the set  $\{1, 2, \ldots\}$  of all natural numbers  $\mathbb{N}$  $\mathbb{N}_0$ the set  $\{0, 1, 2, \ldots\}$  of all non-negative integers  $\mathbb{Z}$ the set of all integers  $\mathbb{Q}$ the set of all rationals  $\mathbb R$ the set of all reals  $\mathbb{C}$ the set of all complex numbers the unit ball of a normed space  $X, B_X = \{x \in X : ||x|| \le 1\}$  $B_X$ the unit sphere of a normed space  $X, S_X = \{x \in X : ||x|| = 1\}$  $S_X$  $X^*$ the dual of a normed space X|A|the cardinality of a set A $\mathbb{1}_A$ the characteristic function of a set Athe identity operator acting on a Banach space X $I_X$ ω the first infinite ordinal number [n]the set  $\{1, 2, ..., n\}$  $\mathcal{P}\Gamma$ the family of all subsets of a given set  $\Gamma$  $\mathcal{P}_{\infty}\Gamma$ the family of all infinite subsets of a given set  $\Gamma$  $\mathcal{F}_n\Gamma$ the family of all *n*-element subsets of  $\Gamma$  $\mathcal{F}\Gamma$ the family of all finite subsets of  $\Gamma$  $\Pi(\Gamma)$ the family of all partitions of  $\Gamma$  $\overline{A}$ the closure of A in the norm topology  $\overline{A}^w$ the closure of A in the weak topology  $\overline{A}^{w*}$ the closure of A in the weak<sup>\*</sup> topology the linear space generated by a set A $\operatorname{span}(A)$ the norm closure of  $\operatorname{span}(A)$  $\overline{\operatorname{span}}(A)$  $\overline{\operatorname{span}}^{w*}(A)$ the closure of  $\operatorname{span}(A)$  in the weak<sup>\*</sup> topology  $\operatorname{conv}(A)$ the convex hull of a set A $\overline{\mathrm{conv}}(A)$ the norm closure of conv(A) $\operatorname{dist}(x, A)$ the distance between a point x and a set Athe *n*th canonical unit vector in a sequence space (unless otherwise stated)  $e_n$  $e_n^*$ the *n*th coordinate functional on a sequence space (unless otherwise stated)  $X \oplus Y$ the direct sum of Banach spaces X and Y, equipped with any norm which is equivalent to  $||(x, y)||_{\infty} := \max\{||x||, ||y||\}$ the Banach space of all scalar functions x defined on  $\Gamma$  such that for every  $c_0(\Gamma)$  $\varepsilon > 0$  there is a finite set  $F \subset \Gamma$  with  $|x(\gamma)| < \varepsilon$  for each  $\gamma \in \Gamma \setminus F$ , equipped with the supremum norm for  $p \in [1, \infty)$ , the Banach space of all scalar functions x defined on  $\Gamma$  such  $\ell_p(\Gamma)$ that  $||x||_p := \left(\sum_{\gamma \in \Gamma} |x(\gamma)|^p\right)^{1/p} < \infty$ , equipped with the norm  $||\cdot||_p$ the Banach space of all scalar bounded functions defined on  $\Gamma$ , equipped  $\ell_{\infty}(\Gamma)$ with the supremum norm  $||x||_{\infty} := \sup\{|x(\gamma)|: \gamma \in \Gamma\}$ operator = bounded and linear operator (unless otherwise stated) *isomorphism* = bounded, linear and bijective operator between Banach spaces *functional* = continuous, linear functional (unless otherwise stated) isometry = linear isometry (unless otherwise stated) = bounded, injective, linear operator with a closed range embedding = closed, linear subspace (unless we talk about a dense subspace) subspace