentiable structures in differential topology
- **57R56** Topological quantum field theories (aspects of differential topology)
- $\bf 57R57$  Applications of global analysis to structures on manifolds [See also  $\bf 57K41,\, 58\text{-}XX]$
- **57R58** Floer homology
- 57R60 Homotopy spheres, Poincaré conjecture
- **57R65** Surgery and handlebodies
- 57R67 Surgery obstructions, Wall groups [See also 19J25]

- 57R70 Critical points and critical submanifolds in differential topology
- 57R75 O- and SO-cobordism
- 57R77 Complex cobordism (U- and SU-cobordism) [See also 55N22]
- 57R80 h- and s-cobordism
- 57R85 Equivariant cobordism
- **57R90** Other types of cobordism [See also 55N22]
- 57R91 Equivariant algebraic topology of manifolds
- **57R95** Realizing cycles by submanifolds
- 57R99 None of the above, but in this section

# 57Sxx Topological transformation groups [See also 20F34, 22-XX, 37-XX, 54H15, 58D05]

- 57S05 Topological properties of groups of homeomorphisms or diffeomorphisms
- **57S10** Compact groups of homeomorphisms
- **57S12** Toric topology
- 57S15 Compact Lie groups of differentiable transformations
- **57S17** Finite transformation groups
- 57S20 Noncompact Lie groups of transformations
- 57S25 Groups acting on specific manifolds
- 57S30 Discontinuous groups of transformations
- 57S99 None of the above, but in this section

# 57Txx Homology and homotopy of topological groups and related structures

- 57T05 Hopf algebras (aspects of homology and homotopy of topological groups) [See also 16T05]
- **57T10** Homology and cohomology of Lie groups
- ${f 57T15}$  Homology and cohomology of homogeneous spaces of Lie groups
- **57T20** Homotopy groups of topological groups and homogeneous spaces
- 57T25 Homology and cohomology of H-spaces
- **57T30** Bar and cobar constructions [See also 18N40, 55Uxx]
- **57T35** Applications of Eilenberg-Moore spectral sequences [See also 55R20, 55T20]
- **57T99** None of the above, but in this section

# 57Zxx Relations of manifolds and cell complexes with science and engineering

- **57Z05** Relations of manifolds and cell complexes with physics
- 57Z10 Relations of manifolds and cell complexes with biology
- ${f 57Z15}$  Relations of manifolds and cell complexes with chemistry

- 57Z20 Relations of manifolds and cell complexes with engineering
- **57Z25** Relations of manifolds and cell complexes with computer and data science
- 57Z99 None of the above, but in this section

#### 58-XX Global analysis, analysis on manifolds [See also 32Cxx, 32Fxx, 32Wxx, 46-XX, 47Hxx, 53Cxx] {For geometric integration theory, see 49Q15}

- 58-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to global analysis
- **58-01** Introductory exposition (textbooks, tutorial papers, etc.) pertaining to global analysis
- **58-02** Research exposition (monographs, survey articles) pertaining to global analysis
- ${\bf 58\text{-}03}$  History of global analysis [Consider also classification numbers pertaining to Section 01]
- **58-04** Software, source code, etc. for problems pertaining to global analysis
- **58-06** Proceedings, conferences, collections, etc. pertaining to global analysis
- **58-08** Computational methods for problems pertaining to global analysis
- ${f 58\text{-}11}$  Research data for problems pertaining to global analysis

# 58Axx General theory of differentiable manifolds [See also 32Cxx]

- 58A03 Topos-theoretic approach to differentiable manifolds
- 58A05 Differentiable manifolds, foundations
- 58A07 Real-analytic and Nash manifolds [See also 14P20, 32C07]
- **58A10** Differential forms in global analysis
- **58A12** de Rham theory in global analysis [See also 14Fxx]
- **58A14** Hodge theory in global analysis [See also 14C30, 14Fxx, 32J25, 32S35]
- **58A15** Exterior differential systems (Cartan theory)
- **58A17** Pfaffian systems
- 58A20 Jets in global analysis
- 58A25 Currents in global analysis [See also 32C30, 53C65]
- 58A30 Vector distributions (subbundles of the tangent bundles)
- **58A32** Natural bundles
- **58A35** Stratified sets [See also 32S60]

- **58A40** Differential spaces
- 58A50 Supermanifolds and graded manifolds [See also  $14A22,\ 32C11$ ]
- **58A99** None of the above, but in this section

#### 58Bxx Infinite-dimensional manifolds

- ${f 58B05}$  Homotopy and topological questions for infinite-dimensional manifolds
- **58B10** Differentiability questions for infinite-dimensional manifolds
- 58B12 Questions of holomorphy and infinite-dimensional manifolds [See also 32-XX, 46G20]
- 58B15 Fredholm structures on infinite-dimensional manifolds [See also 47A53]
- 58B20 Riemannian, Finsler and other geometric structures on infinite-dimensional manifolds [See also 53C20, 53C60]
- 58B25 Group structures and generalizations on infinitedimensional manifolds [See also 22E65, 58D05]
- **58B32** Geometry of quantum groups
- 58B34 Noncommutative geometry (à la Connes)
- **58B99** None of the above, but in this section

# 58Cxx Calculus on manifolds; nonlinear operators [See also 46Txx, 47Hxx, 47Jxx]

- 58C05 Real-valued functions on manifolds
- 58C06 Set-valued and function-space-valued mappings on manifolds [See also 47H04, 54C60]
- 58C07 Continuity properties of mappings on manifolds
- **58C10** Holomorphic maps on manifolds [See also 32-XX]
- ${f 58C15}$  Implicit function theorems; global Newton methods on manifolds
- **58C20** Differentiation theory (Gateaux, Fréchet, etc.) on manifolds [See also 26Exx, 46G05]
- **58C25** Differentiable maps on manifolds
- **58C30** Fixed-point theorems on manifolds [See also 47H10]
- 58C35 Integration on manifolds; measures on manifolds [See also 28Cxx]
- **58C40** Spectral theory; eigenvalue problems on manifolds [See also 47J10, 58E07]
- 58C50 Analysis on supermanifolds or graded manifolds
- **58C99** None of the above, but in this section

# 58Dxx Spaces and manifolds of mappings (including nonlinear versions of 46Exx) [See also 46Txx, 53Cxx]

- 58D05 Groups of diffeomorphisms and homeomorphisms as manifolds [See also  $22E65,\,57805]$
- **58D07** Groups and semigroups of nonlinear operators [See also 17B65, 47H20]
- 58D10 Spaces of embeddings and immersions
- 58D15 Manifolds of mappings [See also 46T10, 54C35]
- **58D17** Manifolds of metrics (especially Riemannian)
- 58D19 Group actions and symmetry properties
- **58D20** Measures (Gaussian, cylindrical, etc.) on manifolds of maps [See also 28Cxx, 46T12]
- **58D25** Equations in function spaces; evolution equations [See also 34Gxx, 35K90, 35L90, 35R15, 37Lxx, 47Jxx]
- 58D27 Moduli problems for differential geometric structures
- **58D29** Moduli problems for topological structures
- 58D30 Applications of manifolds of mappings to the sciences
- 58D99 None of the above, but in this section

#### 58Exx Variational problems in infinitedimensional spaces

- **58E05** Abstract critical point theory (Morse theory, Lyusternik-Shnirel'man theory, etc.) in infinite-dimensional spaces
- **58E07** Variational problems in abstract bifurcation theory in infinite-dimensional spaces
- **58E09** Group-invariant bifurcation theory in infinite-dimensional spaces
- **58E10** Variational problems in applications to the theory of geodesics (problems in one independent variable)
- **58E11** Critical metrics
- $\bf 58E12$  Variational problems concerning minimal surfaces (problems in two independent variables) [See also 49Q05
- ${\bf 58E15}$  Variational problems concerning extremal problems in several variables; Yang-Mills functionals [See also  ${\bf 81T13}],$  etc.
- 58E17 Multiobjective variational problems, Pareto optimality, applications to economics, etc. [See also 90C29, 91Bxx]
- **58E20** Harmonic maps, etc. [See also 53C43]
- **58E25** Applications of variational problems to control theory [See also 49-XX, 93-XX]
- 58E30 Variational principles in infinite-dimensional spaces
- **58E35** Variational inequalities (global problems) in infinite-dimensional spaces
- ${f 58E40}$  Variational aspects of group actions in infinite-dimensional spaces
- ${f 58E50}$  Applications of variational problems in infinite-dimensional spaces to the sciences
- 58E99 None of the above, but in this section

# 58Hxx Pseudogroups, differentiable groupoids and general structures on manifolds

- **58H05** Pseudogroups and differentiable groupoids [See also 22A22, 22E65]
- **58H10** Cohomology of classifying spaces for pseudogroup structures (Spencer, Gelfand-Fuks, etc.) [See also 57R32]
- $58H15\,$  Deformations of general structures on manifolds [See also  $32{\rm Gxx},\,58{\rm J}10]$
- 58H99 None of the above, but in this section

#### 58Jxx Partial differential equations on manifolds; differential operators [See also 32Wxx, 35-XX, 53Cxx]

- **58J05** Elliptic equations on manifolds, general theory [See also 35-XX]
- **58J10** Differential complexes [See also 35Nxx]; elliptic complexes
- **58J15** Relations of PDEs on manifolds with hyperfunctions
- **58J20** Index theory and related fixed-point theorems on manifolds [See also 19K56, 46L80]
- **58J22** Exotic index theories on manifolds [See also 19K56, 46L05, 46L10, 46L80, 46M20]
- 58J26 Elliptic genera
- 58J28 Eta-invariants, Chern-Simons invariants
- 58J30 Spectral flows
- 58J32 Boundary value problems on manifolds
- **58J35** Heat and other parabolic equation methods for PDEs on manifolds
- 58J37 Perturbations of PDEs on manifolds; asymptotics
- **58J40** Pseudodifferential and Fourier integral operators on manifolds [See also 35Sxx]
- ${f 58J42}$  Noncommutative global analysis, noncommutative residues
- **58J45** Hyperbolic equations on manifolds [See also 35Lxx]
- ${f 58J47}$  Propagation of singularities; initial value problems on manifolds
- 58J50 Spectral problems; spectral geometry; scattering theory on manifolds [See also 35Pxx]
- ${f 58J51}$  Relations between spectral theory and ergodic theory, e.g., quantum unique ergodicity
- ${f 58J52}$  Determinants and determinant bundles, analytic torsion
- 58J53 Isospectrality

58J55 Bifurcation theory for PDEs on manifolds [See also 35B32]

**58J60** Relations of PDEs with special manifold structures (Riemannian, Finsler, etc.)

**58J65** Diffusion processes and stochastic analysis on manifolds [See also 35R60, 60H10, 60J60]

58J70 Invariance and symmetry properties for PDEs on manifolds [See also 35A30]

 $\bf 58J72$  Correspondences and other transformation methods (e.g., Lie-Bäcklund) for PDEs on manifolds [See also  $\bf 35A22$ ]

**58J90** Applications of PDEs on manifolds

58J99 None of the above, but in this section

# 58Kxx Theory of singularities and catastrophe theory [See also 32Sxx, 37-XX]

58K05 Critical points of functions and mappings on manifolds

58K10 Monodromy on manifolds

58K15 Topological properties of mappings on manifolds

58K20 Algebraic and analytic properties of mappings on manifolds

58K25 Stability theory for manifolds

58K30 Global theory of singularities

**58K35** Catastrophe theory

58K40 Classification; finite determinacy of map germs

 $\mathbf{58K45}$  Singularities of vector fields, topological aspects

58K50 Normal forms on manifolds

 ${f 58K55}$  Asymptotic behavior of solutions to equations on manifolds

58K60 Deformation of singularities

58K65 Topological invariants on manifolds

58K70 Symmetries, equivariance on manifolds

58K99 None of the above, but in this section

## 58Zxx Applications of global analysis to the sciences

58Z05 Applications of global analysis to the sciences

**58Z99** None of the above, but in this section

60-XX Probability theory and stochastic processes {For additional applications, see 05Cxx, 11Kxx, 34-XX, 35-XX, 62-XX, 90-XX, 76-XX, 81-XX, 82-XX, 91-XX, 92-XX, 93-XX, 94-XX}

**60-00** General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to probability theory

**60-01** Introductory exposition (textbooks, tutorial papers, etc.) pertaining to probability theory

**60-02** Research exposition (monographs, survey articles) pertaining to probability theory

60-03 History of probability theory [Consider also classification numbers pertaining to Section 01]

**60-04** Software, source code, etc. for problems pertaining to probability theory

**60-06** Proceedings, conferences, collections, etc. pertaining to probability theory

**60-08** Computational methods for problems pertaining to probability theory

**60-11** Research data for problems pertaining to probability theory

#### 60Axx Foundations of probability theory

60A05 Axioms; other general questions in probability

60A10 Probabilistic measure theory {For ergodic theory, see 28Dxx, 60Fxx}

60A86 Fuzzy probability

60A99 None of the above, but in this section

# 60Bxx Probability theory on algebraic and topological structures

60B05 Probability measures on topological spaces

60B10 Convergence of probability measures

 $\bf 60B11$  Probability theory on linear topological spaces [See also 28C20]

 ${\bf 60B12}$  Limit theorems for vector-valued random variables (infinite-dimensional case)

**60B15** Probability measures on groups or semigroups, Fourier transforms, factorization

**60B20** Random matrices (probabilistic aspects) {For algebraic aspects, see 15B52}

60B99 None of the above, but in this section

#### 60Cxx Combinatorial probability

60C05 Combinatorial probability

60C99 None of the above, but in this section

# 60Dxx Geometric probability and stochastic geometry [See also 52A22, 53C65]

**60D05** Geometric probability and stochastic geometry [See also 52A22, 53C65]

60D99 None of the above, but in this section

# 60Exx Distribution theory [See also 62Exx, 62Hxx]

- 60E05 Probability distributions: general theory
- 60E07 Infinitely divisible distributions; stable distributions
- ${f 60E10}$  Characteristic functions; other transforms
- 60E15 Inequalities; stochastic orderings
- 60E99 None of the above, but in this section

# 60Fxx Limit theorems in probability theory [See also 28Dxx, 60B12]

- 60F05 Central limit and other weak theorems
- 60F10 Large deviations
- 60F15 Strong limit theorems
- 60F17 Functional limit theorems; invariance principles
- 60F20 Zero-one laws
- **60F25**  $L^p$ -limit theorems
- 60F99 None of the above, but in this section

#### 60Gxx Stochastic processes

- 60G05 Foundations of stochastic processes
- 60G07 General theory of stochastic processes
- 60G09 Exchangeability for stochastic processes
- 60G10 Stationary stochastic processes
- 60G12 General second-order stochastic processes
- 60G15 Gaussian processes
- **60G17** Sample path properties
- 60G18 Self-similar stochastic processes
- 60G20 Generalized stochastic processes
- **60G22** Fractional processes, including fractional Brownian motion
- **60G25** Prediction theory (aspects of stochastic processes) [See also 62M20]
- 60G30 Continuity and singularity of induced measures
- 60G35 Signal detection and filtering (aspects of stochastic processes) [See also 62M20, 93E10, 93E11, 94Axx]
- $60G40\,$  Stopping times; optimal stopping problems; gambling theory [See also 62L15, 91A60]
- 60G42 Martingales with discrete parameter
- 60G44 Martingales with continuous parameter
- 60G46 Martingales and classical analysis
- 60G48 Generalizations of martingales
- 60G50 Sums of independent random variables; random walks
- ${f 60G51}$  Processes with independent increments; Lévy processes
- 60G52 Stable stochastic processes

- 60G53 Feller processes
- **60G55** Point processes (e.g., Poisson, Cox, Hawkes processes)
- 60G57 Random measures
- 60G60 Random fields
- $\bf 60G65$  Nonlinear processes (e.g.,  $\it G\textsubscript{-Brownian}$  motion,  $\it G\textsubscript{-L\'evy}$  processes)
- 60G70 Extreme value theory; extremal stochastic processes
- 60G99 None of the above, but in this section

#### 60Hxx Stochastic analysis [See also 58J65]

- 60H05 Stochastic integrals
- 60H07 Stochastic calculus of variations and the Malliavin calculus
- **60H10** Stochastic ordinary differential equations (aspects of stochastic analysis) [See also 34F05]
- 60H15 Stochastic partial differential equations (aspects of stochastic analysis) [See also 35R60]
- 60H17 Singular stochastic partial differential equations
- 60H20 Stochastic integral equations
- **60H25** Random operators and equations (aspects of stochastic analysis) [See also 47B80]
- 60H30 Applications of stochastic analysis (to PDEs, etc.)
- **60H35** Computational methods for stochastic equations (aspects of stochastic analysis) [See also 65C30]
- 60H40 White noise theory
- 60H50 Regularization by noise
- 60H99 None of the above, but in this section

#### 60Jxx Markov processes

- ${f 60J05}$  Discrete-time Markov processes on general state spaces
- **60J10** Markov chains (discrete-time Markov processes on discrete state spaces)
- **60J20** Applications of Markov chains and discrete-time Markov processes on general state spaces (social mobility, learning theory, industrial processes, etc.) [See also 90B30, 91D10, 91E40]
- **60J22** Computational methods in Markov chains [See also 65C40]
- ${f 60J25}$  Continuous-time Markov processes on general state spaces
- ${f 60J27}$  Continuous-time Markov processes on discrete state spaces
- **60J28** Applications of continuous-time Markov processes on discrete state spaces
- **60J35** Transition functions, generators and resolvents [See also 47D03, 47D07]
- 60J40 Right processes
- 60J45 Probabilistic potential theory [See also 31Cxx, 31D05]
- 60J46 Dirichlet form methods in Markov processes

- 60J50 Boundary theory for Markov processes
- 60J55 Local time and additive functionals
- 60J57 Multiplicative functionals and Markov processes
- 60J60 Diffusion processes [See also 58J65]
- 60J65 Brownian motion [See also 58J65]
- 60J67 Stochastic (Schramm-)Loewner evolution (SLE)
- 60J68 Superprocesses
- 60J70 Applications of Brownian motions and diffusion theory (population genetics, absorption problems, etc.) [See also 92Dxx]
- 60J75 Jump processes on discrete state spaces
- 60J76 Jump processes on general state spaces
- **60J80** Branching processes (Galton-Watson, birth-and-death, etc.)
- 60J85 Applications of branching processes [See also 92Dxx]
- 60J90 Coalescent processes
- **60J95** Applications of coalescent processes [See also 92Dxx]
- 60J99 None of the above, but in this section

#### 60Kxx Special processes

- 60K05 Renewal theory
- **60K10** Applications of renewal theory (reliability, demand theory, etc.)
- 60K15 Markov renewal processes, semi-Markov processes
- **60K20** Applications of Markov renewal processes (reliability, queueing networks, etc.) [See also 90Bxx]
- 60K25 Queueing theory (aspects of probability theory) [See also  $68M20,\ 90B22$ ]
- 60K30 Applications of queueing theory (congestion, allocation, storage, traffic, etc.) [See also 90Bxx]
- 60K35 Interacting random processes; statistical mechanics type models; percolation theory [See also 82B43, 82C43]
- 60K37 Processes in random environments
- 60K40 Other physical applications of random processes
- $\bf 60K50$  Anomalous diffusion models (subdiffusion, superdiffusion, continuous-time random walks, etc.) [See also  $\bf 60G22,\, 60G55,\, 60J75]$  {For applications to physics and the sciences, see 76-XX, 82Cxx, 92-XX}
- 60K99 None of the above, but in this section

#### 60Lxx Rough analysis

- 60L10 Signatures and data streams
- 60L20 Rough paths
- 60L30 Regularity structures
- **60L40** Paracontrolled distributions and alternative approaches
- ${f 60L50}$  Rough partial differential equations
- 60L70 Algebraic structures and computation
- 60L90 Applications of rough analysis
- 60L99 None of the above, but in this section

#### 62-XX Statistics

- **62-00** General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to statistics
- **62-01** Introductory exposition (textbooks, tutorial papers, etc.) pertaining to statistics
- **62-02** Research exposition (monographs, survey articles) pertaining to statistics
- **62-03** History of statistics [Consider also classification numbers pertaining to Section 01]
- **62-04** Software, source code, etc. for problems pertaining to statistics
- **62-06** Proceedings, conferences, collections, etc. pertaining to statistics
- $\mathbf{62\text{-}08}$  Computational methods for problems pertaining to statistics
- ${f 62\text{-}11}$  Research data for problems pertaining to statistics

## 62Axx Foundational and philosophical topics in statistics

- 62A01 Foundations and philosophical topics in statistics
- 62A09 Graphical methods
- 62A86 Fuzzy analysis in statistics
- 62A99 None of the above, but in this section

#### 62Bxx Sufficiency and information

- 62B05 Sufficient statistics and fields
- ${f 62B10}$  Statistical aspects of information-theoretic topics [See also  ${f 94A17}$ ]
- **62B11** Information geometry (statistical aspects) {For differential geometric aspects, see 53B12}
- 62B15 Theory of statistical experiments
- **62B86** Statistical aspects of fuzziness, sufficiency, and information
- 62B99 None of the above, but in this section

# 62Cxx Statistical decision theory [See also 90B50, 91B06] {For game theory, see 91A35]

- 62C05 General considerations in statistical decision theory
- 62C07 Complete class results in statistical decision theory
- 62C10 Bayesian problems; characterization of Bayes procedures
- ${f 62C12}$  Empirical decision procedures; empirical Bayes procedures
- 62C15 Admissibility in statistical decision theory
- 62C20 Minimax procedures in statistical decision theory
- **62C25** Compound decision problems in statistical decision theory
- 62C86 Statistical decision theory and fuzziness
- 62C99 None of the above, but in this section

#### 62Dxx Statistical sampling theory, sample 62Hxx Multivariate analysis [See also 60Exx surveys 62D05 Sampling theory, sample surveys 62H05 Characterization and structure theory for multivariate probability distributions; copulas 62D10 Missing data **62D20** Causal inference from observational studies 62H10 Multivariate distribution of statistics 62D99 None of the above, but in this section 62H11 Directional data; spatial statistics 62H12 Estimation in multivariate analysis 62Exx Statistical distribution theory [See 62H15 Hypothesis testing in multivariate analysis also 60Exx 62H17 Contingency tables 62E10 Characterization and structure theory of statistical distributions 62H20 Measures of association (correlation, canonical corre-**62E15** Exact distribution theory in statistics lation, etc.) **62E17** Approximations to statistical distributions 62H22 Probabilistic graphical models (nonasymptotic) 62H25 Factor analysis and principal components; correspon-**62E20** Asymptotic distribution theory in statistics dence analysis 62E86 Fuzziness in connection with statistical distributions 62H30 Classification and discrimination; cluster analysis 62E99 None of the above, but in this section (statistical aspects) [See also 68T10, 91C20]; mixture models 62Fxx Parametric inference 62H35 Image analysis in multivariate analysis **62F03** Parametric hypothesis testing 62H86 Multivariate analysis and fuzziness 62F05 Asymptotic properties of parametric tests 62H99 None of the above, but in this section 62F07 Statistical ranking and selection procedures **62F10** Point estimation 62Jxx Linear inference, regression 62F12 Asymptotic properties of parametric estimators 62J02 General nonlinear regression **62F15** Bayesian inference **62F25** Parametric tolerance and confidence regions 62J05 Linear regression; mixed models 62F30 Parametric inference under constraints **62J07** Ridge regression; shrinkage estimators (Lasso) **62F35** Robustness and adaptive procedures (parametric in-**62J10** Analysis of variance and covariance (ANOVA) 62J12 Generalized linear models (logistic models) 62F40 Bootstrap, jackknife and other resampling methods 62F86 Parametric inference and fuzziness 62J15 Paired and multiple comparisons; multiple testing 62F99 None of the above, but in this section 62J20 Diagnostics, and linear inference and regression 62J86 Fuzziness, and linear inference and regression 62Gxx Nonparametric inference 62J99 None of the above, but in this section 62G05 Nonparametric estimation 62G07 Density estimation 62Kxx Design of statistical experiments 62G08 Nonparametric regression and quantile regression [See also 05Bxx] 62G09 Nonparametric statistical resampling methods 62K05 Optimal statistical designs **62G10** Nonparametric hypothesis testing **62G15** Nonparametric tolerance and confidence regions 62K10 Statistical block designs 62G20 Asymptotic properties of nonparametric inference 62K15 Factorial statistical designs **62G30** Order statistics; empirical distribution functions 62K20 Response surface designs 62G32 Statistics of extreme values; tail inference 62K25 Robust parameter designs 62G35 Nonparametric robustness

62K86 Fuzziness and design of statistical experiments

62K99 None of the above, but in this section

62G86 Nonparametric inference and fuzziness62G99 None of the above, but in this section

#### 62Lxx Sequential statistical methods

- 62L05 Sequential statistical design
- 62L10 Sequential statistical analysis
- 62L12 Sequential estimation
- 62L15 Optimal stopping in statistics [See also 60G40, 91A60]
- 62L20 Stochastic approximation
- 62L86 Fuzziness and sequential statistical methods
- 62L99 None of the above, but in this section

#### 62Mxx Inference from stochastic processes

- 62M02 Markov processes: hypothesis testing
- 62M05 Markov processes: estimation; hidden Markov models
- 62M07 Non-Markovian processes: hypothesis testing
- 62M09 Non-Markovian processes: estimation
- **62M10** Time series, auto-correlation, regression, etc. in statistics (GARCH) [See also 91B84]
- ${f 62M15}$  Inference from stochastic processes and spectral analysis
- **62M20** Inference from stochastic processes and prediction [See also 60G25]; filtering [See also 60G35, 93E10, 93E11]
- 62M30 Inference from spatial processes
- 62M40 Random fields; image analysis
- ${\bf 62M45}$  Neural nets and related approaches to inference from stochastic processes
- 62M86 Inference from stochastic processes and fuzziness
- 62M99 None of the above, but in this section

#### 62Nxx Survival analysis and censored data

- 62N01 Censored data models
- 62N02 Estimation in survival analysis and censored data
- 62N03 Testing in survival analysis and censored data
- 62N05 Reliability and life testing [See also 90B25]
- 62N86 Fuzziness, and survival analysis and censored data
- 62N99 None of the above, but in this section

# 62Pxx Applications of statistics [See also 90-XX, 91-XX, 92-XX]

- **62P05** Applications of statistics to actuarial sciences and financial mathematics
- **62P10** Applications of statistics to biology and medical sciences; meta analysis
- ${f 62P12}$  Applications of statistics to environmental and related topics
- 62P15 Applications of statistics to psychology

- **62P20** Applications of statistics to economics [See also 91Bxx]
- 62P25 Applications of statistics to social sciences
- 62P30 Applications of statistics in engineering and industry; control charts
- **62P35** Applications of statistics to physics
- 62P99 None of the above, but in this section

#### 62Qxx Statistical tables

- 62Q05 Statistical tables
- 62Q99 None of the above, but in this section

# 62Rxx Statistics on algebraic and topological structures

- 62R01 Algebraic statistics
- 62R07 Statistical aspects of big data and data science {For computer science aspects, see 68T09; for information-theoretic aspects, see 94A16}
- 62R10 Functional data analysis
- 62R20 Statistics on metric spaces
- **62R30** Statistics on manifolds
- **62R40** Topological data analysis [See also 55N31]
- 62R99 None of the above, but in this section

#### 65-XX Numerical analysis

- 65-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to numerical analysis
- **65-01** Introductory exposition (textbooks, tutorial papers, etc.) pertaining to numerical analysis
- **65-02** Research exposition (monographs, survey articles) pertaining to numerical analysis
- 65-03 History of numerical analysis [Consider also classification numbers pertaining to Section 01]
- $\mathbf{65\text{-}04}$  Software, source code, etc. for problems pertaining to numerical analysis
- $\mathbf{65\text{-}06}$  Proceedings, conferences, collections, etc. pertaining to numerical analysis
- ${f 65\text{-}11}$  Research data for problems pertaining to numerical analysis

#### 65Axx Tables in numerical analysis

- 65A05 Tables in numerical analysis
- 65A99 None of the above, but in this section

# merical analysis

- 65B05 Extrapolation to the limit, deferred corrections
- 65B10 Numerical summation of series
- 65B15 Euler-Maclaurin formula in numerical analysis
- 65B99 None of the above, but in this section

#### 65Cxx Probabilistic methods, stochastic differential equations

- 65C05 Monte Carlo methods [See also 82M31]
- 65C10 Random number generation in numerical analysis [See also 11K45]
- 65C20 Probabilistic models, generic numerical methods in probability and statistics [See also 60-08, 62-08]
- 65C30 Numerical solutions to stochastic differential and integral equations {For theoretical aspects, see 60H35} [See also 65M75, 65N75]
- **65C35** Stochastic particle methods [See also 82M60]
- 65C40 Numerical analysis or methods applied to Markov chains [See also 60J22]
- 65C99 None of the above, but in this section

#### 65Dxx Numerical approximation computational geometry (primarily algorithms) {For theoretical aspects, see 41-XX, 68Uxx}

- 65D05 Numerical interpolation
- 65D07 Numerical computation using splines
- **65D10** Numerical smoothing, curve fitting
- 65D12 Numerical radial basis function approximation
- **65D15** Algorithms for approximation of functions
- 65D17 Computer-aided design (modeling of curves and surfaces) [See also 68U07]
- 65D18 Numerical aspects of computer graphics, image analysis, and computational geometry [See also 51N05, 68U05]
- 65D19 Computational issues in computer and robotic vision
- 65D20 Computation of special functions and constants, construction of tables [See also 33F05]
- 65D25 Numerical differentiation
- 65D30 Numerical integration
- 65D32 Numerical quadrature and cubature formulas
- 65D40 High-dimensional functions; sparse grids
- 65D99 None of the above, but in this section

#### 65Bxx Acceleration of convergence in nu- 65Exx Numerical methods in complex analysis (potential theory, etc.)

- 65E05 Numerical methods in complex analysis (potential theory, etc.) [See also 30-08, 31-08, 32-08]
- 65E10 Numerical methods in conformal mappings [See also 30C30
- 65E99 None of the above, but in this section

#### 65Fxx Numerical linear algebra

- 65F05 Direct numerical methods for linear systems and matrix inversion
- **65F08** Preconditioners for iterative methods
- 65F10 Iterative numerical methods for linear systems [See also 65N22]
- 65F15 Numerical computation of eigenvalues and eigenvectors of matrices
- 65F18 Numerical solutions to inverse eigenvalue problems
- **65F20** Numerical solutions to overdetermined systems, pseudoinverses
- 65F22 Ill-posedness and regularization problems in numerical linear algebra
- 65F25 Orthogonalization in numerical linear algebra
- 65F30 Other numerical matrix algorithms
- 65F35 Numerical computation of matrix norms, conditioning, scaling [See also 15A12, 15A60]
- 65F40 Numerical computation of determinants
- 65F45 Numerical methods for matrix equations
- 65F50 Computational methods for sparse matrices
- 65F55 Numerical methods for low-rank matrix approximation; matrix compression
- 65F60 Numerical computation of matrix exponential and similar matrix functions
- 65F99 None of the above, but in this section

#### 65Gxx Error analysis and interval analysis

- 65G20 Algorithms with automatic result verification
- 65G30 Interval and finite arithmetic
- 65G40 General methods in interval analysis
- 65G50 Roundoff error
- 65G99 None of the above, but in this section

#### 65Hxx Nonlinear algebraic or transcendental equations

- 65H04 Numerical computation of roots of polynomial equa-
- 65H05 Numerical computation of solutions to single equations

- ${\bf 65H10}$  Numerical computation of solutions to systems of equations
- 65H14 Numerical algebraic geometry
- 65H17 Numerical solution of nonlinear eigenvalue and eigenvector problems [See also 47Hxx, 47Jxx, 58C40, 58E07, 90C30]
- **65H20** Global methods, including homotopy approaches to the numerical solution of nonlinear equations [See also 58C30, 90C30]
- 65H99 None of the above, but in this section

### 65Jxx Numerical analysis in abstract spaces

- ${\bf 65J05}$  General theory of numerical analysis in abstract spaces
- 65J08 Numerical solutions to abstract evolution equations
- 65J10~ Numerical solutions to equations with linear operators (do not use 65Fxx)
- 65J15 Numerical solutions to equations with nonlinear operators (do not use 65Hxx)
- ${\bf 65J20}$  Numerical solutions of ill-posed problems in abstract spaces; regularization
- ${f 65J22}$  Numerical solution to inverse problems in abstract spaces
- 65J99 None of the above, but in this section

# 65Kxx Numerical methods for mathematical programming, optimization and variational techniques

- **65K05** Numerical mathematical programming methods [See also 90Cxx]
- **65K10** Numerical optimization and variational techniques [See also 49Mxx, 93-08]
- ${f 65K15}$  Numerical methods for variational inequalities and related problems
- 65K99 None of the above, but in this section

# 65Lxx Numerical methods for ordinary differential equations

- ${f 65L03}$  Numerical methods for functional-differential equations
- 65L04 Numerical methods for stiff equations
- 65L05 Numerical methods for initial value problems
- **65L06** Multistep, Runge-Kutta and extrapolation methods for ordinary differential equations
- 65L07 Numerical investigation of stability of solutions
- **65L08** Numerical solution of ill-posed problems involving ordinary differential equations

- **65L09** Numerical solution of inverse problems involving ordinary differential equations
- **65L10** Numerical solution of boundary value problems involving ordinary differential equations
- 65L11 Numerical solution of singularly perturbed problems involving ordinary differential equations
- 65L12 Finite difference and finite volume methods for ordinary differential equations
- **65L15** Numerical solution of eigenvalue problems involving ordinary differential equations
- **65L20** Stability and convergence of numerical methods for ordinary differential equations
- **65L50** Mesh generation, refinement, and adaptive methods for ordinary differential equations
- **65L60** Finite element, Rayleigh-Ritz, Galerkin and collocation methods for ordinary differential equations
- **65L70** Error bounds for numerical methods for ordinary differential equations
- ${f 65L80}$  Numerical methods for differential-algebraic equations
- 65L99 None of the above, but in this section

#### 65Mxx Numerical methods for partial differential equations, initial value and timedependent initial-boundary value problems

- **65M06** Finite difference methods for initial value and initial-boundary value problems involving PDEs
- 65M08 Finite volume methods for initial value and initialboundary value problems involving PDEs
- 65M12 Stability and convergence of numerical methods for initial value and initial-boundary value problems involving PDEs
- 65M15 Error bounds for initial value and initial-boundary value problems involving PDEs
- 65M20 Method of lines for initial value and initial-boundary value problems involving PDEs
- 65M22 Numerical solution of discretized equations for initial value and initial-boundary value problems involving PDEs [See also  $65\mathrm{Fxx},\,65\mathrm{Hxx}]$
- 65M25 Numerical aspects of the method of characteristics for initial value and initial-boundary value problems involving PDEs
- 65M30 Numerical methods for ill-posed problems for initial value and initial-boundary value problems involving PDEs
- 65M32 Numerical methods for inverse problems for initial value and initial-boundary value problems involving PDEs
- 65M38 Boundary element methods for initial value and initial-boundary value problems involving PDEs

- 65M50 Mesh generation, refinement, and adaptive methods for the numerical solution of initial value and initialboundary value problems involving PDEs
- 65M55 Multigrid methods; domain decomposition for initial value and initial-boundary value problems involving PDEs
- 65M60 Finite element, Rayleigh-Ritz and Galerkin methods for initial value and initial-boundary value problems involving PDEs
- **65M70** Spectral, collocation and related methods for initial value and initial-boundary value problems involving PDEs
- 65M75 Probabilistic methods, particle methods, etc. for initial value and initial-boundary value problems involving PDEs
- 65M80 Fundamental solutions, Green's function methods, etc. for initial value and initial-boundary value problems involving PDEs
- 65M85 Fictitious domain methods for initial value and initial-boundary value problems involving PDEs
- 65M99 None of the above, but in this section

#### 65Nxx Numerical methods for partial differential equations, boundary value problems

- 65N06 Finite difference methods for boundary value problems involving PDEs
- ${f 65N08}$  Finite volume methods for boundary value problems involving PDEs
- 65N12 Stability and convergence of numerical methods for boundary value problems involving PDEs
- ${f 65N15}$  Error bounds for boundary value problems involving PDEs
- 65N20 Numerical methods for ill-posed problems for boundary value problems involving PDEs
- ${f 65N21}$  Numerical methods for inverse problems for boundary value problems involving PDEs
- 65N22 Numerical solution of discretized equations for boundary value problems involving PDEs [See also 65Fxx, 65Hxx]
- 65N25 Numerical methods for eigenvalue problems for boundary value problems involving PDEs
- 65N30 Finite element, Rayleigh-Ritz and Galerkin methods for boundary value problems involving PDEs
- ${f 65N35}$  Spectral, collocation and related methods for boundary value problems involving PDEs
- **65N38** Boundary element methods for boundary value problems involving PDEs
- 65 N 40 Method of lines for boundary value problems involving PDEs

- **65N45** Method of contraction of the boundary for boundary value problems involving PDEs
- 65N50 Mesh generation, refinement, and adaptive methods for boundary value problems involving PDEs
- 65N55 Multigrid methods; domain decomposition for boundary value problems involving PDEs
- 65N75 Probabilistic methods, particle methods, etc. for boundary value problems involving PDEs
- 65N80 Fundamental solutions, Green's function methods, etc. for boundary value problems involving PDEs
- 65N85 Fictitious domain methods for boundary value problems involving PDEs
- 65N99 None of the above, but in this section

# 65Pxx Numerical problems in dynamical systems [See also 37Mxx]

- 65P10 Numerical methods for Hamiltonian systems including symplectic integrators
- 65P20 Numerical chaos
- 65P30 Numerical bifurcation problems
- 65P40 Numerical nonlinear stabilities in dynamical systems
- 65P99 None of the above, but in this section

# 65Qxx Numerical methods for difference and functional equations, recurrence relations

- 65Q10 Numerical methods for difference equations
- 65Q20 Numerical methods for functional equations
- 65Q30 Numerical aspects of recurrence relations
- 65Q99 None of the above, but in this section

# 65Rxx Numerical methods for integral equations, integral transforms

- 65R10 Numerical methods for integral transforms
- **65R15** Numerical methods for eigenvalue problems in integral equations
- ${f 65R20}$  Numerical methods for integral equations
- **65R30** Numerical methods for ill-posed problems for integral equations
- ${f 65R32}$  Numerical methods for inverse problems for integral equations
- 65R99 None of the above, but in this section

## 65Sxx Graphical methods in numerical analysis

- 65S05 Graphical methods in numerical analysis
- 65S99 None of the above, but in this section

#### 65Txx Numerical methods in Fourier anal- 68Mxx Computer system organization vsis

65T40 Numerical methods for trigonometric approximation and interpolation

65T50 Numerical methods for discrete and fast Fourier transforms

**65T60** Numerical methods for wavelets

65T99 None of the above, but in this section

#### 65Yxx Computer aspects of numerical algorithms

65Y04 Numerical algorithms for computer arithmetic, etc. [See also 68M07]

65Y05 Parallel numerical computation

65Y10 Numerical algorithms for specific classes of architec-

65Y15 Packaged methods for numerical algorithms

65Y20 Complexity and performance of numerical algorithms [See also 68Q25]

65Y99 None of the above, but in this section

#### 65Zxx Applications to the sciences

**65Z05** Applications to the sciences

65Z99 None of the above, but in this section

#### 68-XX Computer science {For papers containing software, source code, etc. in a specific mathematical area, see the classification number -04 in that area}

68-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to computer science

**68-01** Introductory exposition (textbooks, tutorial papers, etc.) pertaining to computer science

**68-02** Research exposition (monographs, survey articles) pertaining to computer science

68-03 History of computer science [Consider also classification numbers pertaining to Section 01]

68-04 Software, source code, etc. for problems pertaining to computer science

**68-06** Proceedings, conferences, collections, etc. pertaining to computer science

68-11 Research data for problems pertaining to computer science

**68M01** General theory of computer systems

68M07 Mathematical problems of computer architecture [See also 68W35]

**68M10** Network design and communication in computer systems [See also 68R10, 90B18]

**68M11** Internet topics [See also 68U35]

68M12 Network protocols

68M14 Distributed systems

68M15 Reliability, testing and fault tolerance of networks and computer systems

68M18 Wireless sensor networks as related to computer science [See also 90B18, 90B80]

68M20 Performance evaluation, queueing, and scheduling in the context of computer systems [See also 60K20, 60K25, 90B22, 90B35, 90B36

**68M25** Computer security

68M99 None of the above, but in this section

#### 68Nxx Theory of software

68N01 General topics in the theory of software

68N15 Theory of programming languages

68N17 Logic programming

68N18 Functional programming and lambda calculus [See also 03B40]

68N19 Other programming paradigms (object-oriented, sequential, concurrent, automatic, etc.)

68N20 Theory of compilers and interpreters

68N25 Theory of operating systems

**68N30** Mathematical aspects of software engineering (specification, verification, metrics, requirements, etc.)

68N99 None of the above, but in this section

#### 68Pxx Theory of data

68P01 General topics in the theory of data

68P05 Data structures

**68P10** Searching and sorting

68P15 Database theory

68P20 Information storage and retrieval of data

68P25 Data encryption (aspects in computer science) [See also 81P94, 94A60]

68P27 Privacy of data

68P30 Coding and information theory (compaction, compression, models of communication, encoding schemes, etc.) (aspects in computer science) [See also 94Axx, 94Bxx

68P99 None of the above, but in this section

#### 68Qxx Theory of computing

- 68Q01 General topics in the theory of computing
- **68Q04** Classical models of computation (Turing machines, etc.) [See also 03D10]
- 68Q06 Networks and circuits as models of computation; circuit complexity [See also 94C11]
- **68Q07** Biologically inspired models of computation (DNA computing, membrane computing, etc.)
- **68Q09** Other nonclassical models of computation {For quantum computing, see mainly 68Q12, 81P68}
- **68Q10** Modes of computation (nondeterministic, parallel, interactive, probabilistic, etc.) [See also 68Q85]
- 68Q11 Communication complexity, information complexity
- **68Q12** Quantum algorithms and complexity in the theory of computing [See also 68Q09, 81P68]
- **68Q15** Complexity classes (hierarchies, relations among complexity classes, etc.) [See also 03D15, 68Q17, 68Q19]
- 68Q17 Computational difficulty of problems (lower bounds, completeness, difficulty of approximation, etc.) [See also 68Q15]
- **68Q19** Descriptive complexity and finite models [See also 03C13]
- 68Q25 Analysis of algorithms and problem complexity [See also 68W40]
- 68Q27 Parameterized complexity, tractability and kerneliza-
- **68Q30** Algorithmic information theory (Kolmogorov complexity, etc.) [See also 03D32]
- **68Q32** Computational learning theory [See also 68T05]
- 68Q42 Grammars and rewriting systems
- 68Q45 Formal languages and automata [See also 03D05, 68Q70, 94A45]
- $\bf 68Q55$  Semantics in the theory of computing [See also 03B70, 06B35, 18C50]
- 68Q60 Specification and verification (program logics, model checking, etc.) [See also 03B70]
- 68Q65 Abstract data types; algebraic specification [See also 18C50]
- $68\mathbf{Q70}$  Algebraic theory of languages and automata [See also  $18\mathbf{B20},\ 20\mathbf{M35}$ ]
- 68Q80 Cellular automata (computational aspects) {For cellular automata as dynamical systems, see 37B15}
- 68Q85 Models and methods for concurrent and distributed computing (process algebras, bisimulation, transition nets, etc.)
- **68Q87** Probability in computer science (algorithm analysis, random structures, phase transitions, etc.) [See also  $68W20,\ 68W40$ ]
- 68Q99 None of the above, but in this section

## 68Rxx Discrete mathematics in relation to computer science

- 68R01 General topics of discrete mathematics in relation to computer science
- 68R05 Combinatorics in computer science
- $68\mathbf{R}07$  Computational aspects of satisfiability [See also  $68\mathbf{T}20$ ]
- 68R10 Graph theory (including graph drawing) in computer science [See also 05Cxx, 90B10, 90C35]
- **68R12** Metric embeddings as related to computational problems and algorithms
- 68R15 Combinatorics on words
- 68R99 None of the above, but in this section

#### 68Txx Artificial intelligence

- 68T01 General topics in artificial intelligence
- 68T05 Learning and adaptive systems in artificial intelligence [See also 68Q32]
- 68T07 Artificial neural networks and deep learning
- $\bf 68T09$  Computational aspects of data analysis and big data [See also 62R07] {For homological aspects, see  $55N31\}$
- **68T10** Pattern recognition, speech recognition {For cluster analysis, see 62H30}
- **68T20** Problem solving in the context of artificial intelligence (heuristics, search strategies, etc.)
- **68T27** Logic in artificial intelligence
- 68T30 Knowledge representation
- **68T35** Theory of languages and software systems (knowledge-based systems, expert systems, etc.) for artificial intelligence
- **68T37** Reasoning under uncertainty in the context of artificial intelligence
- 68T40 Artificial intelligence for robotics [See also 93C85]
- 68T42 Agent technology and artificial intelligence
- 68T45 Machine vision and scene understanding
- 68T50 Natural language processing [See also 03B65, 91F20]
- **68T99** None of the above, but in this section

# 68Uxx Computing methodologies and applications

- 68U01 General topics in computing methodologies
- **68U03** Computational aspects of digital topology {For topological aspects, see 54H30; for homological aspects, see 55-XX}
- **68U05** Computer graphics; computational geometry (digital and algorithmic aspects) {For methods of numerical mathematics, see 65D18}

- **68U07** Computer science aspects of computer-aided design {For methods of numerical mathematics, see 65D17}
- 68U10 Computing methodologies for image processing
- 68U15 Computing methodologies for text processing; mathematical typography
- **68U35** Computing methodologies for information systems (hypertext navigation, interfaces, decision support, etc.) [See also 68M11]
- 68U99 None of the above, but in this section

# 68Vxx Computer science support for mathematical research and practice

- 68V05 Computer assisted proofs of proofs-by-exhaustion type {For rigorous numerics, see 65Gxx; for proofs employing automated or interactive theorem provers, see  $68V15\}$
- 68V15 Theorem proving (automated and interactive theorem provers, deduction, resolution, etc.) [See also 03B35]
- $68V20\,$  Formalization of mathematics in connection with theorem provers [See also 03B35, 68V15]
- 68V25 Presentation and content markup for mathematics
- 68V30 Mathematical knowledge management
- 68V35 Digital mathematics libraries and repositories
- 68V99 None of the above, but in this section

# 68Wxx Algorithms in computer science {For numerical algorithms, see 65-XX; for combinatorics and graph theory, see 05C85, 68Rxx}

- 68W01 General topics in the theory of algorithms
- 68W05 Nonnumerical algorithms
- 68W10 Parallel algorithms in computer science
- 68W15 Distributed algorithms
- 68W20 Randomized algorithms
- 68W25 Approximation algorithms
- 68W27 Online algorithms; streaming algorithms
- $\bf 68W30$  Symbolic computation and algebraic computation [See also 11Yxx, 12-08, 13Pxx, 14Qxx, 16Z05, 17-08, 33F10]
- 68W32 Algorithms on strings
- 68W35 Hardware implementations of nonnumerical algorithms (VLSI algorithms, etc.) [See also 68M07]
- 68W40 Analysis of algorithms [See also 68Q25]
- 68W50 Evolutionary algorithms, genetic algorithms (computational aspects) [See also  $68T05,\,68T20,\,90C59$ ]
- 68W99 None of the above, but in this section

# 70-XX Mechanics of particles and systems {For relativistic mechanics, see 83A05, 83C10; for statistical mechanics, see 82-XX}

- **70-00** General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to mechanics of particles and systems
- **70-01** Introductory exposition (textbooks, tutorial papers, etc.) pertaining to mechanics of particles and systems
- 70-02 Research exposition (monographs, survey articles) pertaining to mechanics of particles and systems
- 70-03 History of mechanics of particles and systems [Consider also classification numbers pertaining to Section 01]
- **70-04** Software, source code, etc. for problems pertaining to mechanics of particles and systems
- **70-05** Experimental work for problems pertaining to mechanics of particles and systems
- **70-06** Proceedings, conferences, collections, etc. pertaining to mechanics of particles and systems
- 70-08 Computational methods for problems pertaining to mechanics of particles and systems
- **70-10** Mathematical modeling or simulation for problems pertaining to mechanics of particles and systems
- 70-11 Research data for problems pertaining to mechanics of particles and systems

#### 70Axx Axiomatics, foundations

- 70A05 Axiomatics, foundations
- 70A99 None of the above, but in this section

#### 70Bxx Kinematics [See also 53A17]

- 70B05 Kinematics of a particle
- 70B10 Kinematics of a rigid body
- **70B15** Kinematics of mechanisms and robots [See also 68T40, 70Q05, 93C85]
- 70B99 None of the above, but in this section

#### **70Cxx Statics**

- 70C20 Statics
- 70C99 None of the above, but in this section

#### 70Exx Dynamics of a rigid body and of 70G60 Dynamical systems methods for problems in mechanmultibody systems

**70E05** Motion of the gyroscope

**70E15** Free motion of a rigid body [See also 70M20]

70E17 Motion of a rigid body with a fixed point

**70E18** Motion of a rigid body in contact with a solid surface [See also 70F25]

70E20 Perturbation methods for rigid body dynamics

70E40 Integrable cases of motion in rigid body dynamics

70E45 Higher-dimensional generalizations in rigid body dy-

**70E50** Stability problems in rigid body dynamics

70E55 Dynamics of multibody systems

70E60 Robot dynamics and control of rigid bodies [See also 68T40, 70Q05, 93C85

**70E99** None of the above, but in this section

#### 70Fxx Dynamics of a system of particles, including celestial mechanics

70F05 Two-body problems

70F07 Three-body problems

**70F10** *n*-body problems

**70F15** Celestial mechanics

70F16 Collisions in celestial mechanics, regularization

70F17 Inverse problems for systems of particles

70F20 Holonomic systems related to the dynamics of a system of particles

70F25 Nonholonomic systems related to the dynamics of a system of particles

70F35 Collision of rigid or pseudo-rigid bodies

70F40 Problems involving a system of particles with friction

**70F45** The dynamics of infinite particle systems

70F99 None of the above, but in this section

#### 70Gxx General models, approaches, and methods [See also 37-XX]

70G10 Generalized coordinates; event, impulse-energy, configuration, state, or phase space for problems in mechanics

70G40 Topological and differential topological methods for problems in mechanics

70G45 Differential geometric methods (tensors, connections, symplectic, Poisson, contact, Riemannian, nonholonomic, etc.) for problems in mechanics [See also 53Cxx, 53Dxx, 58Axx]

70G55 Algebraic geometry methods for problems in mechanics

70G65 Symmetries, Lie group and Lie algebra methods for problems in mechanics

70G70 Functional analytic methods for problems in mechan-

**70G75** Variational methods for problems in mechanics

70G99 None of the above, but in this section

#### 70Hxx Hamiltonian and Lagrangian mechanics [See also 37Jxx]

70H03 Lagrange's equations

**70H05** Hamilton's equations

70H06 Completely integrable systems and methods of integration for problems in Hamiltonian and Lagrangian mechanics

70H07 Nonintegrable systems for problems in Hamiltonian and Lagrangian mechanics

70H08 Nearly integrable Hamiltonian systems, KAM theory

70H09 Perturbation theories for problems in Hamiltonian and Lagrangian mechanics

70H11 Adiabatic invariants for problems in Hamiltonian and Lagrangian mechanics

70H12 Periodic and almost periodic solutions for problems in Hamiltonian and Lagrangian mechanics

70H14 Stability problems for problems in Hamiltonian and Lagrangian mechanics

70H15 Canonical and symplectic transformations for problems in Hamiltonian and Lagrangian mechanics

70H20 Hamilton-Jacobi equations in mechanics

70H25 Hamilton's principle

70H30 Other variational principles in mechanics

70H33 Symmetries and conservation laws, reverse symmetries, invariant manifolds and their bifurcations, reduction for problems in Hamiltonian and Lagrangian me-

70H40 Relativistic dynamics for problems in Hamiltonian and Lagrangian mechanics

70H45 Constrained dynamics, Dirac's theory of constraints [See also 70F20, 70F25, 70Gxx]

70H50 Higher-order theories for problems in Hamiltonian and Lagrangian mechanics

70H99 None of the above, but in this section

#### 70Jxx Linear vibration theory

70J10 Modal analysis in linear vibration theory

70J25 Stability for problems in linear vibration theory

**70J30** Free motions in linear vibration theory

70J35 Forced motions in linear vibration theory

70J40 Parametric resonances in linear vibration theory

**70J50** Systems arising from the discretization of structural vibration problems

**70J99** None of the above, but in this section

## 70Kxx Nonlinear dynamics in mechanics [See also 34Cxx, 37-XX]

70 K 05 Phase plane analysis, limit cycles for nonlinear problems in mechanics

70K20 Stability for nonlinear problems in mechanics

70K25 Free motions for nonlinear problems in mechanics

70K28 Parametric resonances for nonlinear problems in mechanics

70K30 Nonlinear resonances for nonlinear problems in mechanics

70K40 Forced motions for nonlinear problems in mechanics

**70K42** Equilibria and periodic trajectories for nonlinear problems in mechanics

**70K43** Quasi-periodic motions and invariant tori for nonlinear problems in mechanics

70K44 Homoclinic and heteroclinic trajectories for nonlinear problems in mechanics

70K45 Normal forms for nonlinear problems in mechanics

70K50 Bifurcations and instability for nonlinear problems in mechanics

70K55 Transition to stochasticity (chaotic behavior) for non-linear problems in mechanics [See also 37D45]

70 K 60 General perturbation schemes for nonlinear problems in mechanics

**70K65** Averaging of perturbations for nonlinear problems in mechanics

70K70 Systems with slow and fast motions for nonlinear problems in mechanics

70K75 Nonlinear modes

70K99 None of the above, but in this section

#### 70Lxx Random and stochastic aspects of the mechanics of particles and systems

70L05 Random vibrations in mechanics of particles and systems [See also 74H50]

70L10 Stochastic geometric mechanics

70L99 None of the above, but in this section

#### 70Mxx Orbital mechanics

70M20 Orbital mechanics

70M99 None of the above, but in this section

#### 70Pxx Variable mass, rockets

70P05 Variable mass, rockets

70P99 None of the above, but in this section

# 70Qxx Control of mechanical systems [See also 60Gxx, 60Jxx]

70Q05 Control of mechanical systems

70Q99 None of the above, but in this section

# 70Sxx Classical field theories [See also 37Kxx, 37Lxx, 78-XX, 81Txx, 83-XX]

70S05 Lagrangian formalism and Hamiltonian formalism in mechanics of particles and systems

**70S10** Symmetries and conservation laws in mechanics of particles and systems

70S15 Yang-Mills and other gauge theories in mechanics of particles and systems

**70S20** More general nonquantum field theories in mechanics of particles and systems

**70S99** None of the above, but in this section

# 74-XX Mechanics of deformable solids

74-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to mechanics of deformable solids

**74-01** Introductory exposition (textbooks, tutorial papers, etc.) pertaining to mechanics of deformable solids

**74-02** Research exposition (monographs, survey articles) pertaining to mechanics of deformable solids

**74-03** History of mechanics of deformable solids [Consider also classification numbers pertaining to Section 01]

74-04 Software, source code, etc. for problems pertaining to mechanics of deformable solids

**74-05** Experimental work for problems pertaining to mechanics of deformable solids

**74-06** Proceedings, conferences, collections, etc. pertaining to mechanics of deformable solids

**74-10** Mathematical modeling or simulation for problems pertaining to mechanics of deformable solids

 ${\bf 74\text{-}11}\,$  Research data for problems pertaining to mechanics of deformable solids

# 74Axx Generalities, axiomatics, foundations of continuum mechanics of solids

**74A05** Kinematics of deformation

74A10 Stress

74A15 Thermodynamics in solid mechanics

74A20 Theory of constitutive functions in solid mechanics

74A25 Molecular, statistical, and kinetic theories in solid mechanics

**74A30** Nonsimple materials

74A35 Polar materials

74A40 Random materials and composite materials

74A45 Theories of fracture and damage

74A50 Structured surfaces and interfaces, coexistent phases

**74A55** Theories of friction (tribology)

**74A60** Micromechanical theories

**74A65** Reactive materials

74A70 Peridynamics

74A99 None of the above, but in this section

#### 74Bxx Elastic materials

74B05 Classical linear elasticity

74B10 Linear elasticity with initial stresses

**74B15** Equations linearized about a deformed state (small deformations superposed on large)

74B20 Nonlinear elasticity

74B99 None of the above, but in this section

## 74Cxx Plastic materials, materials of stress-rate and internal-variable type

**74C05** Small-strain, rate-independent theories of plasticity (including rigid-plastic and elasto-plastic materials)

74C10 Small-strain, rate-dependent theories of plasticity (including theories of viscoplasticity)

**74C15** Large-strain, rate-independent theories of plasticity (including nonlinear plasticity)

74C20 Large-strain, rate-dependent theories of plasticity

74C99 None of the above, but in this section

# 74Dxx Materials of strain-rate type and history type, other materials with memory (including elastic materials with viscous damping, various viscoelastic materials)

 ${\bf 74D05} \ \ {\bf Linear} \ {\bf constitutive} \ {\bf equations} \ {\bf for} \ {\bf materials} \ {\bf with} \ {\bf memory}$ 

74D10 Nonlinear constitutive equations for materials with memory

74D99 None of the above, but in this section

### 74Exx Material properties given special treatment

74E05 Inhomogeneity in solid mechanics

74E10 Anisotropy in solid mechanics

**74E15** Crystalline structure

74E20 Granularity

**74E25** Texture in solid mechanics

**74E30** Composite and mixture properties

74E35 Random structure in solid mechanics

**74E40** Chemical structure in solid mechanics

74E99 None of the above, but in this section

# 74Fxx Coupling of solid mechanics with other effects

74F05 Thermal effects in solid mechanics

**74F10** Fluid-solid interactions (including aero- and hydroelasticity, porosity, etc.)

**74F15** Electromagnetic effects in solid mechanics

**74F20** Mixture effects in solid mechanics

74F25 Chemical and reactive effects in solid mechanics

74F99 None of the above, but in this section

### 74Gxx Equilibrium (steady-state) problems in solid mechanics

74G05 Explicit solutions of equilibrium problems in solid mechanics

74G10 Analytic approximation of solutions (perturbation methods, asymptotic methods, series, etc.) of equilibrium problems in solid mechanics

74G15 Numerical approximation of solutions of equilibrium problems in solid mechanics

 ${\bf 74G25} \ \ {\bf Existence} \ {\bf of} \ {\bf solutions} \ {\bf of} \ {\bf equilibrium} \ {\bf problems} \ {\bf in} \ {\bf solid} \\ {\bf mechanics}$ 

74G30 Uniqueness of solutions of equilibrium problems in solid mechanics

74G35 Multiplicity of solutions of equilibrium problems in solid mechanics

**74G40** Regularity of solutions of equilibrium problems in solid mechanics

**74G45** Bounds for solutions of equilibrium problems in solid mechanics

 ${\bf 74G50} \ \ {\bf Saint-Venant's \ principle}$ 

74G55 Qualitative behavior of solutions of equilibrium problems in solid mechanics

**74G60** Bifurcation and buckling

**74G65** Energy minimization in equilibrium problems in solid mechanics

74G70 Stress concentrations, singularities in solid mechanics

74G75 Inverse problems in equilibrium solid mechanics

74G99 None of the above, but in this section

# 74Hxx Dynamical problems in solid mechanics

- 74H05 Explicit solutions of dynamical problems in solid mechanics
- **74H10** Analytic approximation of solutions (perturbation methods, asymptotic methods, series, etc.) of dynamical problems in solid mechanics
- **74H15** Numerical approximation of solutions of dynamical problems in solid mechanics
- 74H20 Existence of solutions of dynamical problems in solid mechanics
- **74H25** Uniqueness of solutions of dynamical problems in solid mechanics
- 74H30 Regularity of solutions of dynamical problems in solid mechanics
- **74H35** Singularities, blow-up, stress concentrations for dynamical problems in solid mechanics
- **74H40** Long-time behavior of solutions for dynamical problems in solid mechanics
- 74H45 Vibrations in dynamical problems in solid mechanics
- 74H50 Random vibrations in dynamical problems in solid mechanics
- **74H55** Stability of dynamical problems in solid mechanics
- **74H60** Dynamical bifurcation of solutions to dynamical problems in solid mechanics
- **74H65** Chaotic behavior of solutions to dynamical problems in solid mechanics
- 74H75 Inverse problems in dynamical solid mechanics
- **74H80** Energy minimization in dynamical problems in solid mechanics
- 74H99 None of the above, but in this section

#### 74Jxx Waves in solid mechanics

- **74J05** Linear waves in solid mechanics
- 74J10 Bulk waves in solid mechanics
- 74J15 Surface waves in solid mechanics
- 74J20 Wave scattering in solid mechanics
- 74J25 Inverse problems for waves in solid mechanics
- 74J30 Nonlinear waves in solid mechanics
- 74J35 Solitary waves in solid mechanics
- 74J40 Shocks and related discontinuities in solid mechanics
- 74J99 None of the above, but in this section

#### 74Kxx Thin bodies, structures

- 74K05 Strings
- 74K10 Rods (beams, columns, shafts, arches, rings, etc.)
- 74K15 Membranes

- 74K20 Plates
- 74K25 Shells
- 74K30 Junctions
- 74K35 Thin films
- 74K99 None of the above, but in this section

#### 74Lxx Special subfields of solid mechanics

- 74L05 Geophysical solid mechanics [See also 86-XX]
- 74L10 Soil and rock mechanics
- 74L15 Biomechanical solid mechanics [See also 92C10]
- 74L99 None of the above, but in this section

### 74Mxx Special kinds of problems in solid mechanics

- **74M05** Control, switches and devices ("smart materials") in solid mechanics [See also 93Cxx]
- 74M10 Friction in solid mechanics
- 74M15 Contact in solid mechanics
- 74M20 Impact in solid mechanics
- 74M25 Micromechanics of solids
- 74M99 None of the above, but in this section

# 74Nxx Phase transformations in solids [See also 74A50, 80Axx, 82B26, 82C26]

- **74N05** Crystals in solids
- 74N10 Displacive transformations in solids
- 74N15 Analysis of microstructure in solids
- 74N20 Dynamics of phase boundaries in solids
- 74N25 Transformations involving diffusion in solids
- **74N30** Problems involving hysteresis in solids
- 74N99 None of the above, but in this section

# 74Pxx Optimization problems in solid mechanics [See also 49Qxx]

- 74P05 Compliance or weight optimization in solid mechanics
- 74P10 Optimization of other properties in solid mechanics
- **74P15** Topological methods for optimization problems in solid mechanics
- **74P20** Geometrical methods for optimization problems in solid mechanics
- 74P99 None of the above, but in this section

#### 74Qxx Homogenization, determination of 76-01 Introductory exposition (textbooks, tutorial papers, effective properties in solid mechanics

- 74Q05 Homogenization in equilibrium problems of solid mechanics
- 74Q10 Homogenization and oscillations in dynamical problems of solid mechanics
- 74Q15 Effective constitutive equations in solid mechanics
- **74Q20** Bounds on effective properties in solid mechanics
- 74Q99 None of the above, but in this section

#### 74Rxx Fracture and damage

- 74R05 Brittle damage
- **74R10** Brittle fracture
- 74R15 High-velocity fracture
- 74R20 Anelastic fracture and damage
- 74R99 None of the above, but in this section

#### 74Sxx Numerical and other methods in solid mechanics [See also 65-XX, 74G15, 74H15

- 74S05 Finite element methods applied to problems in solid mechanics
- 74S10 Finite volume methods applied to problems in solid mechanics
- **74S15** Boundary element methods applied to problems in solid mechanics
- 74S20 Finite difference methods applied to problems in solid mechanics
- 74S22 Isogeometric methods applied to problems in solid me-
- **74S25** Spectral and related methods applied to problems in solid mechanics
- 74S30 Other numerical methods applied to problems in solid mechanics
- 74S40 Applications of fractional calculus in solid mechanics
- **74S50** Applications of graph theory in solid mechanics
- 74S60 Stochastic and other probabilistic methods applied to problems in solid mechanics
- 74S70 Complex-variable methods applied to problems in solid mechanics
- 74S99 None of the above, but in this section

#### 76-XX Fluid mechanics {For general continuum mechanics, see 74Axx, or other parts of 74-XX

76-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to fluid mechanics

- etc.) pertaining to fluid mechanics
- **76-02** Research exposition (monographs, survey articles) pertaining to fluid mechanics
- 76-03 History of fluid mechanics [Consider also classification numbers pertaining to Section 01]
- **76-04** Software, source code, etc. for problems pertaining to fluid mechanics
- 76-05 Experimental work for problems pertaining to fluid mechanics
- **76-06** Proceedings, conferences, collections, etc. pertaining to fluid mechanics
- 76-10 Mathematical modeling or simulation for problems pertaining to fluid mechanics
- **76-11** Research data for problems pertaining to fluid mechan-

#### 76Axx Foundations, constitutive equations, rheology, hydrodynamical models of non-fluid phenomena

- 76A02 Foundations of fluid mechanics
- 76A05 Non-Newtonian fluids
- 76A10 Viscoelastic fluids
- 76A15 Liquid crystals [See also 82D30]
- 76A20 Thin fluid films
- **76A25** Superfluids (classical aspects)
- **76A30** Traffic and pedestrian flow models
- 76A99 None of the above, but in this section

#### 76Bxx Incompressible inviscid fluids

- 76B03 Existence, uniqueness, and regularity theory for incompressible inviscid fluids [See also 35Q35]
- 76B07 Free-surface potential flows for incompressible inviscid fluids
- 76B10 Jets and cavities, cavitation, free-streamline theory, water-entry problems, airfoil and hydrofoil theory, sloshing
- 76B15 Water waves, gravity waves; dispersion and scattering, nonlinear interaction [See also 35Q30]
- 76B20 Ship waves
- 76B25 Solitary waves for incompressible inviscid fluids [See also 35C11]
- 76B45 Capillarity (surface tension) for incompressible inviscid fluids [See also 76D45]
- 76B47 Vortex flows for incompressible inviscid fluids
- 76B55 Internal waves for incompressible inviscid fluids
- 76B70 Stratification effects in inviscid fluids
- 76B75 Flow control and optimization for incompressible inviscid fluids [See also 49Q10, 93C20, 93C95]
- 76B99 None of the above, but in this section

#### 76Dxx Incompressible viscous fluids

**76D03** Existence, uniqueness, and regularity theory for incompressible viscous fluids [See also 35Q30]

**76D05** Navier-Stokes equations for incompressible viscous fluids [See also 35Q30]

**76D06** Statistical solutions of Navier-Stokes and related equations [See also 60H30, 76M35]

76D07 Stokes and related (Oseen, etc.) flows

**76D08** Lubrication theory

76D09 Viscous-inviscid interaction

**76D10** Boundary-layer theory, separation and reattachment, higher-order effects

**76D17** Viscous vortex flows

76D25 Wakes and jets

76D27 Other free boundary flows; Hele-Shaw flows

**76D33** Waves for incompressible viscous fluids

**76D45** Capillarity (surface tension) for incompressible viscous fluids [See also 76B45]

76D50 Stratification effects in viscous fluids

**76D55** Flow control and optimization for incompressible viscous fluids [See also 49Q10, 93C20, 93C95]

76D99 None of the above, but in this section

#### 76Exx Hydrodynamic stability

**76E05** Parallel shear flows in hydrodynamic stability

**76E06** Convection in hydrodynamic stability

76E07 Rotation in hydrodynamic stability

**76E09** Stability and instability of nonparallel flows in hydrodynamic stability

**76E15** Absolute and convective instability and stability in hydrodynamic stability

**76E17** Interfacial stability and instability in hydrodynamic

76E19 Compressibility effects in hydrodynamic stability

76E20 Stability and instability of geophysical and astrophysical flows

**76E25** Stability and instability of magnetohydrodynamic and electrohydrodynamic flows

**76E30** Nonlinear effects in hydrodynamic stability

**76E99** None of the above, but in this section

# 76Fxx Turbulence [See also 37-XX, 60Gxx, 60Jxx]

76F02 Fundamentals of turbulence

**76F05** Isotropic turbulence; homogeneous turbulence

76F06 Transition to turbulence

76F10 Shear flows and turbulence

**76F20** Dynamical systems approach to turbulence [See also 37-XX]

76F25 Turbulent transport, mixing

76F30 Renormalization and other field-theoretical methods for turbulence [See also 81T99]

76F35 Convective turbulence [See also 76E15, 76Rxx]

76F40 Turbulent boundary layers

**76F45** Stratification effects in turbulence

76F50 Compressibility effects in turbulence

**76F55** Statistical turbulence modeling [See also 76M35]

**76F60** k- $\varepsilon$  modeling in turbulence

**76F65** Direct numerical and large eddy simulation of turbulence

76F70 Control of turbulent flows

76F80 Turbulent combustion; reactive turbulence

**76F99** None of the above, but in this section

### 76Gxx General aerodynamics and subsonic flows

76G25 General aerodynamics and subsonic flows

76G99 None of the above, but in this section

#### 76Hxx Transonic flows

76H05 Transonic flows

76H99 None of the above, but in this section

#### 76Jxx Supersonic flows

**76J20** Supersonic flows

76J99 None of the above, but in this section

#### 76Kxx Hypersonic flows

**76K05** Hypersonic flows

76K99 None of the above, but in this section

# 76Lxx Shock waves and blast waves in fluid mechanics [See also 35L67]

76L05 Shock waves and blast waves in fluid mechanics [See also 35L67]

76L99 None of the above, but in this section

# 76Mxx Basic methods in fluid mechanics [See also 65-XX]

**76M10** Finite element methods applied to problems in fluid mechanics

**76M12** Finite volume methods applied to problems in fluid mechanics

76M15 Boundary element methods applied to problems in fluid mechanics

76M20 Finite difference methods applied to problems in fluid mechanics

76M21 Inverse problems in fluid mechanics

76M22 Spectral methods applied to problems in fluid mechanics

76M23 Vortex methods applied to problems in fluid mechanics

 ${\bf 76M25} \ \, {\rm Other \ numerical \ methods \ applied \ to \ problems \ in \ fluid} \\ {\rm mechanics}$ 

76M27 Visualization algorithms applied to problems in fluid mechanics

76M28 Particle methods and lattice-gas methods

**76M30** Variational methods applied to problems in fluid mechanics

76M35 Stochastic analysis applied to problems in fluid mechanics

**76M40** Complex variables methods applied to problems in fluid mechanics

76M45 Asymptotic methods, singular perturbations applied to problems in fluid mechanics

76M50 Homogenization applied to problems in fluid mechanics

**76M55** Dimensional analysis and similarity applied to problems in fluid mechanics

**76M60** Symmetry analysis, Lie group and Lie algebra methods applied to problems in fluid mechanics

76M99 None of the above, but in this section

# 76Nxx Compressible fluids and gas dynamics, general

76N05 Compressible Navier-Stokes equations

**76N10** Existence, uniqueness, and regularity theory for compressible fluids and gas dynamics [See also 35L60, 35L65, 35Q30]

**76N15** Gas dynamics, general

76N17 Viscous-inviscid interaction for compressible fluids and gas dynamics

76N20 Boundary-layer theory for compressible fluids and gas dynamics

76N25 Flow control and optimization for compressible fluids and gas dynamics

**76N30** Waves in compressible fluids

76N99 None of the above, but in this section

# 76Pxx Rarefied gas flows, Boltzmann equation in fluid mechanics [See also 82B40, 82C40, 82D05]

**76P05** Rarefied gas flows, Boltzmann equation in fluid mechanics [See also 82B40, 82C40, 82D05]

76P99 None of the above, but in this section

#### 76Qxx Hydro- and aero-acoustics

76Q05 Hydro- and aero-acoustics

76Q99 None of the above, but in this section

#### 76Rxx Diffusion and convection

**76R05** Forced convection

**76R10** Free convection

**76R50** Diffusion [See also 60J60]

76R99 None of the above, but in this section

# 76Sxx Flows in porous media; filtration; seepage

76S05 Flows in porous media; filtration; seepage

**76S99** None of the above, but in this section

## 76Txx Multiphase and multicomponent flows

76T05 Liquid-liquid two component flows

76T10 Liquid-gas two-phase flows, bubbly flows

76T15 Dusty-gas two-phase flows

76T17 Two gas multicomponent flows

**76T20** Suspensions

**76T25** Granular flows [See also 74C99, 74E20]

**76T30** Three or more component flows

76T99 None of the above, but in this section

#### 76Uxx Rotating fluids

76U05 Rotating fluids

**76U60** Geophysical flows [See also 86A05, 86A10]

**76U65** Rossby waves [See also 86A05, 86A10]

76U99 None of the above, but in this section

# 76Vxx Reaction effects in flows [See also 80A32]

76V05 Reaction effects in flows [See also 80A32]

76V99 None of the above, but in this section

# 76Wxx Magnetohydrodynamics and electrohydrodynamics

76W05 Magnetohydrodynamics and electrohydrodynamics

76W99 None of the above, but in this section

# 76Xxx Ionized gas flow in electromagnetic fields; plasmic flow [See also 82D10]

 $\bf 76X05$  Ionized gas flow in electromagnetic fields; plasmic flow [See also  $82\mathrm{D}10]$ 

76X99 None of the above, but in this section

# 76Yxx Quantum hydrodynamics and relativistic hydrodynamics [See also 82D50, 83C55, 85A30]

**76Y05** Quantum hydrodynamics and relativistic hydrodynamics [See also 82D50, 83C55, 85A30]

76Y99 None of the above, but in this section

# 76Zxx Biological fluid mechanics [See also 74F10, 74L15, 92Cxx]

76Z05 Physiological flows [See also 92C35]

76Z10 Biopropulsion in water and in air

76Z99 None of the above, but in this section

# 78-XX Optics, electromagnetic theory {For quantum optics, see 81V80}

- 78-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to optics and electromagnetic theory
- **78-01** Introductory exposition (textbooks, tutorial papers, etc.) pertaining to optics and electromagnetic theory
- **78-02** Research exposition (monographs, survey articles) pertaining to optics and electromagnetic theory
- 78-03 History of optics and electromagnetic theory [Consider also classification numbers pertaining to Section 01]
- **78-04** Software, source code, etc. for problems pertaining to optics and electromagnetic theory
- **78-05** Experimental work for problems pertaining to optics and electromagnetic theory
- **78-06** Proceedings, conferences, collections, etc. pertaining to optics and electromagnetic theory
- $\bf 78\text{-}10$  Mathematical modeling or simulation for problems pertaining to optics and electromagnetic theory
- 78-11 Research data for problems pertaining to optics and electromagnetic theory

#### 78Axx General

78A02 Foundations in optics and electromagnetic theory

78A05 Geometric optics

78A10 Physical optics

78A15 Electron optics

**78A20** Space charge waves

**78A25** Electromagnetic theory, general

78A30 Electro- and magnetostatics

**78A35** Motion of charged particles

**78A37** Ion traps

78A40 Waves and radiation in optics and electromagnetic theory

**78A45** Diffraction, scattering {For WKB methods see 34E20}

**78A46** Inverse problems (including inverse scattering) in optics and electromagnetic theory

**78A48** Composite media; random media in optics and electromagnetic theory

78A50 Antennas, waveguides in optics and electromagnetic theory

78A55 Technical applications of optics and electromagnetic theory

**78A57** Electrochemistry

 $\bf 78A60$  Lasers, masers, optical bistability, nonlinear optics [See also  $\bf 81V80]$ 

**78A70** Biological applications of optics and electromagnetic theory [See also 91D30, 92C30]

**78A97** Mathematically heuristic optics and electromagnetic theory (must also be assigned at least one other classification number in Section 78)

**78A99** None of the above, but in this section

# 78Mxx Basic methods for problems in optics and electromagnetic theory [See also 65-XX]

78M05 Method of moments applied to problems in optics and electromagnetic theory

78M10 Finite element, Galerkin and related methods applied to problems in optics and electromagnetic theory

**78M12** Finite volume methods, finite integration techniques applied to problems in optics and electromagnetic theory

78M15 Boundary element methods applied to problems in optics and electromagnetic theory

78M16 Multipole methods applied to problems in optics and electromagnetic theory

78M20 Finite difference methods applied to problems in optics and electromagnetic theory

78M22 Spectral, collocation and related methods applied to problems in optics and electromagnetic theory

- **78M25** Other numerical methods applied to problems in optics and electromagnetic theory
- **78M30** Variational methods applied to problems in optics and electromagnetic theory
- **78M31** Monte Carlo methods applied to problems in optics and electromagnetic theory
- **78M32** Neural and heuristic methods applied to problems in optics and electromagnetic theory
- **78M34** Model reduction in optics and electromagnetic theory
- 78M35 Asymptotic analysis in optics and electromagnetic theory
- **78M40** Homogenization in optics and electromagnetic theory
- ${\bf 78M50} \ \, {\rm Optimization \; problems \; in \; optics \; and \; electromagnetic} \\ {\rm theory}$
- 78M99 None of the above, but in this section

# 80-XX Classical thermodynamics, heat transfer {For thermodynamics of solids, see 74A15}

- 80-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to classical thermodynamics
- 80-01 Introductory exposition (textbooks, tutorial papers, etc.) pertaining to classical thermodynamics
- **80-02** Research exposition (monographs, survey articles) pertaining to classical thermodynamics
- **80-03** History of classical thermodynamics [Consider also classification numbers pertaining to Section 01]
- $\bf 80\text{-}04$  Software, source code, etc. for problems pertaining to classical thermodynamics
- 80-05 Experimental work for problems pertaining to classical thermodynamics
- 80-06 Proceedings, conferences, collections, etc. pertaining to classical thermodynamics
- 80-10 Mathematical modeling or simulation for problems pertaining to classical thermodynamics
- 80-11 Research data for problems pertaining to classical thermodynamics

#### 80Axx Thermodynamics and heat transfer

- 80A05 Foundations of thermodynamics and heat transfer
- 80A10 Classical and relativistic thermodynamics
- **80A17** Thermodynamics of continua [See also 74A15]
- $\bf 80A20~$  Diffusive and convective heat and mass transfer, heat flow
- 80A22 Stefan problems, phase changes, etc. [See also 74Nxx]
- 80A23 Inverse problems in thermodynamics and heat transfer

- 80A25 Combustion
- **80A30** Chemical kinetics in thermodynamics and heat transfer [See also 76V05, 92C45, 92E20]
- 80A32 Chemically reacting flows [See also 92C45, 92E20]
- **80A50** Chemistry (general) in thermodynamics and heat transfer [See mainly 92Exx]
- 80A60 Radiative heat transfer
- 80A99 None of the above, but in this section

# 80Mxx Basic methods in thermodynamics and heat transfer [See also 65-XX]

- 80M10 Finite element, Galerkin and related methods applied to problems in thermodynamics and heat transfer
- 80M12 Finite volume methods applied to problems in thermodynamics and heat transfer
- 80M15 Boundary element methods applied to problems in thermodynamics and heat transfer
- 80M20 Finite difference methods applied to problems in thermodynamics and heat transfer
- 80M22 Spectral, collocation and related (meshless) methods applied to problems in thermodynamics and heat transfer
- 80M25 Other numerical methods applied to problems in thermodynamics and heat transfer
- **80M30** Variational methods applied to problems in thermodynamics and heat transfer
- **80M31** Monte Carlo methods applied to problems in thermodynamics and heat transfer
- 80M35 Asymptotic analysis for problems in thermodynamics and heat transfer
- 80M40 Homogenization for problems in thermodynamics and heat transfer
- 80M50 Optimization problems in thermodynamics and heat
- 80M60 Stochastic analysis in thermodynamics and heat transfer
- 80M99 None of the above, but in this section

#### 81-XX Quantum theory

- 81-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to quantum theory
- 81-01 Introductory exposition (textbooks, tutorial papers, etc.) pertaining to quantum theory
- 81-02 Research exposition (monographs, survey articles) pertaining to quantum theory
- 81-03 History of quantum theory [Consider also classification numbers pertaining to Section 01]
- 81-04 Software, source code, etc. for problems pertaining to quantum theory
- 81-05 Experimental work for problems pertaining to quantum theory

- 81-06 Proceedings, conferences, collections, etc. pertaining to quantum theory
- 81-08 Computational methods for problems pertaining to quantum theory
- 81-10 Mathematical modeling or simulation for problems pertaining to quantum theory
- 81-11 Research data for problems pertaining to quantum theory

# 81Pxx Foundations, quantum information and its processing, quantum axioms, and philosophy

- ${f 81P05}$  General and philosophical questions in quantum theory
- 81P10 Logical foundations of quantum mechanics; quantum logic (quantum-theoretic aspects) [See also 03G12, 06C15]
- 81P13 Contextuality in quantum theory
- ${f 81P15}$  Quantum measurement theory, state operations, state preparations
- $\bf 81P16\,$  Quantum state spaces, operational and probabilistic concepts
- 81P17 Quantum entropies
- 81P18 Quantum state tomography, quantum state discrimination
- 81P20 Stochastic mechanics (including stochastic electrodynamics)
- 81P40 Quantum coherence, entanglement, quantum correlations
- 81P42 Entanglement measures, concurrencies, separability criteria
- 81P43 Quantum discord
- 81P45 Quantum information, communication, networks (quantum-theoretic aspects) [See also 94A15, 94A17]
- 81P47 Quantum channels, fidelity [See also 94A40]
- 81P48 LOCC, teleportation, dense coding, remote state operations, distillation
- 81P50 Quantum state estimation, approximate cloning
- 81P55 Special bases (entangled, mutual unbiased, etc.)
- 81P65 Quantum gates
- 81P68 Quantum computation [See also 68Q09] {For algorithmic aspects, see 68Q12}
- 81P70 Quantum coding (general)
- 81P73 Computational stability and error-correcting codes for quantum computation and communication processing
- 81P94 Quantum cryptography (quantum-theoretic aspects) [See also 94A60]
- 81P99 None of the above, but in this section

# 81Qxx General mathematical topics and methods in quantum theory

- 81Q05 Closed and approximate solutions to the Schrödinger, Dirac, Klein-Gordon and other equations of quantum mechanics
- 81Q10 Selfadjoint operator theory in quantum theory, including spectral analysis
- 81Q12 Nonselfadjoint operator theory in quantum theory including creation and destruction operators
- **81Q15** Perturbation theories for operators and differential equations in quantum theory
- 81Q20 Semiclassical techniques, including WKB and Maslov methods applied to problems in quantum theory
- 81Q30 Feynman integrals and graphs; applications of algebraic topology and algebraic geometry [See also 14D05, 32S40]
- **81Q35** Quantum mechanics on special spaces: manifolds, fractals, graphs, lattices [See also 81R20]
- 81Q37 Quantum dots, waveguides, ratchets, etc. [See also 82D20, 82D77]
- 81Q40 Bethe-Salpeter and other integral equations arising in quantum theory
- 81Q50 Quantum chaos [See also 37Dxx]
- 81Q60 Supersymmetry and quantum mechanics
- 81Q65 Alternative quantum mechanics (including hidden variables, etc.)
- 81Q70 differential geometric methods, including holonomy, Berry and Hannay phases, Aharonov-Bohm effect, etc. in quantum theory
- 81Q80 Special quantum systems, such as solvable systems
- 81Q93 Quantum control
- 81Q99 None of the above, but in this section

# 81Rxx Groups and algebras in quantum theory

- 81R05 Finite-dimensional groups and algebras motivated by physics and their representations [See also 20C35, 22E70]
- 81R10 Infinite-dimensional groups and algebras motivated by physics, including Virasoro, Kac-Moody, W-algebras and other current algebras and their representations [See also 17B65, 17B67, 22E65, 22E67, 22E70]
- $\bf 81R12$  Groups and algebras in quantum theory and relations with integrable systems [See also 17Bxx, 37J35]
- 81R15 Operator algebra methods applied to problems in quantum theory [See also 46Lxx, 81T05]
- $\bf 81R20$  Covariant wave equations in quantum theory, relativistic quantum mechanics [See also  $\bf 81Q35$ ]
- 81R25 Spinor and twistor methods applied to problems in quantum theory [See also 32L25]

- 81R30 Coherent states [See also 22E45]; squeezed states in 81T30 String and superstring theories; other extended obquantum theory [See also 81V80]
- 81R40 Symmetry breaking in quantum theory
- 81R50 Quantum groups and related algebraic methods applied to problems in quantum theory [See also 16T20,
- 81R60 Noncommutative geometry in quantum theory
- 81R99 None of the above, but in this section

#### 81Sxx General quantum mechanics and problems of quantization

- 81S05 Commutation relations and statistics as related to quantum mechanics (general)
- 81S07 Uncertainty relations, also entropic
- 81S08 Canonical quantization
- 81S10 Geometry and quantization, symplectic methods [See also 53D50]
- 81S20 Stochastic quantization
- 81S22 Open systems, reduced dynamics, master equations, decoherence [See also 82C31]
- 81S25 Quantum stochastic calculus
- 81S30 Phase-space methods including Wigner distributions, etc. applied to problems in quantum mechanics
- 81S40 Path integrals in quantum mechanics [See also 58D30, 81Q30, 81T18
- 81S99 None of the above, but in this section

#### 81Txx Quantum field theory; related classical field theories [See also 70Sxx]

- 81T05 Axiomatic quantum field theory; operator algebras
- 81T08 Constructive quantum field theory
- 81T10 Model quantum field theories
- 81T11 Higher spin theories
- 81T12 Effective quantum field theories
- 81T13 Yang-Mills and other gauge theories in quantum field theory [See also 53C07, 58E15]
- 81T15 Perturbative methods of renormalization applied to problems in quantum field theory
- 81T16 Nonperturbative methods of renormalization applied to problems in quantum field theory
- 81T17 Renormalization group methods applied to problems in quantum field theory
- 81T18 Feynman diagrams
- 81T20 Quantum field theory on curved space or space-time backgrounds
- 81T25 Quantum field theory on lattices
- 81T27 Continuum limits in quantum field theory
- 81T28 Thermal quantum field theory [See also 82B30]

- jects (e.g., branes) in quantum field theory [See also
- 81T32 Matrix models and tensor models for quantum field theory
- 81T33 Dimensional compactification in quantum field theory
- 81T35 Correspondence, duality, holography (ADS/CFT, gauge/gravity, etc.) [See also 83E05]
- 81T40 Two-dimensional field theories, conformal field theories, etc. in quantum mechanics
- 81T45 Topological field theories in quantum mechanics [See also 57R56, 58Dxx]
- 81T50 Anomalies in quantum field theory
- 81T55 Casimir effect in quantum field theory
- 81T60 Supersymmetric field theories in quantum mechanics
- 81T70 Quantization in field theory; cohomological methods [See also 58D29]
- 81T75 Noncommutative geometry methods in quantum field theory [See also 46L85, 46L87, 58B34]
- 81T99 None of the above, but in this section

#### 81Uxx Quantum scattering theory [See also 34A55, 34L25, 34L40, 35P25, 47A40]

- 81U05 2-body potential quantum scattering theory {For WKB methods, see also 34E20}
- 81U10 *n*-body potential quantum scattering theory
- 81U15 Exactly and quasi-solvable systems arising in quantum theory
- 81U20 S-matrix theory, etc. in quantum theory
- 81U24 Resonances in quantum scattering theory
- 81U26 Tunneling in quantum theory
- 81U30 Dispersion theory, dispersion relations arising in quantum theory
- 81U35 Inelastic and multichannel quantum scattering
- 81U40 Inverse scattering problems in quantum theory
- 81U90 Particle decays in scattering
- 81U99 None of the above, but in this section

#### 81Vxx Applications of quantum theory to specific physical systems

- 81V05 Strong interaction, including quantum chromody-
- 81V10 Electromagnetic interaction; quantum electrodynam-
- 81V15 Weak interaction in quantum theory
- 81V17 Gravitational interaction in quantum theory [See also 83Cxx, 83Exx
- 81V19 Other fundamental interactions in quantum theory
- 81V22 Unified quantum theories

- 81V25 Other elementary particle theory in quantum theory
- 81V27 Anyons
- 81V35 Nuclear physics
- 81V45 Atomic physics
- 81V55 Molecular physics [See also 92E10]
- 81V60 Mono-, di- and multipole moments (EM and other), gyromagnetic relations
- 81V65 Quantum dots as quasi particles [See also 82D20]
- 81V70 Many-body theory; quantum Hall effect
- 81V72 Particle exchange symmetries in quantum theory (general)
- 81V73 Bosonic systems in quantum theory
- 81V74 Fermionic systems in quantum theory
- 81V80 Quantum optics
- 81V99 None of the above, but in this section

# 82-XX Statistical mechanics, structure of matter

- 82-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to statistical mechanics
- 82-01 Introductory exposition (textbooks, tutorial papers, etc.) pertaining to statistical mechanics
- 82-02 Research exposition (monographs, survey articles) pertaining to statistical mechanics
- 82-03 History of statistical mechanics [Consider also classification numbers pertaining to Section 01]
- 82-04 Software, source code, etc. for problems pertaining to statistical mechanics
- 82-05 Experimental work for problems pertaining to statistical mechanics
- 82-06 Proceedings, conferences, collections, etc. pertaining to statistical mechanics
- $\bf 82\text{-}10$  Mathematical modeling or simulation for problems pertaining to statistical mechanics
- 82-11 Research data for problems pertaining to statistical mechanics

#### 82Bxx Equilibrium statistical mechanics

- 82B03 Foundations of equilibrium statistical mechanics
- 82B05 Classical equilibrium statistical mechanics (general)
- 82B10 Quantum equilibrium statistical mechanics (general)
- 82B20 Lattice systems (Ising, dimer, Potts, etc.) and systems on graphs arising in equilibrium statistical mechanics
- 82B21 Continuum models (systems of particles, etc.) arising in equilibrium statistical mechanics
- 82B23 Exactly solvable models; Bethe ansatz

- **82B24** Interface problems; diffusion-limited aggregation arising in equilibrium statistical mechanics
- 82B26 Phase transitions (general) in equilibrium statistical mechanics
- ${f 82B27}$  Critical phenomena in equilibrium statistical mechanics
- 82B28 Renormalization group methods in equilibrium statistical mechanics [See also 81T17]
- 82B30 Statistical thermodynamics [See also 80-XX]
- 82B31 Stochastic methods applied to problems in equilibrium statistical mechanics
- 82B35 Irreversible thermodynamics, including Onsager-Machlup theory [See also 92E20]
- 82B40 Kinetic theory of gases in equilibrium statistical mechanics
- 82B41 Random walks, random surfaces, lattice animals, etc. in equilibrium statistical mechanics [See also 60G50, 82C41]
- **82B43** Percolation [See also 60K35]
- 82B44 Disordered systems (random Ising models, random Schrödinger operators, etc.) in equilibrium statistical mechanics
- 82B99 None of the above, but in this section

# 82Cxx Time-dependent statistical mechanics (dynamic and nonequilibrium)

- 82C03 Foundations of time-dependent statistical mechanics
- 82C05 Classical dynamic and nonequilibrium statistical mechanics (general)
- **82C10** Quantum dynamics and nonequilibrium statistical mechanics (general)
- 82C20 Dynamic lattice systems (kinetic Ising, etc.) and systems on graphs in time-dependent statistical mechanics
- 82C21 Dynamic continuum models (systems of particles, etc.) in time-dependent statistical mechanics
- $\bf 82C22$  Interacting particle systems in time-dependent statistical mechanics [See also 60K35]
- 82C23 Exactly solvable dynamic models in time-dependent statistical mechanics [See also 37K60]
- $\bf 82C24$  Interface problems; diffusion-limited aggregation in time-dependent statistical mechanics
- 82C26 Dynamic and nonequilibrium phase transitions (general) in statistical mechanics
- 82C27 Dynamic critical phenomena in statistical mechanics
- 82C28 Dynamic renormalization group methods applied to problems in time-dependent statistical mechanics [See also 81T17]
- 82C31 Stochastic methods (Fokker-Planck, Langevin, etc.) applied to problems in time-dependent statistical mechanics [See also 60H10]
- 82C32 Neural nets applied to problems in time-dependent statistical mechanics [See also 68T05, 91E40, 92B20]

- 82C35 Irreversible thermodynamics, including Onsager-Machlup theory
- 82C40 Kinetic theory of gases in time-dependent statistical mechanics
- 82C41 Dynamics of random walks, random surfaces, lattice animals, etc. in time-dependent statistical mechanics [See also 60G50]
- 82C43 Time-dependent percolation in statistical mechanics [See also 60K35]
- 82C44 Dynamics of disordered systems (random Ising systems, etc.) in time-dependent statistical mechanics
- 82C70 Transport processes in time-dependent statistical mechanics
- 82C99 None of the above, but in this section

### 82Dxx Applications of statistical mechanics to specific types of physical systems

- 82D03 Statistical mechanical studies in condensed matter (general)
- 82D05 Statistical mechanical studies of gases
- 82D10 Statistical mechanical studies of plasmas
- 82D15 Statistical mechanical studies of liquids
- 82D20 Statistical mechanical studies of solids
- 82D25 Statistical mechanical studies of crystals {For crystallographic group theory, see 20H15}
- 82D30 Statistical mechanical studies of random media, disordered materials (including liquid crystals and spin glasses)
- 82D35 Statistical mechanical studies of metals
- 82D37 Statistical mechanical studies of semiconductors
- 82D40 Statistical mechanical studies of magnetic materials
- 82D45 Statistical mechanical studies of ferroelectrics
- 82D50 Statistical mechanical studies of superfluids
- 82D55 Statistical mechanical studies of superconductors
- 82D60 Statistical mechanical studies of polymers
- 82D75 Nuclear reactor theory; neutron transport
- 82D77 Quantum waveguides, quantum wires [See also 78A50]
- 82D80 Statistical mechanical studies of nanostructures and nanoparticles
- 82D99 None of the above, but in this section

### 82Mxx Basic methods in statistical mechanics [See also 65-XX]

- 82M10 Finite element, Galerkin and related methods applied to problems in statistical mechanics
- 82M12 Finite volume methods applied to problems in statistical mechanics

- 82M15 Boundary element methods applied to problems in statistical mechanics
- 82M20 Finite difference methods applied to problems in statistical mechanics
- 82M22 Spectral, collocation and related (meshless) methods applied to problems in statistical mechanics
- 82M25 Other numerical methods applied to problems in statistical mechanics
- 82M30 Variational methods applied to problems in statistical mechanics
- 82M31 Monte Carlo methods applied to problems in statistical mechanics [See also 65C05]
- 82M36 Computational density functional analysis in statistical mechanics
- 82M37 Computational molecular dynamics in statistical mechanics
- 82M60 Stochastic analysis in statistical mechanics [See also 65C35]
- 82M99 None of the above, but in this section

### 83-XX Relativity and gravitational theory

- 83-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to relativity and gravitational theory
- 83-01 Introductory exposition (textbooks, tutorial papers, etc.) pertaining to relativity and gravitational theory
- 83-02 Research exposition (monographs, survey articles) pertaining to relativity and gravitational theory
- 83-03 History of relativity and gravitational theory [Consider also classification numbers pertaining to Section 01]
- 83-04 Software, source code, etc. for problems pertaining to relativity and gravitational theory
- 83-05 Experimental work for problems pertaining to relativity and gravitational theory
- 83-06 Proceedings, conferences, collections, etc. pertaining to relativity and gravitational theory
- 83-08 Computational methods for problems pertaining to relativity and gravitational theory
- 83-10 Mathematical modeling or simulation for problems pertaining to relativity and gravitational theory
- 83-11 Research data for problems pertaining to relativity and gravitational theory

#### 83Axx Special relativity

- 83A05 Special relativity
- 83A99 None of the above, but in this section

#### 83Bxx Observational and experimental 83Exx Unified, higher-dimensional and suquestions in relativity and gravitational per field theories theory

83B05 Observational and experimental questions in relativity and gravitational theory

83B99 None of the above, but in this section

#### 83Cxx General relativity

83C05 Einstein's equations (general structure, canonical formalism, Cauchy problems)

83C10 Equations of motion in general relativity and gravitational theory

83C15 Exact solutions to problems in general relativity and gravitational theory

83C20 Classes of solutions; algebraically special solutions, metrics with symmetries for problems in general relativity and gravitational theory

83C22 Einstein-Maxwell equations

83C25 Approximation procedures, weak fields in general relativity and gravitational theory

83C27 Lattice gravity, Regge calculus and other discrete methods in general relativity and gravitational theory

83C30 Asymptotic procedures (radiation, news functions,  $\mathcal{H}$ spaces, etc.) in general relativity and gravitational the-

83C35 Gravitational waves

83C40 Gravitational energy and conservation laws; groups of motions

83C45 Quantization of the gravitational field

83C47 Methods of quantum field theory in general relativity and gravitational theory [See also 81T20]

83C50 Electromagnetic fields in general relativity and gravitational theory

83C55 Macroscopic interaction of the gravitational field with matter (hydrodynamics, etc.)

83C56 Dark matter and dark energy

83C57 Black holes

83C60 Spinor and twistor methods in general relativity and gravitational theory; Newman-Penrose formalism

83C65 Methods of noncommutative geometry in general relativity [See also 58B34]

83C75 Space-time singularities, cosmic censorship, etc.

83C80 Analogues of general relativity in lower dimensions

83C99 None of the above, but in this section

#### 83Dxx Relativistic gravitational theories other than Einstein's, including asymmetric field theories

83D05 Relativistic gravitational theories other than Einstein's, including asymmetric field theories

83D99 None of the above, but in this section

83E05 Geometrodynamics and the holographic principle [See also 81T35]

83E15 Kaluza-Klein and other higher-dimensional theories

83E30 String and superstring theories in gravitational theory [See also 81T30]

83E50 Supergravity

83E99 None of the above, but in this section

#### 83Fxx Cosmology

83F05 Cosmology

83F99 None of the above, but in this section

#### 85-XX Astronomy and astrophysics {For celestial mechanics, see 70F15}

85-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to astronomy and astrophysics

85-01 Introductory exposition (textbooks, tutorial papers, etc.) pertaining to astronomy and astrophysics

85-02 Research exposition (monographs, survey articles) pertaining to astronomy and astrophysics

85-03 History of astronomy and astrophysics [Consider also classification numbers pertaining to Section 01]

85-04 Software, source code, etc. for problems pertaining to astronomy and astrophysics

85-05 Experimental work for problems pertaining to astronomy and astrophysics

85-06 Proceedings, conferences, collections, etc. pertaining to astronomy and astrophysics

85-08 Computational methods for problems pertaining to astronomy and astrophysics

85-10 Mathematical modeling or simulation for problems pertaining to astronomy and astrophysics

85-11 Research data for problems pertaining to astronomy and astrophysics

### 85 Axx Astronomy and astrophysics {For celestial mechanics, see 70F15}

- 85A04 General questions in astronomy and astrophysics
- 85A05 Galactic and stellar dynamics
- 85A15 Galactic and stellar structure
- 85A20 Planetary atmospheres
- 85A25 Radiative transfer in astronomy and astrophysics
- 85A30 Hydrodynamic and hydromagnetic problems in astronomy and astrophysics [See also 76Y05]
- 85A35 Statistical astronomy
- 85A40 Cosmology {For relativistic cosmology, see 83F05}
- 85A99 None of the above, but in this section

### 86-XX Geophysics [See also 76U05, 76V05]

- **86-00** General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to geophysics
- 86-01 Introductory exposition (textbooks, tutorial papers, etc.) pertaining to geophysics
- **86-02** Research exposition (monographs, survey articles) pertaining to geophysics
- 86-03 History of geophysics [Consider also classification numbers pertaining to Section 01]
- 86-04 Software, source code, etc. for problems pertaining to geophysics
- **86-05** Experimental work for problems pertaining to geophysics
- **86-06** Proceedings, conferences, collections, etc. pertaining to geophysics
- 86-08 Computational methods for problems pertaining to geophysics
- **86-10** Mathematical modeling or simulation for problems pertaining to geophysics
- **86-11** Research data for problems pertaining to geophysics

### 86Axx Geophysics [See also 76U05, 76V05]

- 86A04 General questions in geophysics
- **86A05** Hydrology, hydrography, oceanography [See also 76Bxx, 76E20, 76Q05, 76Rxx, 76U05]
- 86A08 Climate science and climate modeling
- **86A10** Meteorology and atmospheric physics [See also 76Bxx, 76E20, 76N15, 76Q05, 76Rxx, 76U05]
- 86A15 Seismology (including tsunami modeling), earthquakes
- 86A20 Potentials, prospecting
- 86A22 Inverse problems in geophysics [See also 35R30]

- **86A25** Geo-electricity and geomagnetism [See also 76W05, 78A25]
- 86A30 Geodesy, mapping problems
- 86A32 Geostatistics
- 86A40 Glaciology
- 86A60 Geological problems
- 86A70 Vulcanology; magma and lava flow
- 86A99 None of the above, but in this section

## 90-XX Operations research, mathematical programming

- 90-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to operations research and mathematical programming
- 90-01 Introductory exposition (textbooks, tutorial papers, etc.) pertaining to operations research and mathematical programming
- 90-02 Research exposition (monographs, survey articles) pertaining to operations research and mathematical programming
- 90-03 History of operations research and mathematical programming [Consider also classification numbers pertaining to Section 01]
- 90-04 Software, source code, etc. for problems pertaining to operations research and mathematical programming
- **90-05** Experimental work for problems pertaining to operations research and mathematical programming
- 90-06 Proceedings, conferences, collections, etc. pertaining to operations research and mathematical programming
- 90-08 Computational methods for problems pertaining to operations research and mathematical programming
- 90-10 Mathematical modeling or simulation for problems pertaining to operations research and mathematical programming
- **90-11** Research data for problems pertaining to operations research and mathematical programming

### 90Bxx Operations research and management science

- 90B05 Inventory, storage, reservoirs
- 90B06 Transportation, logistics and supply chain management
- 90B10 Deterministic network models in operations research  $\{For\ network\ control,\ see\ 93B70\}$
- $\bf 90B15$  Stochastic network models in operations research {For network control, see  $93B70\}$
- **90B18** Communication networks in operations research [See also 68M10, 68M12, 68M18, 94A05] {For networks as computational models, see 68Q06}
- 90B20 Traffic problems in operations research

- $\bf 90B22$  Queues and service in operations research [See also  $60K25,\,68M20]$
- 90B25 Reliability, availability, maintenance, inspection in operations research [See also 60K10, 62N05]
- 90B30 Production models
- 90B35 Deterministic scheduling theory in operations research [See also 68M20]
- 90B36 Stochastic scheduling theory in operations research [See also 68M20]
- 90B40 Search theory
- 90B50 Management decision making, including multiple objectives [See also 90C29, 90C31, 91A35, 91B06]
- 90B60 Marketing, advertising [See also 91B60]
- $\bf 90B70$  Theory of organizations, manpower planning in operations research [See also 91D35]
- 90B80 Discrete location and assignment [See also 90C10]
- 90B85 Continuous location
- 90B90 Case-oriented studies in operations research
- 90B99 None of the above, but in this section

### 90Cxx Mathematical programming [See also 49Mxx, 65Kxx]

- 90C05 Linear programming
- 90C06 Large-scale problems in mathematical programming
- 90C08 Special problems of linear programming (transportation, multi-index, data envelopment analysis, etc.)
- 90C09 Boolean programming
- 90C10 Integer programming
- 90C11 Mixed integer programming
- 90C15 Stochastic programming
- 90C17 Robustness in mathematical programming
- 90C20 Quadratic programming
- 90C22 Semidefinite programming
- 90C23 Polynomial optimization
- 90C24 Tropical optimization (e.g., max-plus optimization)
- 90C25 Convex programming
- 90C26 Nonconvex programming, global optimization
- 90C27 Combinatorial optimization
- 90C29 Multi-objective and goal programming
- 90C30 Nonlinear programming
- 90C31 Sensitivity, stability, parametric optimization
- 90C32 Fractional programming
- **90C33** Complementarity and equilibrium problems and variational inequalities (finite dimensions) (aspects of mathematical programming)
- 90C34 Semi-infinite programming

- **90C35** Programming involving graphs or networks [See also 90C27]
- 90C39 Dynamic programming [See also 49L20]
- 90C40 Markov and semi-Markov decision processes
- **90C46** Optimality conditions and duality in mathematical programming [See also 49N15]
- 90C47 Minimax problems in mathematical programming [See also 49K35]
- 90C48 Programming in abstract spaces
- 90C49 Extreme-point and pivoting methods
- 90C51 Interior-point methods
- 90C52 Methods of reduced gradient type
- 90C53 Methods of quasi-Newton type
- 90C55 Methods of successive quadratic programming type
- 90C56 Derivative-free methods and methods using generalized derivatives [See also 49J52]
- 90C57 Polyhedral combinatorics, branch-and-bound, branch-and-cut
- **90C59** Approximation methods and heuristics in mathematical programming
- 90C60 Abstract computational complexity for mathematical programming problems [See also 68Q25]
- 90C70 Fuzzy and other nonstochastic uncertainty mathematical programming
- 90C90 Applications of mathematical programming
- 90C99 None of the above, but in this section

# 91-XX Game theory, economics, finance, and other social and behavioral sciences

- 91-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to game theory, economics, and finance
- 91-01 exposition (textbooks, tutorial papers, etc.) pertaining to game theory, economics, and finance
- 91-02 Research exposition (monographs, survey articles) pertaining to game theory, economics, and finance
- $\bf 91\text{-}03$  History of game theory, economics, and finance [Consider also classification numbers pertaining to Section  $\bf 01$ ]
- 91-04 Software, source code, etc. for problems pertaining to game theory, economics, and finance
- 91-05 Experimental work for problems pertaining to game theory, economics, and finance
- $\bf 91\text{-}06$  Proceedings, conferences, collections, etc. pertaining to game theory, economics, and finance
- **91-08** Computational methods for problems pertaining to game theory, economics, and finance

- **91-10** Mathematical modeling or simulation for problems pertaining to game theory, economics, and finance
- **91-11** Research data for problems pertaining to game theory, economics, and finance

#### 91Axx Game theory

- 91A05 2-person games
- **91A06** *n*-person games, n > 2
- 91A07 Games with infinitely many players
- 91A10 Noncooperative games
- 91A11 Equilibrium refinements
- 91A12 Cooperative games
- 91A14 Potential and congestion games
- 91A15 Stochastic games, stochastic differential games
- 91A16 Mean field games (aspects of game theory) [See also 35Q89, 49N80]
- 91A18 Games in extensive form
- 91A20 Multistage and repeated games
- 91A22 Evolutionary games
- 91A23 Differential games (aspects of game theory) [See also 49N70]
- 91A24 Positional games (pursuit and evasion, etc.) [See also 49N75]
- 91A25 Dynamic games
- 91A26 Rationality and learning in game theory
- 91A27 Games with incomplete information, Bayesian games
- 91A28 Signaling and communication in game theory
- 91A30 Utility theory for games [See also 91B16]
- 91A35 Decision theory for games [See also 62Cxx, 90B50, 91B06]
- 91A40 Other game-theoretic models
- **91A43** Games involving graphs {For games on graphs, see 05C57}
- 91A44 Games involving topology, set theory, or logic
- 91A46 Combinatorial games
- 91A50 Discrete-time games
- 91A55 Games of timing
- 91A60 Probabilistic games; gambling [See also 60G40]
- 91A65 Hierarchical games (including Stackelberg games)
- $\bf 91A68$  Algorithmic game theory and complexity [See also  $\bf 68Qxx,\, 68Wxx]$
- 91A70 Spaces of games
- 91A80 Applications of game theory
- 91A81 Quantum games
- 91A86 Game theory and fuzziness
- 91A90 Experimental studies
- 91A99 None of the above, but in this section

### 91Bxx Mathematical economics {For econometrics, see 62P20}

- 91B02 Fundamental topics (basic mathematics, methodology; applicable to economics in general)
- 91B03 Mechanism design theory
- 91B05 Risk models (general) {For actuarial and financial risk, see 91Gxx}
- 91B06 Decision theory [See also 62Cxx, 90B50, 91A35]
- 91B08 Individual preferences
- 91B10 Group preferences
- 91B12 Voting theory
- 91B14 Social choice
- 91B15 Welfare economics
- 91B16 Utility theory [See also 91A30]
- 91B18 Public goods
- 91B24 Microeconomic theory (price theory and economic markets)
- 91B26 Auctions, bargaining, bidding and selling, and other market models
- 91B32 Resource and cost allocation (including fair division, apportionment, etc.)
- 91B38 Production theory, theory of the firm
- 91B39 Labor markets
- 91B41 Contract theory (moral hazard, adverse selection)
- 91B42 Consumer behavior, demand theory
- 91B43 Principal-agent models
- 91B44 Economics of information
- 91B50 General equilibrium theory
- 91B51 Dynamic stochastic general equilibrium theory
- 91B52 Special types of economic equilibria
- 91B54 Special types of economic markets (including Cournot, Bertrand)
- 91B55 Economic dynamics
- 91B60 Trade models
- 91B62 Economic growth models
- 91B64 Macroeconomic theory (monetary models, models of taxation)
- 91B66 Multisectoral models in economics
- 91B68 Matching models
- 91B69 Heterogeneous agent models
- 91B70 Stochastic models in economics
- 91B72 Spatial models in economics [See also 91D25]
- **91B74** Economic models of real-world systems (e.g., electricity markets, etc.)
- **91B76** Environmental economics (natural resource models, harvesting, pollution, etc.)

- **91B80** Applications of statistical and quantum mechanics to economics (econophysics)
- 91B82 Statistical methods; economic indices and measures [See also 62P20]
- 91B84 Economic time series analysis {For statistical theory of time series, see 62M10}
- 91B86 Mathematical economics and fuzziness
- 91B99 None of the above, but in this section

### 91Cxx Social and behavioral sciences: general topics {For statistics, see 62P25}

- 91C05 Measurement theory in the social and behavioral sciences
- 91C15 One- and multidimensional scaling in the social and behavioral sciences
- 91C20 Clustering in the social and behavioral sciences [See also 62H30]
- 91C99 None of the above, but in this section

### 91Dxx Mathematical sociology (including anthropology)

- 91D10 Models of societies, social and urban evolution
- 91D15 Social learning
- 91D20 Mathematical geography and demography
- 91D25 Spatial models in sociology [See also 91B72]
- 91D30 Social networks; opinion dynamics
- 91D35 Manpower systems in sociology [See also 90B70, 91B39]
- 91D99 None of the above, but in this section

### 91Exx Mathematical psychology {For psychometrics, see 62P15}

- **91E10** Cognitive psychology
- 91E30 Psychophysics and psychophysiology; perception
- 91E40 Memory and learning in psychology [See also 68T05]
- 91E45 Measurement and performance in psychology
- 91E99 None of the above, but in this section

### 91Fxx Other social and behavioral sciences (mathematical treatment)

- 91F10 History, political science
- **91F20** Linguistics [See also 03B65, 68T50]
- 91F99 None of the above, but in this section

### 91Gxx Actuarial science and mathematical finance {For statistics, see 62P05}

- 91G05 Actuarial mathematics
- 91G10 Portfolio theory
- 91G15 Financial markets
- 91G20 Derivative securities (option pricing, hedging, etc.)
- 91G30 Interest rates, asset pricing, etc. (stochastic models)
- 91G40 Credit risk
- 91G45 Financial networks (including contagion, systemic risk, regulation)
- 91G50 Corporate finance (dividends, real options, etc.)
- 91G60 Numerical methods (including Monte Carlo methods)
- 91G70 Statistical methods; risk measures [See also 62P05, 62P20]
- **91G80** Financial applications of other theories [See also 35Q91, 37N40, 49N90, 60J70, 60K10, 60H30, 93E20]
- 91G99 None of the above, but in this section

### 92-XX Biology and other natural sciences

- **92-00** General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to biology
- 92-01 Introductory exposition (textbooks, tutorial papers, etc.) pertaining to biology
- 92-02 Research exposition (monographs, survey articles) pertaining to biology
- $\bf 92\text{-}03\,$  History of biology [Consider also classification numbers pertaining to Section 01]
- $\bf 92\text{-}04$  Software, source code, etc. for problems pertaining to biology
- 92-05 Experimental work for problems pertaining to biology
- 92-06 Proceedings, conferences, collections, etc. pertaining to biology
- **92-08** Computational methods for problems pertaining to biology
- $\bf 92\text{-}10$  Mathematical modeling or simulation for problems pertaining to biology
- 92-11 Research data for problems pertaining to biology

#### 92Bxx Mathematical biology in general

- 92B05 General biology and biomathematics
- 92B10 Taxonomy, cladistics, statistics in mathematical biology
- 92B15 General biostatistics [See also 62P10]
- 92B20 Neural networks for/in biological studies, artificial life and related topics [See also 68T05, 82C32, 94Cxx]
- 92B25 Biological rhythms and synchronization
- 92B99 None of the above, but in this section

92Cxx Physiological, cellular and medical topics	92Fxx Other natural sciences (mathematical treatment)
92C05 Biophysics	92F05 Other natural sciences (mathematical treatment)
92C10 Biomechanics [See also 74L15]	
92C15 Developmental biology, pattern formation	92F99 None of the above, but in this section
92C17 Cell movement (chemotaxis, etc.)	
92C20 Neural biology	02 VV Ct th
92C30 Physiology (general)	93-XX Systems theory; control
92C32 Pathology, pathophysiology	$\{For optimal control, see 49-XX\}$
92C35 Physiological flow [See also 76Z05]	02 00 Characherforn and the distinguish th
92C37 Cell biology	<b>93-00</b> General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to systems and control the-
92C40 Biochemistry, molecular biology	ory
92C42 Systems biology, networks	93-01 Introductory exposition (textbooks, tutorial papers,
<b>92C45</b> Kinetics in biochemical problems (pharmacokinetics, enzyme kinetics, etc.) [See also 80A30]	etc.) pertaining to systems and control theory
92C47 Biosensors (not for medical applications)	93-02 Research exposition (monographs, survey articles) pertaining to systems and control theory
92C50 Medical applications (general)	taining to systems and control theory
$\bf 92C55$ Biomedical imaging and signal processing [See also 44A12, 65R10, 94A08, 94A12]	93-03 History of systems and control theory [Consider also classification numbers pertaining to Section 01]
$92C60$ Medical epidemiology {For theoretical aspects, see $92\mathrm{D}30\}$	93-04 Software, source code, etc. for problems pertaining to systems and control theory
92C70 Microbiology	93-05 Experimental work for problems pertaining to systems and control theory
92C75 Biotechnology	
92C80 Plant biology	09.06 D
92C99 None of the above, but in this section	<b>93-06</b> Proceedings, conferences, collections, etc. pertaining to systems and control theory
92Dxx Genetics and population dynamics	93-08 Computational methods for problems pertaining to
92D10 Genetics and epigenetics {For genetic algebras, see	systems and control theory
17D92}	93-10 Mathematical modeling or simulation for problems
92D15 Problems related to evolution	pertaining to systems and control theory
92D20 Protein sequences, DNA sequences	93-11 Research data for problems pertaining to systems and
92D25 Population dynamics (general)	control theory
<b>92D30</b> Epidemiology {For medical applications, see 92C60}	
92D40 Ecology	93Axx General systems theory
92D45 Pest management	bollan denotal systems theory
92D50 Animal behavior	93A05 Axiomatic systems theory
<b>92D99</b> None of the above, but in this section	93A10 General systems
92Exx Chemistry {For biochemistry, see 92C40}	93A13 Hierarchical systems
92E10 Molecular structure (graph-theoretic methods, meth-	93A14 Decentralized systems
ods of differential topology, etc.)  92E20 Classical flows, reactions, etc. in chemistry [See also	93A15 Large-scale systems
80A30, 80A32]	93A16 Multi-agent systems
<b>92E99</b> None of the above, but in this section	<b>93A99</b> None of the above, but in this section
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93Bxx Controllability, observability, and system structure	93C30 Control/observation systems governed by functional relations other than differential equations (such as hybrid and switching systems)
<ul><li>93B03 Attainable sets, reachability</li><li>93B05 Controllability</li></ul>	93C35 Multivariable systems, multidimensional control systems
93B07 Observability	93C40 Adaptive control/observation systems
<ul><li>93B10 Canonical structure</li><li>93B11 System structure simplification</li></ul>	93C41 Control/observation systems with incomplete information
93B12 Variable structure systems	93C42 Fuzzy control/observation systems
93B15 Realizations from input-output data	93C50 Delay control/observation systems
93B17 Transformations	93C55 Discrete-time control/observation systems
93B18 Linearizations	93C57 Sampled-data control/observation systems
93B20 Minimal systems representations	93C62 Digital control/observation systems
93B24 Topological methods	93C65 Discrete event control/observation systems
93B25 Algebraic methods	$93C70~{\rm Time\text{-}scale}$ analysis and singular perturbations in control/observation systems
93B27 Geometric methods	93C73 Perturbations in control/observation systems
93B28 Operator-theoretic methods [See also 47A48, 47A57,	93C80 Frequency-response methods in control theory
47B35, 47N70]  93B30 System identification	93C83 Control/observation systems involving computers (process control, etc.)
93B35 Sensitivity (robustness)	93C85 Automated systems (robots, etc.) in control theory
93B36 $H^{\infty}$ -control	[See also 68T40, 70B15, 70Q05]
93B45 Model predictive control	93C95 Application models in control theory
93B47 Iterative learning control	93C99 None of the above, but in this section
93B50 Synthesis problems	02Dyry Stability of control systems
$\bf 93B51$ Design techniques (robust design, computer-aided design, etc.)	<ul><li>93Dxx Stability of control systems</li><li>93D05 Lyapunov and other classical stabilities (Lagrange,</li></ul>
93B52 Feedback control	Poisson, $L^p, l^p$ , etc.) in control theory
93B53 Observers	93D09 Robust stability
93B55 Pole and zero placement problems	93D10 Popov-type stability of feedback systems
93B60 Eigenvalue problems	93D15 Stabilization of systems by feedback
93B70 Networked control	93D20 Asymptotic stability in control theory
93B99 None of the above, but in this section	93D21 Adaptive or robust stabilization
	93D22 Exponential stability
93Cxx Model systems in control theory	93D25 Input-output approaches in control theory
93C05 Linear systems in control theory	93D30 Lyapunov and storage functions
93C10 Nonlinear systems in control theory	93D40 Finite-time stability
$\bf 93C15$ Control/observation systems governed by ordinary differential equations [See also $34H05]$	<ul><li>93D50 Consensus</li><li>93D99 None of the above, but in this section</li></ul>
$\bf 93C20$ Control/observation systems governed by partial differential equations	93Exx Stochastic systems and control
93C23 Control/observation systems governed by functional-	93E03 Stochastic systems in control theory (general)
differential equations [See also 34K35]  93C25 Control/observation systems in abstract spaces	93E10 Estimation and detection in stochastic control theory [See also 60G35]
93C27 Impulsive control/observation systems	93E11 Filtering in stochastic control theory [See also 60G35]
93C28 Positive control/observation systems	93E12 Identification in stochastic control theory
93C29 Boolean control/observation systems	93E14 Data smoothing in stochastic control theory

- 93E15 Stochastic stability in control theory
- 93E20 Optimal stochastic control [See also 49J55, 49K45]
- 93E24 Least squares and related methods for stochastic control systems
- 93E35 Stochastic learning and adaptive control
- 93E99 None of the above, but in this section

### 94-XX Information and communication theory, circuits

- 94-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to information and communication theory
- 94-01 Introductory exposition (textbooks, tutorial papers, etc.) pertaining to information and communication theory
- 94-02 Research exposition (monographs, survey articles) pertaining to information and communication theory
- 94-03 History of information and communication theory [Consider also classification numbers pertaining to Section 01]
- **94-04** Software, source code, etc. for problems pertaining to information and communication theory
- **94-05** Experimental work for problems pertaining to information and communication theory
- **94-06** Proceedings, conferences, collections, etc. pertaining to information and communication theory
- 94-08 Computational methods for problems pertaining to information and communication theory
- **94-10** Mathematical modeling or simulation for problems pertaining to information and communication theory
- 94-11 Research data for problems pertaining to information and communication theory

#### 94Axx Communication, information

- 94A05 Communication theory [See also 60G35, 90B18]
- $\bf 94A08$  Image processing (compression, reconstruction, etc.) in information and communication theory [See also  $\bf 68U10$ ]
- 94A11 Application of orthogonal and other special functions
- 94A12 Signal theory (characterization, reconstruction, filtering, etc.)
- $\bf 94A13$  Detection theory in information and communication theory
- 94A14 Modulation and demodulation in information and communication theory
- 94A15 Information theory (general) [See also 62B10, 81P45]
- 94A16 Informational aspects of data analysis and big data [See also 62R07, 68T09] {For homological aspects, see  $55N31\}$

- 94A17 Measures of information, entropy
- ${f 94A20}$  Sampling theory in information and communication theory
- 94A24 Coding theorems (Shannon theory)
- 94A29 Source coding [See also 68P30]
- 94A34 Rate-distortion theory in information and communication theory
- 94A40 Channel models (including quantum) in information and communication theory [See also 81P47]
- 94A45 Prefix, length-variable, comma-free codes [See also 20M35, 68Q45]
- 94A50 Theory of questionnaires
- 94A55 Shift register sequences and sequences over finite alphabets in information and communication theory
- **94A60** Cryptography [See also 11T71, 14G50, 68P25, 81P94]
- 94A62 Authentication, digital signatures and secret sharing [See also 81P94]
- 94A99 None of the above, but in this section

### 94Bxx Theory of error-correcting codes and error-detecting codes

- 94B05 Linear codes, general
- 94B10 Convolutional codes
- 94B12 Combined modulation schemes (including trellis codes) in coding theory
- 94B15 Cyclic codes
- 94B20 Burst-correcting codes
- 94B25 Combinatorial codes
- 94B27 Geometric methods (including applications of algebraic geometry) applied to coding theory [See also 11T71, 14G50]
- 94B30 Majority codes
- 94B35 Decoding
- 94B40 Arithmetic codes [See also 11T71, 14G50]
- 94B50 Synchronization error-correcting codes
- 94B60 Other types of codes
- 94B65 Bounds on codes
- 94B70 Error probability in coding theory
- 94B75 Applications of the theory of convex sets and geometry of numbers (covering radius, etc.) to coding theory [See also 11H31, 11H71]
- 94B99 None of the above, but in this section

#### 94Cxx Circuits, networks [See also 68Q06]

- 94C05 Analytic circuit theory
- 94C11 Switching theory, applications of Boolean algebras to circuits and networks
- 94C12 Fault detection; testing in circuits and networks
- **94C15** Applications of graph theory to circuits and networks [See also 05Cxx, 68R10]
- 94C30 Applications of design theory to circuits and networks [See also 05Bxx]
- 94C60 Circuits in qualitative investigation and simulation of models
- 94C99 None of the above, but in this section

### 94Dxx Miscellaneous topics in information and communication theory

- 94D05 Fuzzy sets and logic (in connection with information, communication, or circuits theory) [See also 03B52, 03E72, 28E10]
- **94D10** Boolean functions [See also 06E30] {For connections with circuits and networks, see 94C11}
- 94D99 None of the above, but in this section

#### 97-XX Mathematics education

- 97-00 General reference works (handbooks, dictionaries, bibliographies, etc.) pertaining to mathematics education
- 97-01 Introductory exposition (textbooks, tutorial papers, etc.) pertaining to mathematics education
- 97-02 Research exposition (monographs, survey articles) pertaining to mathematics education
- 97-03 History of mathematics education [Consider also classification numbers pertaining to Section 01]
- ${f 97\text{-}06}$  Proceedings, conferences, collections, etc. pertaining to mathematics education
- ${f 97\text{-}11}$  Research data for problems pertaining to mathematics education

### 97Axx History and society (aspects of mathematics education)

- **97A30** History in mathematics education {For mathematics history, see 01-XX; for biographies, see 01A70; for history of mathematics education, see 97-03}
- 97A40 Mathematics education and society {For sociology (and profession) of mathematics, see 01A80}
- 97A99 None of the above, but in this section

#### 97Bxx Educational policy and systems

- 97B10 Mathematics educational research and planning
- 97B20 Educational policy for general education
- 97B30 Educational policy for vocational education
- 97B40 Educational policy for higher education
- 97B50 Mathematics teacher education
- 97B60 Educational policy for adult and further education
- 97B70 Syllabuses, educational standards
- 97B99 None of the above, but in this section

### 97Cxx Psychology of mathematics education, research in mathematics education

- 97C10 Comprehensive works on psychology of mathematics education
- 97C20 Affective behavior and mathematics education
- 97C30 Cognitive processes, learning theories (aspects of mathematics education)
- **97C40** Intelligence and aptitudes (aspects of mathematics education)
- 97C50 Language and verbal communities (aspects of mathematics education)
- 97C60 Sociological aspects of learning (aspects of mathematics education)
- 97C70 Teaching-learning processes in mathematics education
- 97C99 None of the above, but in this section

### 97Dxx Education and instruction in mathematics

- 97D10 Comprehensive works and comparative studies on education and instruction in mathematics
- 97D20 Philosophical and theoretical contributions (maths didactics)
- $\bf 97D30$  Objectives and goals of mathematics teaching
- 97D40 Mathematics teaching methods and classroom techniques
- ${f 97D50}$  Teaching mathematical problem solving and heuristic strategies
- $\bf 97D60$  Student assessment, achievement control and rating (aspects of mathematics education)
- 97D70 Learning difficulties and student errors (aspects of mathematics education)
- 97D80 Mathematics teaching units and draft lessons
- 97D99 None of the above, but in this section

### 97Exx Education of foundations of mathematics

97E10 Comprehensive works on education of foundations of mathematics

97E20 Philosophy and mathematics (educational aspects)

97E30 Logic (educational aspects)

97E40 Language of mathematics (educational aspects)

97E50 Reasoning and proving in the mathematics classroom

97E60 Sets, relations, set theory (educational aspects)

97E99 None of the above, but in this section

### 97Fxx Education of arithmetic and number theory

97F10 Comprehensive works on education of arithmetic and number theory

97F20 Pre-numerical stage, concept of numbers

97F30 Natural numbers (educational aspects)

97F40 Integers, rational numbers (educational aspects)

97F50 Real numbers, complex numbers (educational aspects)

97F60 Number theory (educational aspects)

97F70 Measures and units (educational aspects)

97F80 Ratio and proportion, percentages (educational aspects)

97F90 Real life mathematics, practical arithmetic (educational aspects)

97F99 None of the above, but in this section

#### 97Gxx Geometry education

97G10 Comprehensive works on geometry education

97G20 Informal geometry (educational aspects)

97G30 Area and volume (educational aspects)

97G40 Plane and solid geometry (educational aspects)

97G50 Transformation geometry (educational aspects)

97G60 Plane and spherical trigonometry (educational aspects)

97G70 Analytic geometry, vector algebra (educational aspects)

97G80 Descriptive geometry (educational aspects)

97G99 None of the above, but in this section

#### 97Hxx Algebra education

97H10 Comprehensive works on algebra education

97H20 Elementary algebra (educational aspects)

97H30 Equations and inequalities (educational aspects)

97H40 Groups, rings, fields (educational aspects)

97H50 Ordered algebraic structures (educational aspects)

97H60 Linear algebra (educational aspects)

97H99 None of the above, but in this section

#### 97Ixx Analysis education

97I10 Comprehensive works on analysis education

97I20 Mappings and functions (educational aspects)

97I30 Sequences and series (educational aspects)

97I40 Differential calculus (educational aspects)

**97I50** Integral calculus (educational aspects)

97I60 Functions of several variables (educational aspects)

**97I70** Functional equations (educational aspects)

97I80 Complex analysis (educational aspects)

97199 None of the above, but in this section

### 97Kxx Education of combinatorics, graph theory, probability theory, and statistics

97K10 Comprehensive works on combinatorics, graph theory, and probability (educational aspects)

97K20 Combinatorics (educational aspects)

97K30 Graph theory (educational aspects)

97K40 Descriptive statistics (educational aspects)

97K50 Probability theory (educational aspects)

97K60 Distributions and stochastic processes (educational aspects)

97K70 Foundations and methodology of statistics (educational aspects)

97K80 Applied statistics (educational aspects)

97K99 None of the above, but in this section

### 97Mxx Education of mathematical modeling and applications of mathematics

97M10 Modeling and interdisciplinarity (aspects of mathematics education)

97M20 Mathematics in vocational training and career education

 $\bf 97M30$  Financial and insurance mathematics (aspects of mathematics education)

97M40 Operations research, economics (aspects of mathematics education)

 $\bf 97M50$  Physics, astronomy, technology, engineering (aspects of mathematics education)

97M60 Biology, chemistry, medicine (aspects of mathematics education)

97M70 Behavioral and social sciences (aspects of mathematics education)

**97M80** Arts, music, language, architecture (aspects of mathematics education)

97M99 None of the above, but in this section

### 97Nxx Education of numerical mathematics

- 97N10 Comprehensive works education of numerical mathematics
- 97N20 Rounding, estimation, theory of errors (educational aspects)
- 97N30 Numerical algebra (educational aspects)
- 97N40 Numerical analysis (educational aspects)
- 97N50 Interpolation and approximation (educational aspects)
- ${\bf 97N60} \ \ {\rm Mathematical \ programming \ (educational \ aspects)}$
- 97N70 Discrete mathematics (educational aspects)
- 97N80 Mathematical software, computer programs (educational aspects)
- 97N99 None of the above, but in this section

### 97Pxx Computer science (educational aspects)

- 97P10 Comprehensive works on computer science (educational aspects)
- 97P20 Theoretical computer science (educational aspects)
- 97P30 Systems, databases (educational aspects)
- 97P40 Programming languages (educational aspects)
- 97P50 Programming techniques (educational aspects)

- 97P80 Artificial intelligence (educational aspects)
- 97P99 None of the above, but in this section

#### 97Uxx Educational material and media and educational technology in mathematics education

- 97U10 Comprehensive works on educational material and media and educational technology in mathematics education
- 97U20 Textbooks, textbook research (aspects of mathematics education)
- 97U30 Teachers' manuals and planning aids (aspects of mathematics education)
- 97U40 Problem books, competitions, examinations (aspects of mathematics education)
- 97U50 Computer-assisted instruction, e-learning (aspects of mathematics education)
- 97U60 Manipulative materials (aspects of mathematics education)
- 97U70 Technological tools, calculators (aspects of mathematics education)
- 97U80 Audiovisual media (aspects of mathematics education)
- 97U99 None of the above, but in this section